

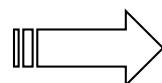
# プラズマ中のダスト粒子挙動の シミュレーション

21 July, 2011

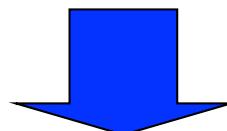
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A.Yu.Pigarov, R.D.Smirnov, S.I.Krasheninnikov (UCSD),  
N.Asakura, H.Takenaga (JAEA),  
N.Ohno (Nagoya Univ.), Y. Uesugi (Kanazawa Univ.)**

## *Background-1*

- **Dust** in fusion devices is one of the most critical issues, mainly related to the safety hazard.
  - Enhancement of the tritium inventory
  - Risk of explosion at an accidental air or coolant leakage
- **Dust** may be an important contributor of impurities in the main and SOL plasmas in some devices  
(← The impurities may increase radiation loss )



Numerical simulation is a powerful tool nowadays for basic understanding of **dust particle formation and its transport in edge plasma condition of fusion devices.**



-Ion drag force & dust potential, etc  
-Electron emission  
-Improved to treat various materials

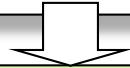
**DUSTT code has been developed by Dr.A.Pigarov, UCSD  
cooperating UEDGE code (Dr.T.Rognlien, LLNL)**

## *-Present work*

### **Calculation of behaviors of C dust particles in a plasma in JT-60U configuration with DUSTT code**

- Behavior of individual dust launched  
from different wall positions with different initial radii and  
different initial velocities.**
- Statistical analysis of dust particles  
with different initial velocities.**

1-100 micron



**-Calculation of trajectories, temporal evolution in  
temperature, mass, electronic charge, velocity etc of dust  
particles in a plasma in JT-60U.**

Other examples:

**Behavior of ablating particles in plasmas**

- Spallation particle flight from polymer bulk irradiated by plasmas**
- Evaporation simulation of polymer particle**

## *Underlying physics equations of dust particles in a plasma-1*

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### -Equation of motion of dust particle:

$$\frac{4}{3}\pi r_d^3 \rho_d \frac{d\mathbf{v}_d}{dt} = \zeta (F_c + F_o) + \mathbf{F}_a - eZ_d \mathbf{E} + M_d \mathbf{g}$$

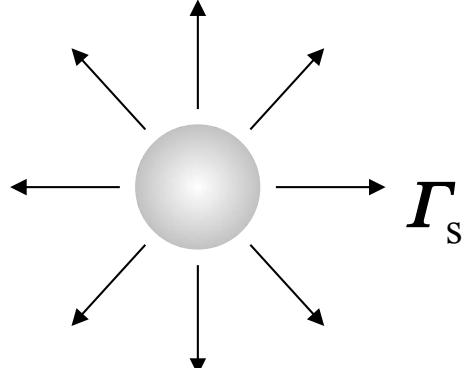
-Ion friction forces  
 -Neutral particle friction forces  
 -Shape factor(=1.0 for sphere)

Spinning effect  
 is neglected  
 -Gravity  
 -Electric field force  
 due to charging of the dust

### -Equation of mass of dust particle:

$$\frac{d}{dt} \left( \rho_d \frac{4}{3}\pi r_d^3 \right) = -4\pi r_d^2 m_s \Gamma_s$$

-Mass flux due to  
 physical & chemical  
 sputtering, RES,  
 thermal evaporation/sublimation



Uniform mass loss  
 in radial direction  
 → Dust shape is always sphere.

## *Underlying physics equations of dust particles in a plasma-2*

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-Equation of energy (uniform temperature profile assumption inside a dust particle):

$$\frac{d}{dt} \left( \rho_d \frac{4}{3} \pi r_d^3 \int_0^{T_d} c_{pd} dT \right) \\ (T_d < T_m, \quad T_m < T_d)$$

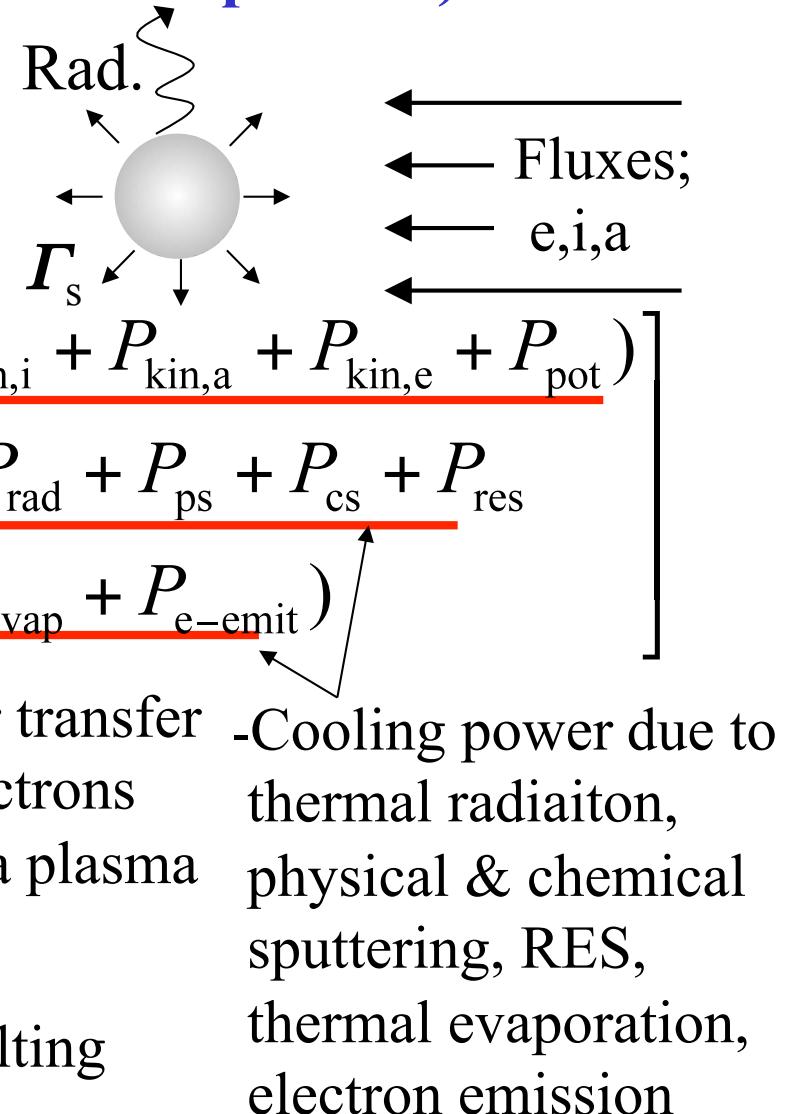
-Liquid fraction

$$\frac{d}{dt} \left( \rho_d \frac{4}{3} \pi r_d^3 H_m \eta_\ell \right) \\ (T_d = T_m)$$

For melting process

} = 4\pi r\_d^2 \left[ \begin{array}{l} (P\_{kin,i} + P\_{kin,a} + P\_{kin,e} + P\_{pot}) \\ - (P\_{rad} + P\_{ps} + P\_{cs} + P\_{res}) \\ + P\_{evap} + P\_{e-emit} \end{array} \right]

-Latent heat for melting

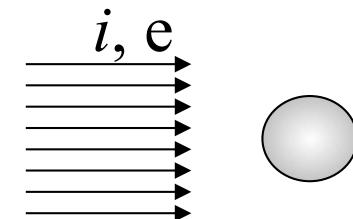


## *Calculation of floating potential of dust from quasi-equilibrium (1)*

### -Quasi-equilibrium condition for dust:

$$\Gamma_e = \Gamma_i + \Gamma_e^{\text{TE}} + \Gamma_e^{\text{SEE}} \quad \phi_d[\text{V}] = -\frac{T_i[\text{eV}]}{e} \chi = \frac{Z_d e^2}{r_d}$$

(Floating potential of dust)



### For negative floating potential of dust

-Electron flux from thermoionic emission  
(Richardson-Dushman's equation):

$$\Gamma_e^{\text{TE}} = \sigma_{\text{sb}} \left( \frac{4\pi m_e (kT_d)^2}{h^3} \right) \exp \left( -\frac{W_d}{kT_d} \right)$$

-Electron flux from plasma:

$$\Gamma_e = \frac{1}{4} n_e \left( \frac{8T_e}{\pi m_e} \right)^{1/2} \exp \left[ -\left( \frac{T_i}{T_e} \right) \chi \right]$$

-Ion flux from plasma:

$$\Gamma_i = n_e \left( \frac{2T_i}{m_i} \right)^{1/2} \frac{u}{4} \left\{ \left( 1 + \frac{1}{2u^2} + \frac{\chi}{u^2} \right) \text{erf}(u) + \frac{e^{-u^2}}{u\sqrt{\pi}} \right\}$$

Relative drift velocity:

$$u = \frac{|v_i - v_d|}{v_n} = \frac{|v_i - v_d|}{\left( \frac{2T_i}{m_i} \right)^{1/2}}$$

If  $\Gamma_e^{\text{TE}}$  or  $\Gamma_e^{\text{SEE}}$  is high,  
the floating potential  
of dust can be positive.

## *Calculation of floating potential of dust from quasi-equilibrium (2)*

-Quasi-equilibrium condition for dust:

$$\Gamma_e = \Gamma_i + \Gamma_e^{\text{TE}} + \Gamma_e^{\text{SEE}}$$

$$\phi_d[\text{V}] = -\frac{T_i[\text{eV}]}{e} \chi = \frac{Z_d e^2}{r_d}$$

**For positive floating potential of dust**

-Electron flux from thermoionic emission

(Richardson-Dushman's equation):

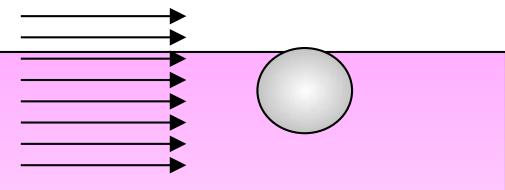
$$\Gamma_e^{\text{TE}} = \sigma_{\text{sb}} \left( \frac{4\pi m_e (kT_d)^2}{h^3} \right) \exp \left( -\frac{W_d}{kT_d} \right)$$

-Electron flux from plasma:

$$\Gamma_e = \frac{1}{4} n_e \left( \frac{8T_e}{\pi m_e} \right)^{\frac{1}{2}} \left[ 1 - \left( \frac{T_i}{T_e} \right) \chi \right]$$

-Ion flux from plasma:

$$\Gamma_i = n_e \left( \frac{2T_i}{m_i} \right)^{\frac{1}{2}} \frac{u}{8} \left\{ \begin{aligned} & \left( 1 + \frac{1}{2u^2} + \frac{\chi}{u^2} \right) \left[ \text{erf}(u + \sqrt{-\chi}) + \text{erf}(u - \sqrt{-\chi}) \right] \\ & + \frac{1}{u^2 \sqrt{\pi}} \left[ (u + \sqrt{-\chi}) \exp[-(u + \sqrt{-\chi})^2] + (u - \sqrt{-\chi}) \exp[-(u - \sqrt{-\chi})^2] \right] \end{aligned} \right\}$$

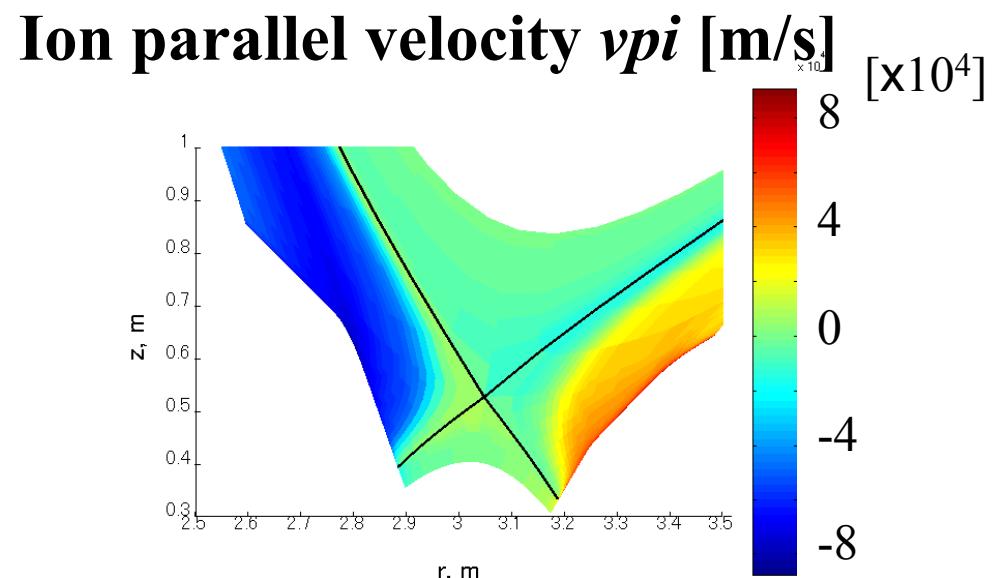
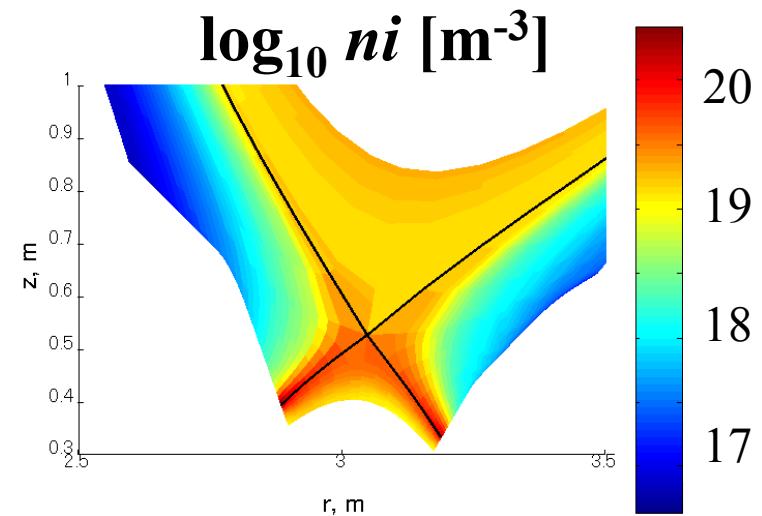
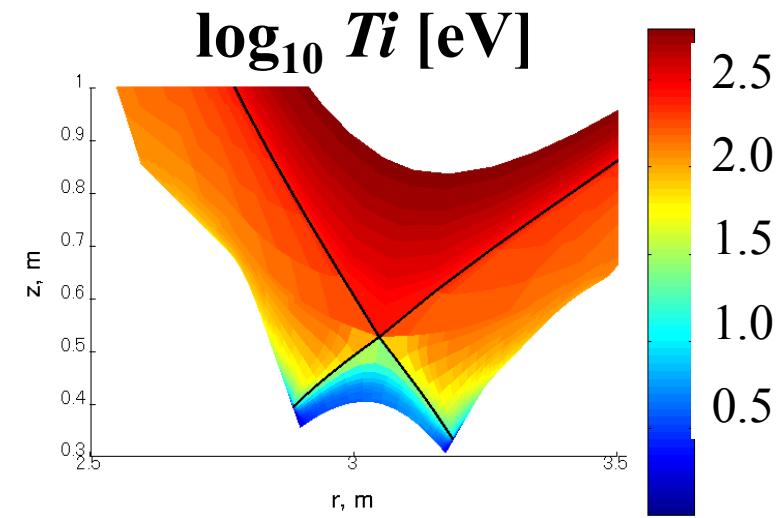
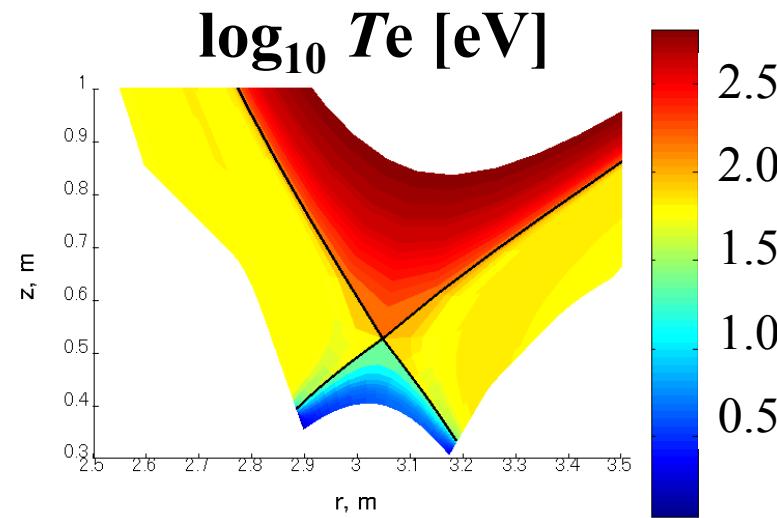


Relative drift velocity:

$$u = \frac{|v_i - v_d|}{v_n} = \frac{|v_i - v_d|}{\left( \frac{2T_i}{m_i} \right)^{1/2}}$$

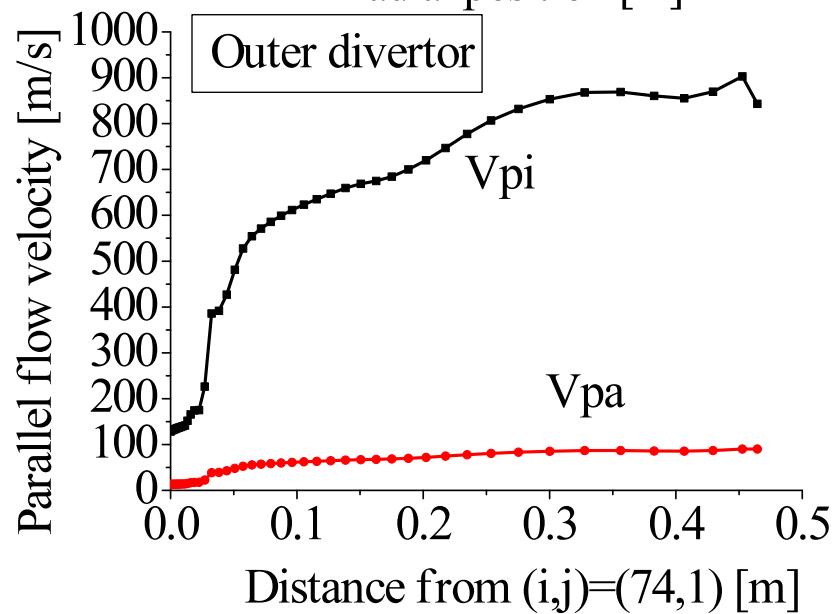
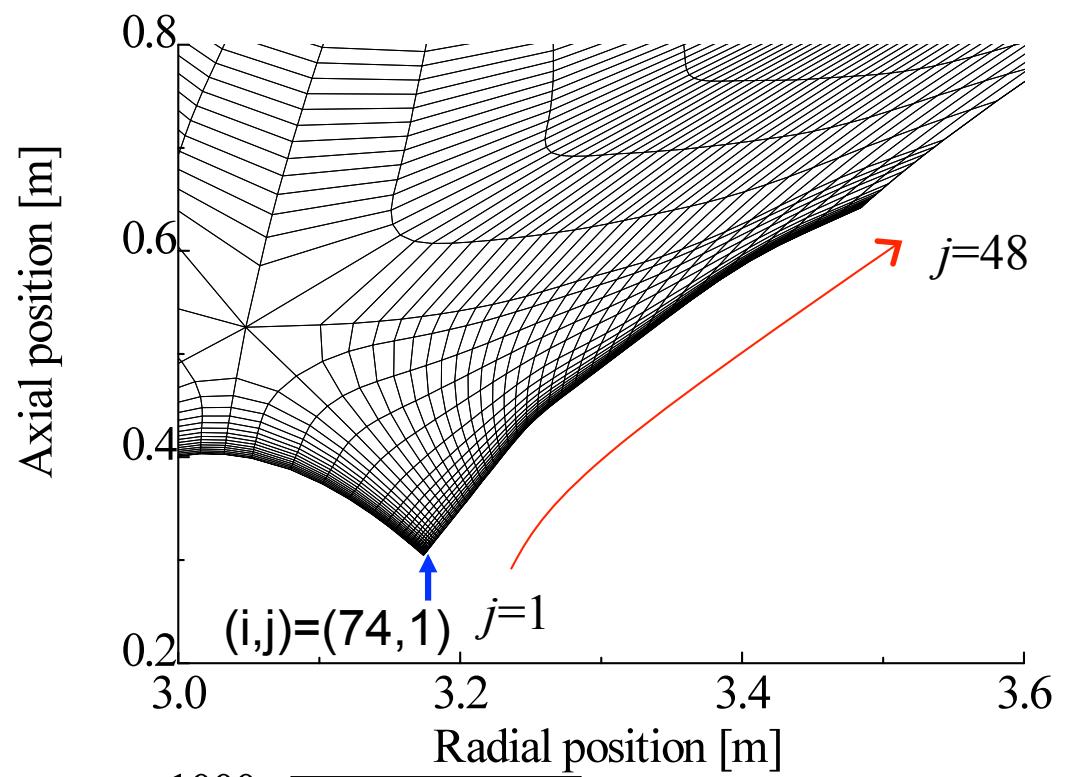
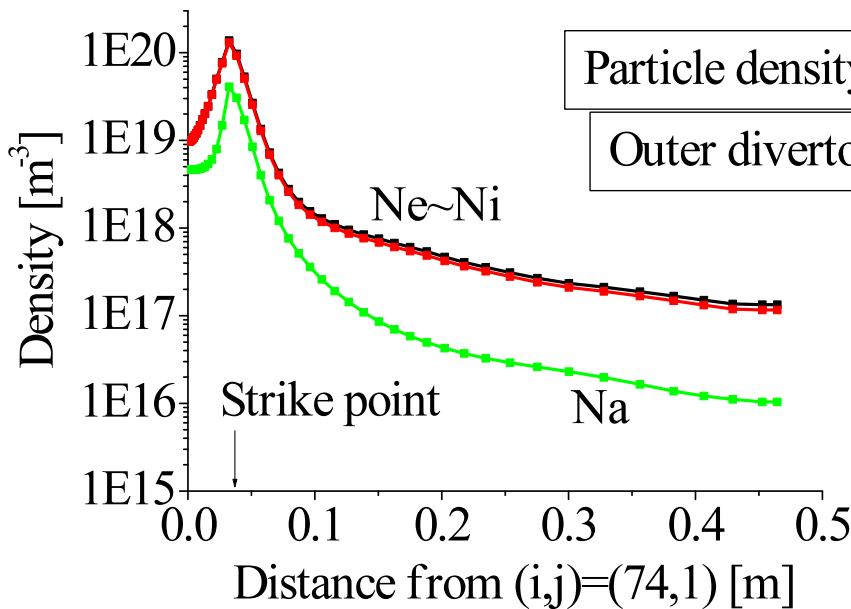
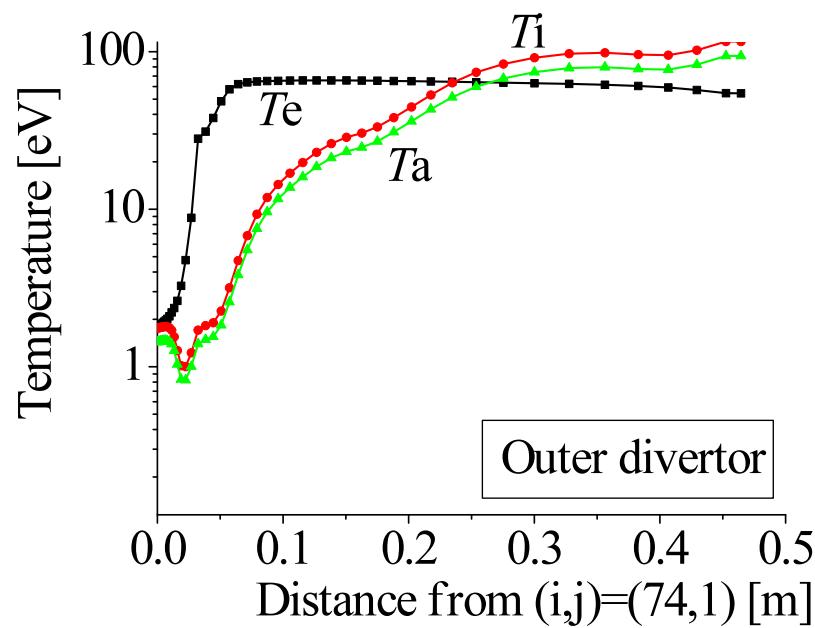
## *Parameters of background plasma calculated with UEDGE code*

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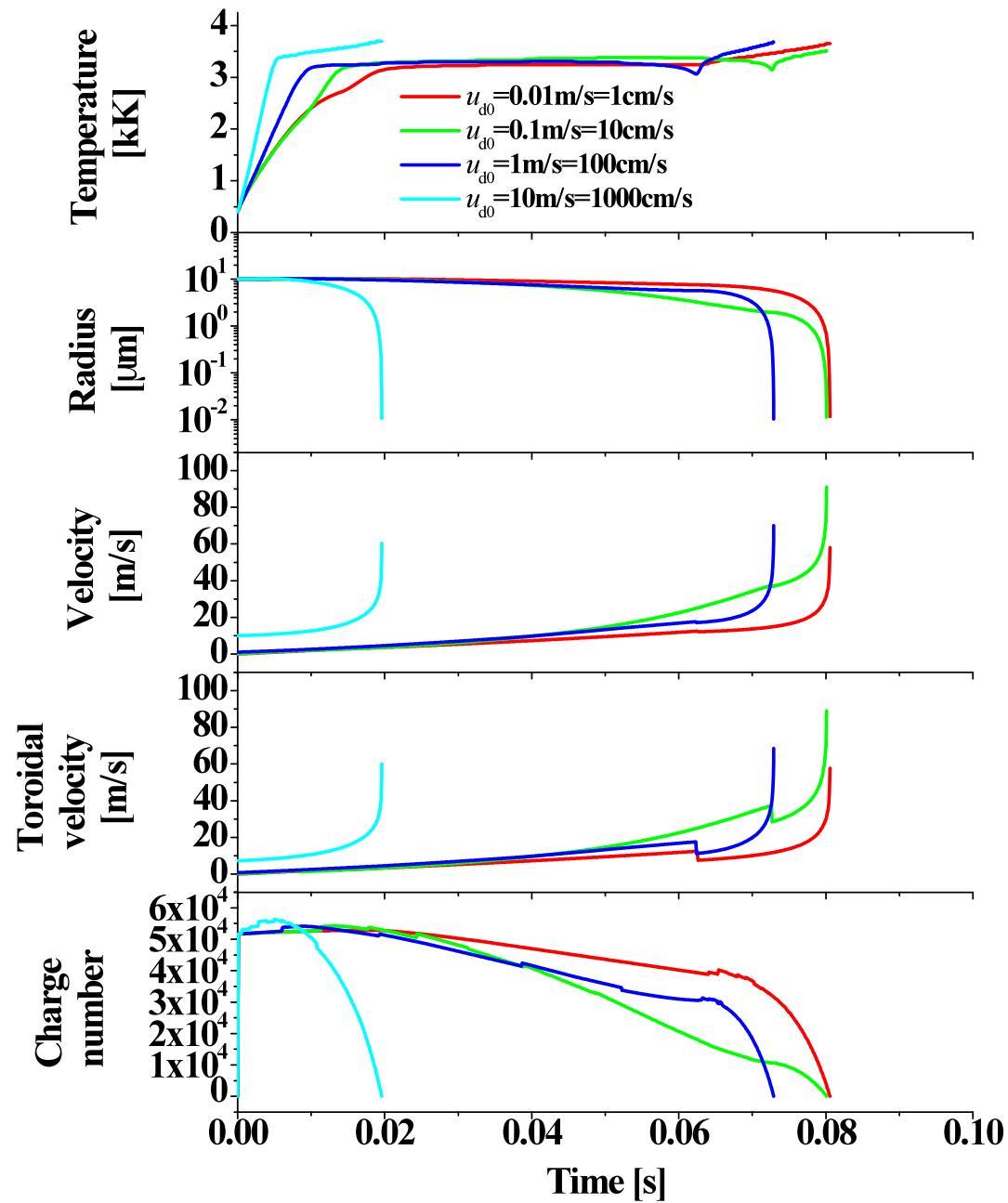
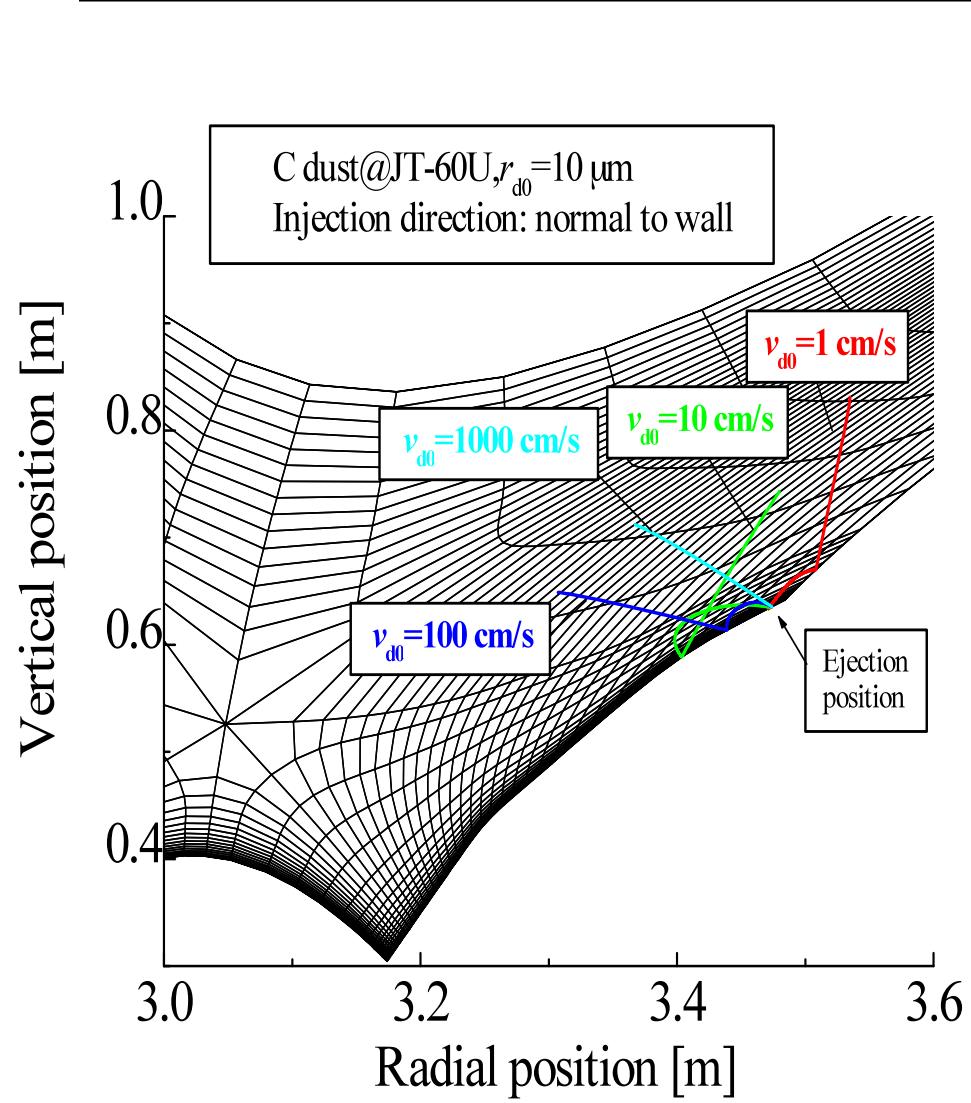


Calculated by Dr. Pigarov, UCSD

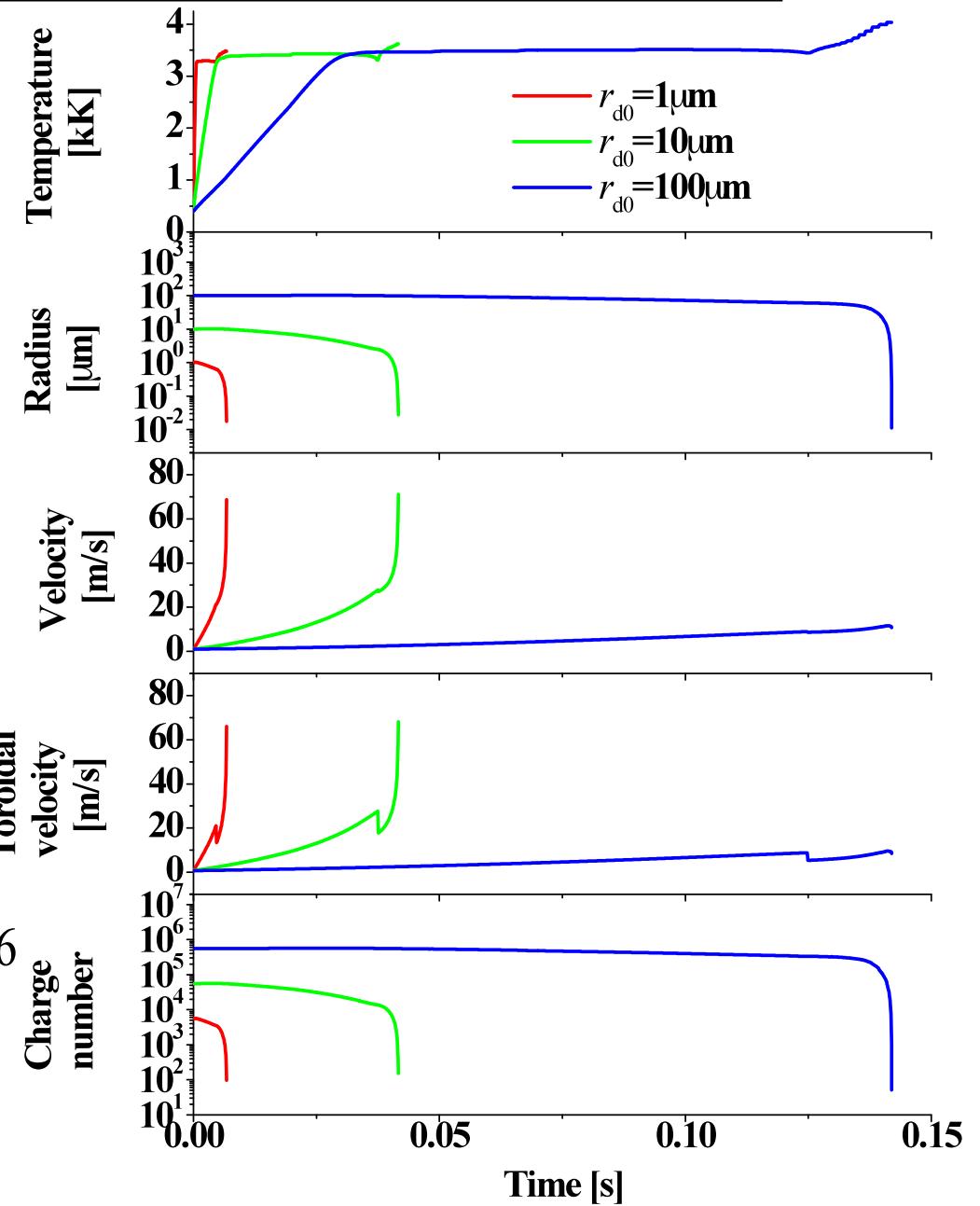
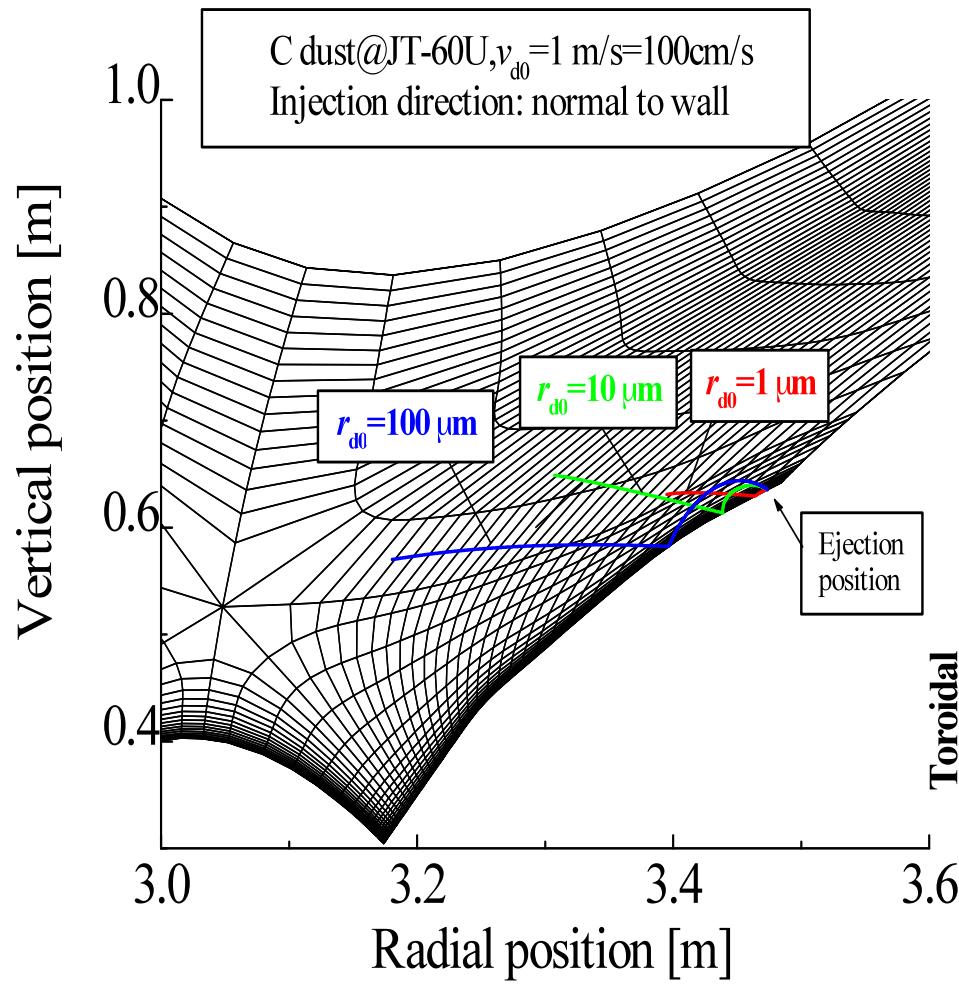
## Outer-divertor



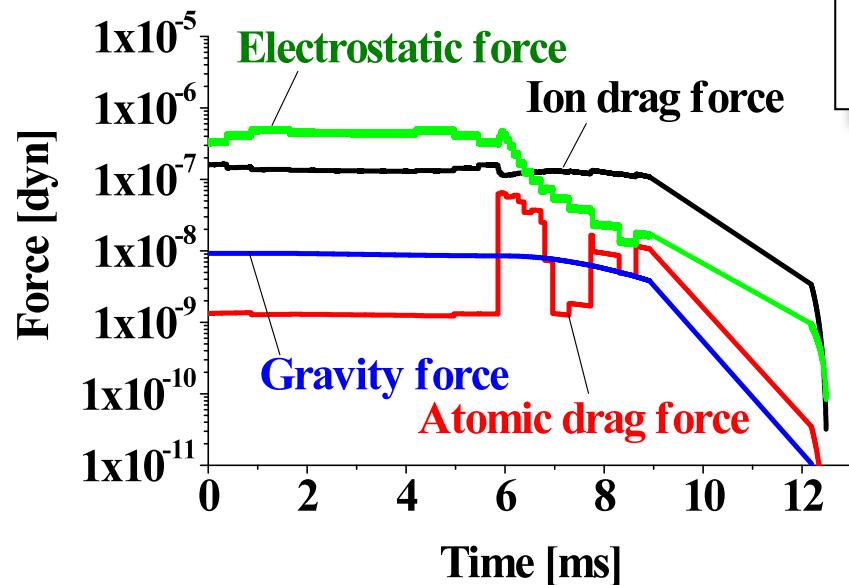
# Trajectories of the dust from outer region for different initial dust velocities -#O1



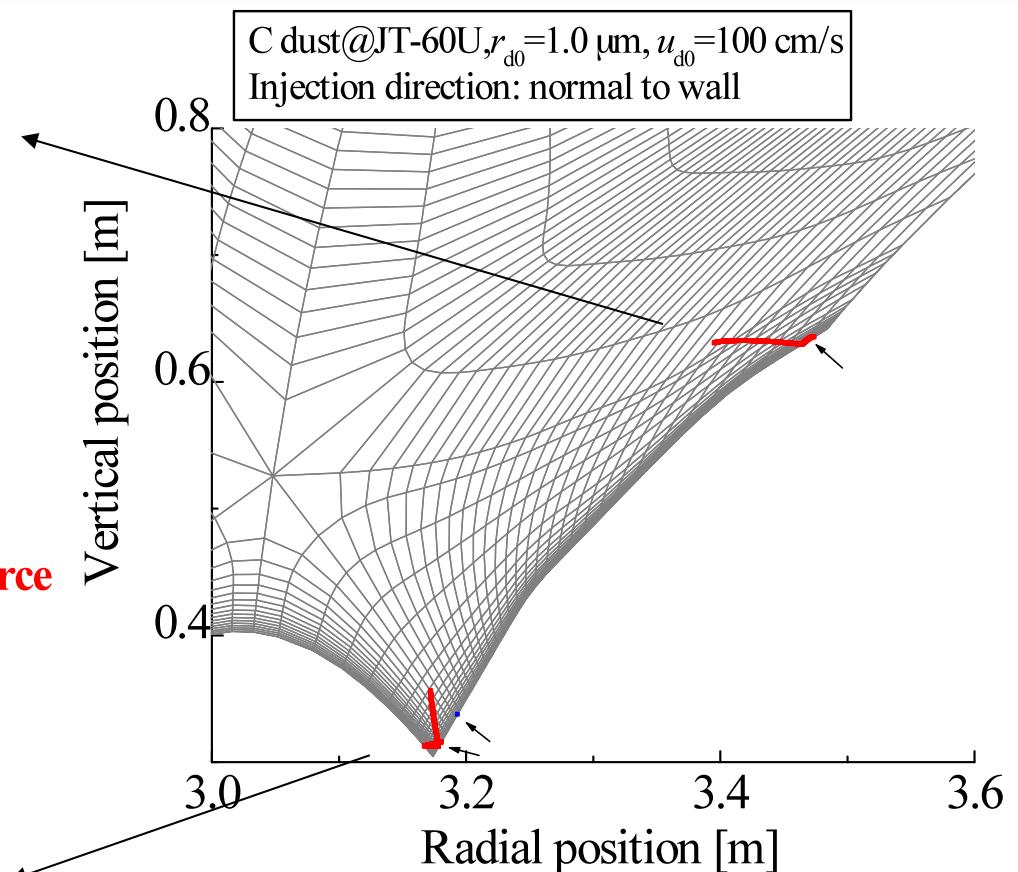
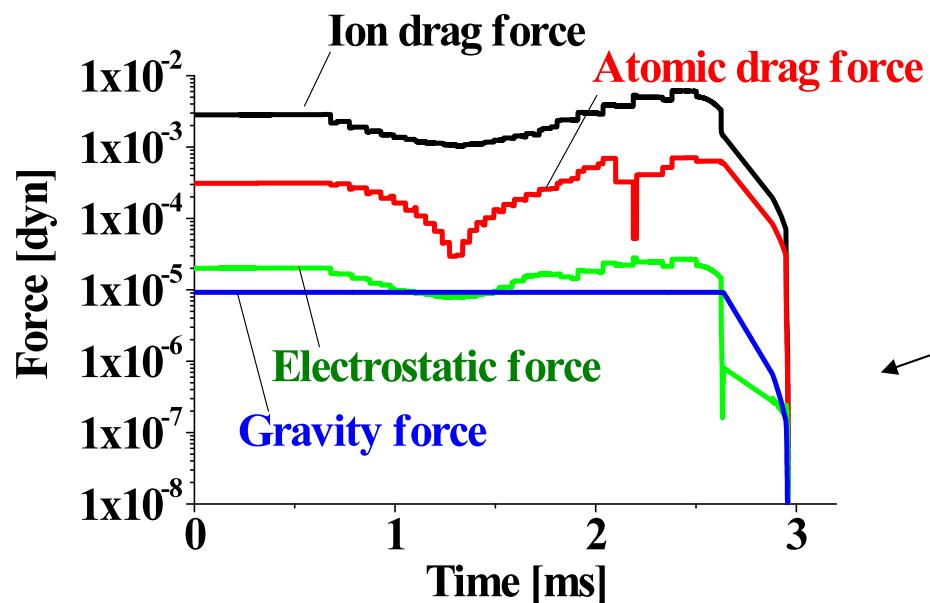
# Trajectories of the dust from outer region for different initial dust radii -#O3



## *Applied forces onto the dust*

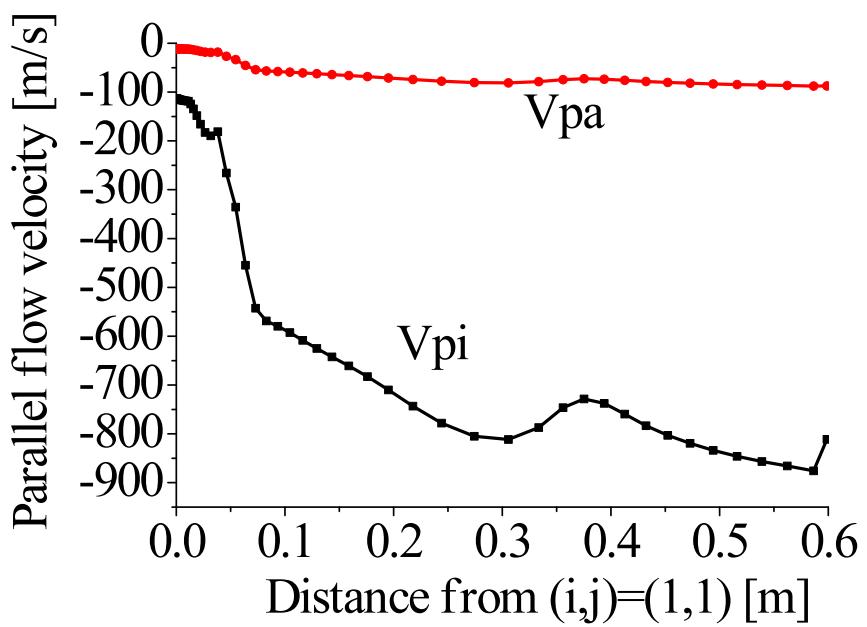
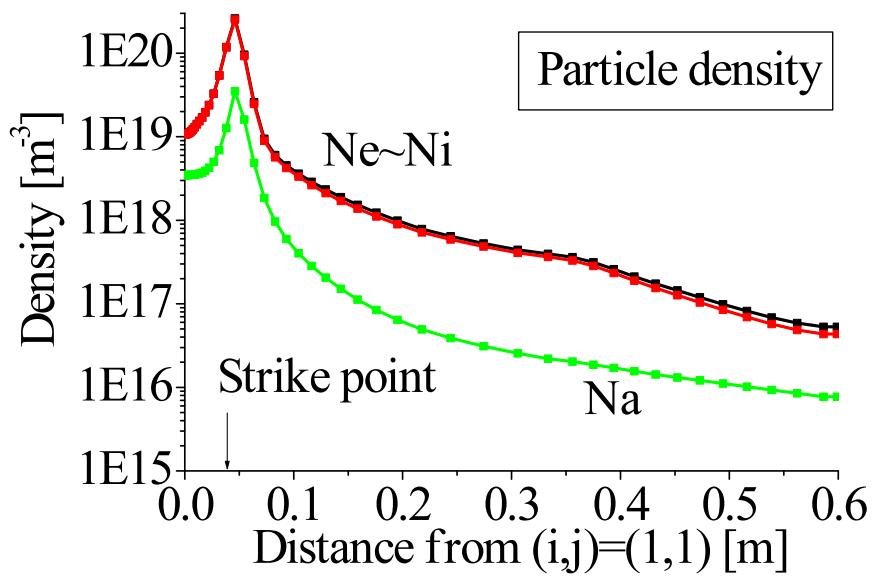
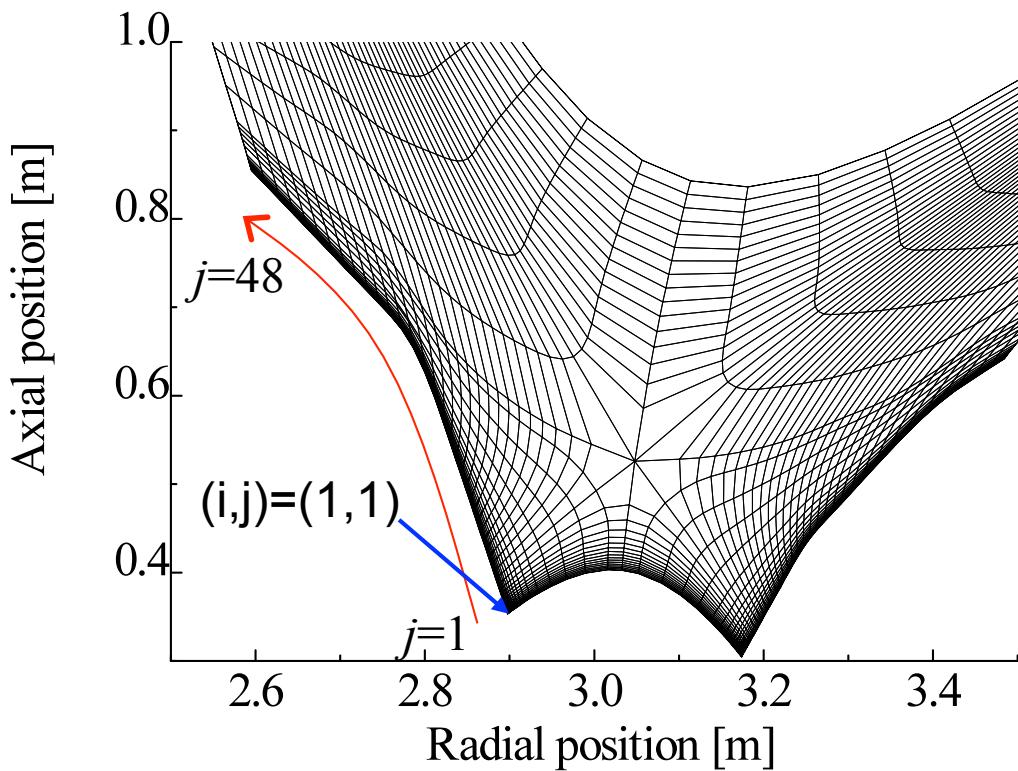
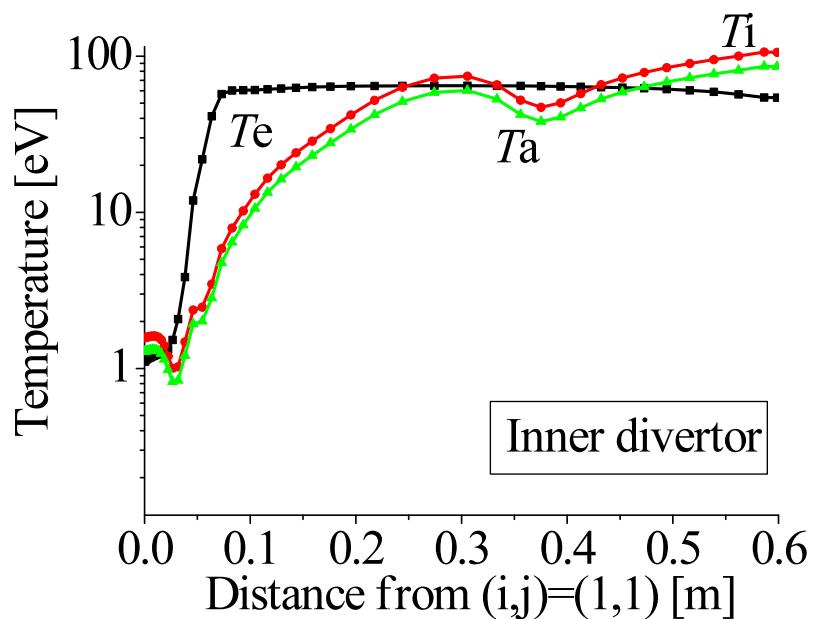


-Initially, electrostatic force is dominant, and then is ion drag force

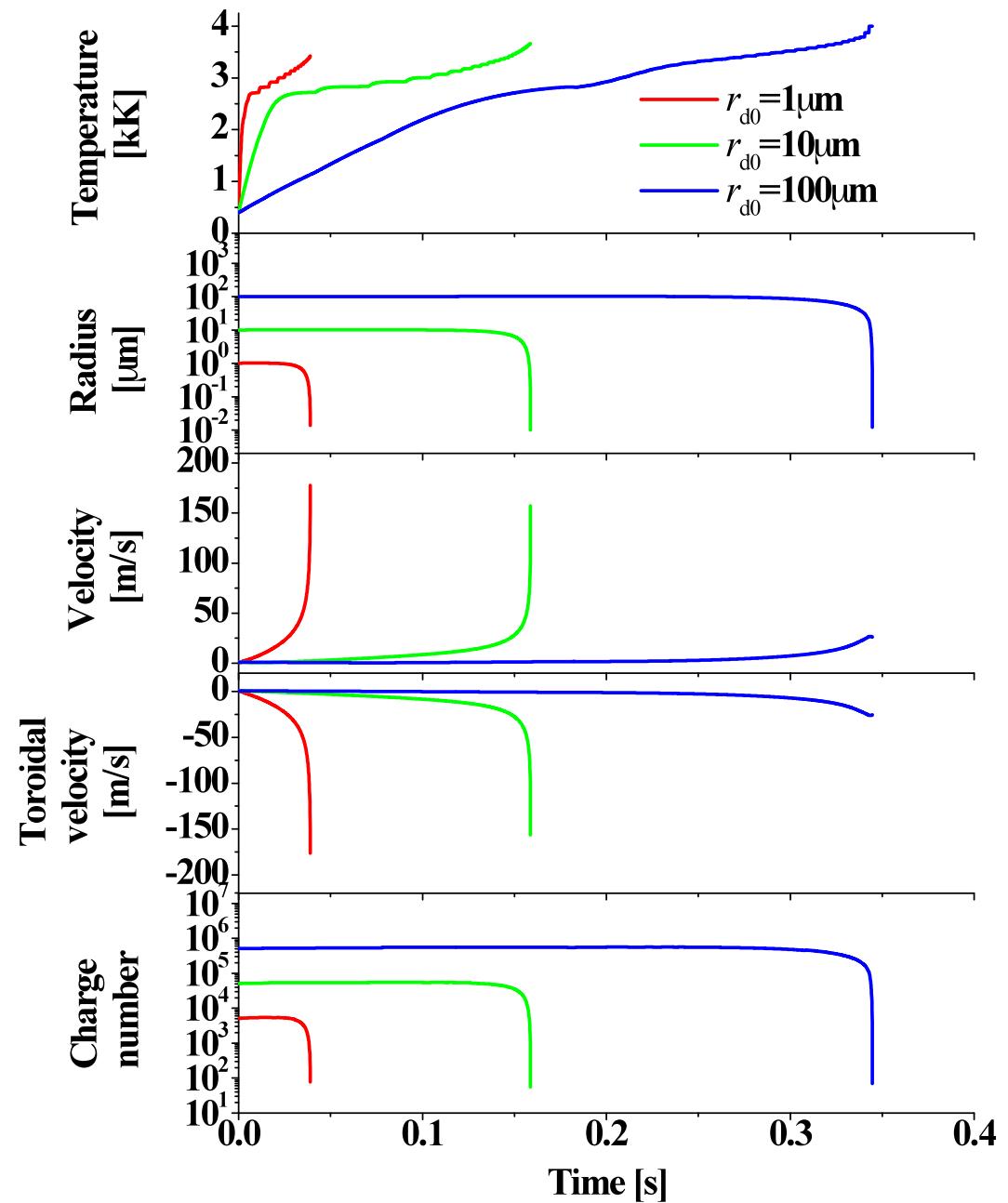
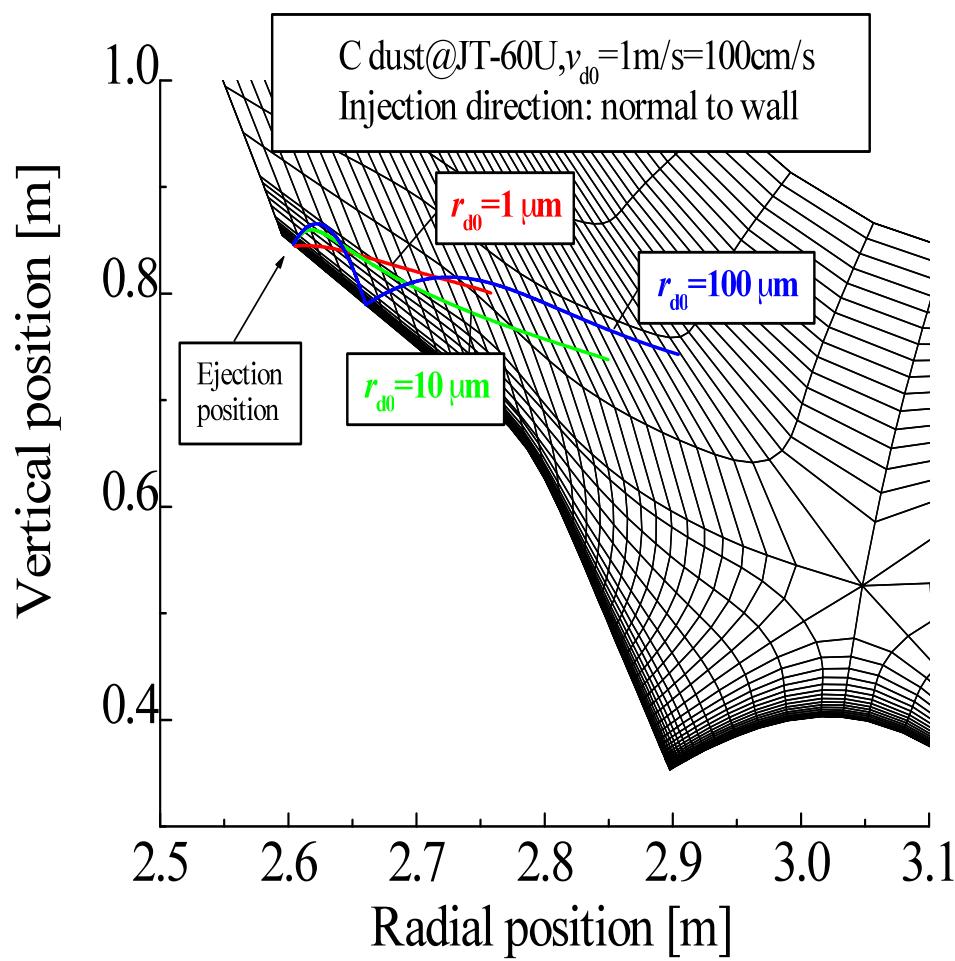


-Dominant force is ion drag force, and atomic drag force.

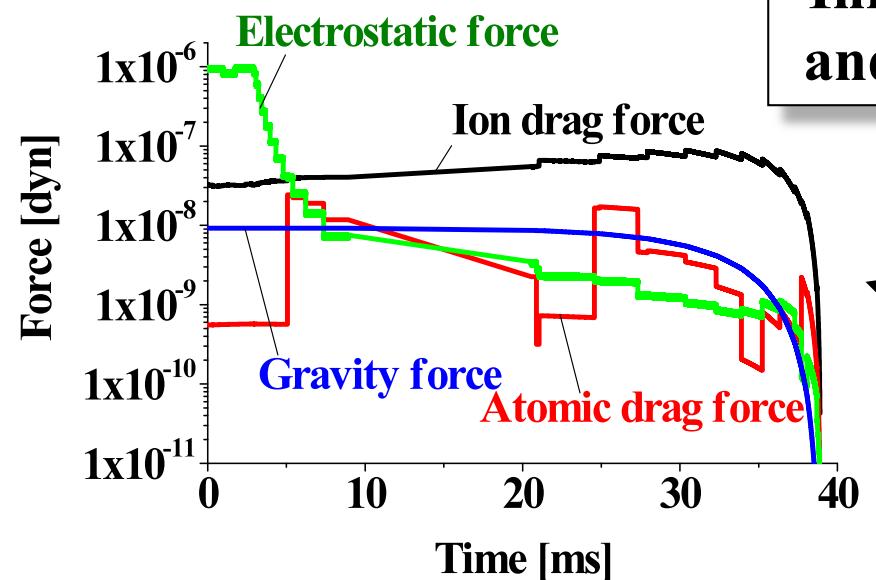
## Inner-divertor



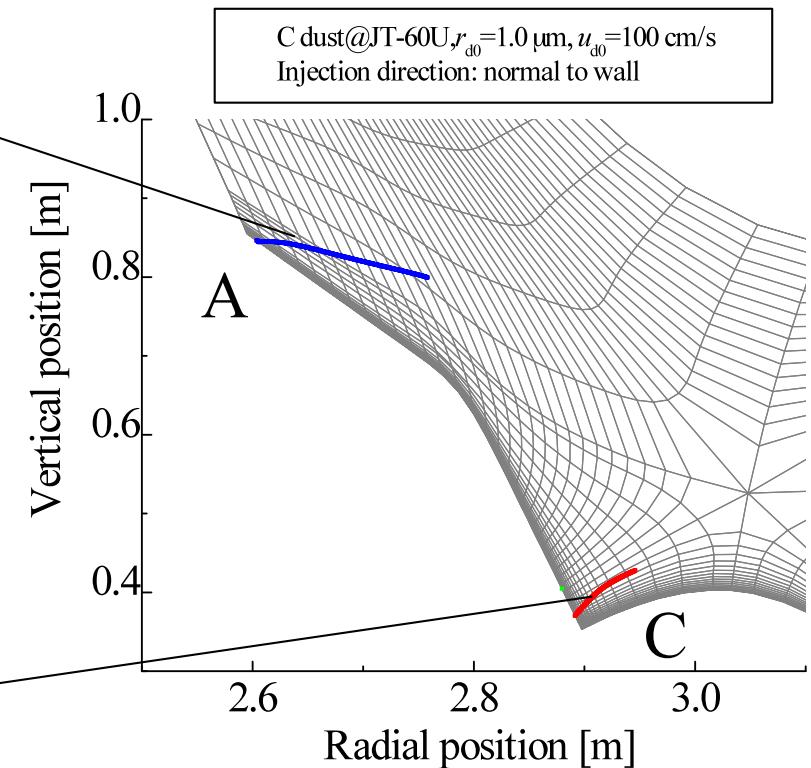
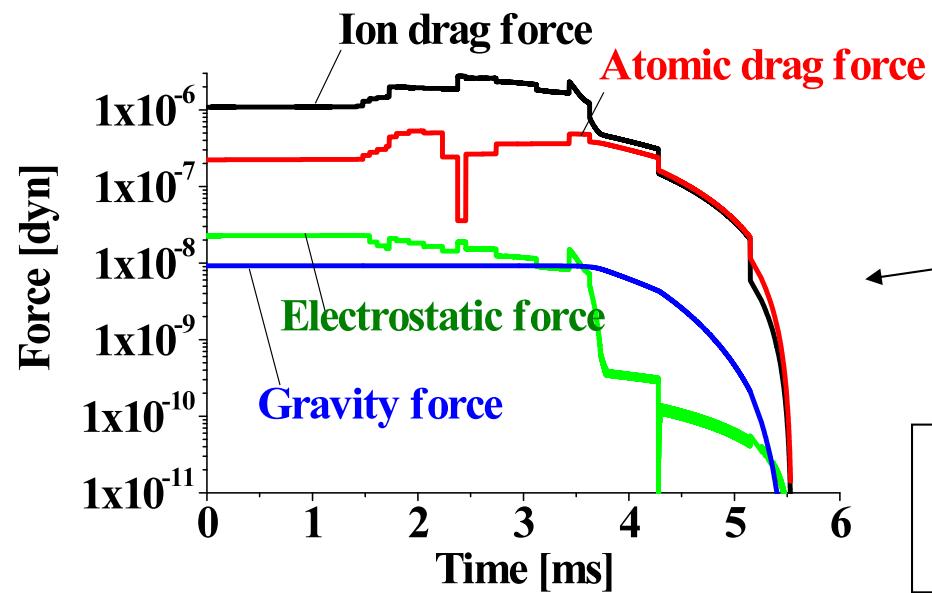
## Trajectories of the dust from inner region for different initial dust radii -#I3



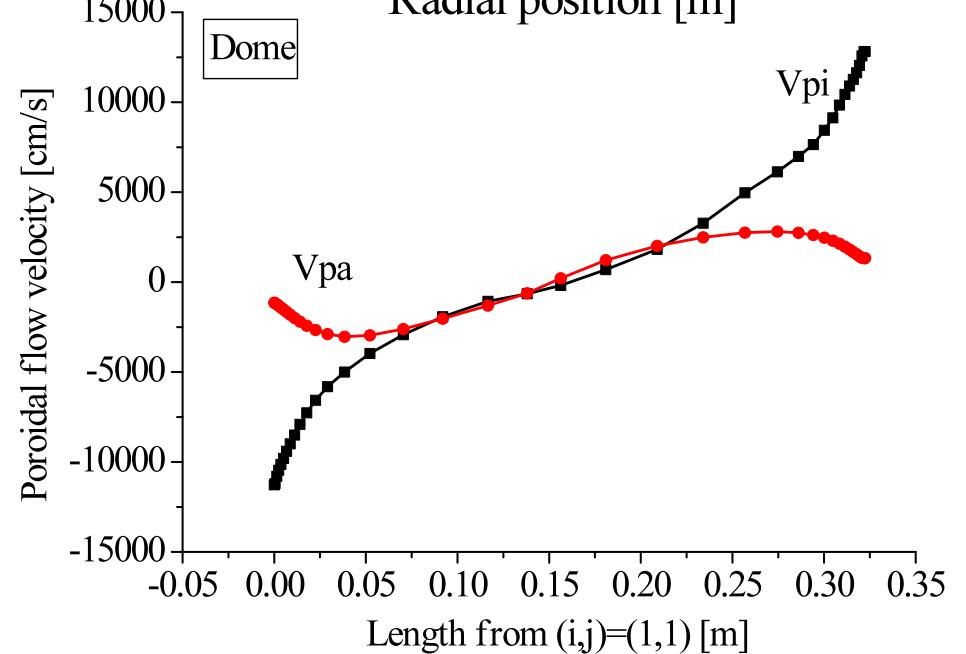
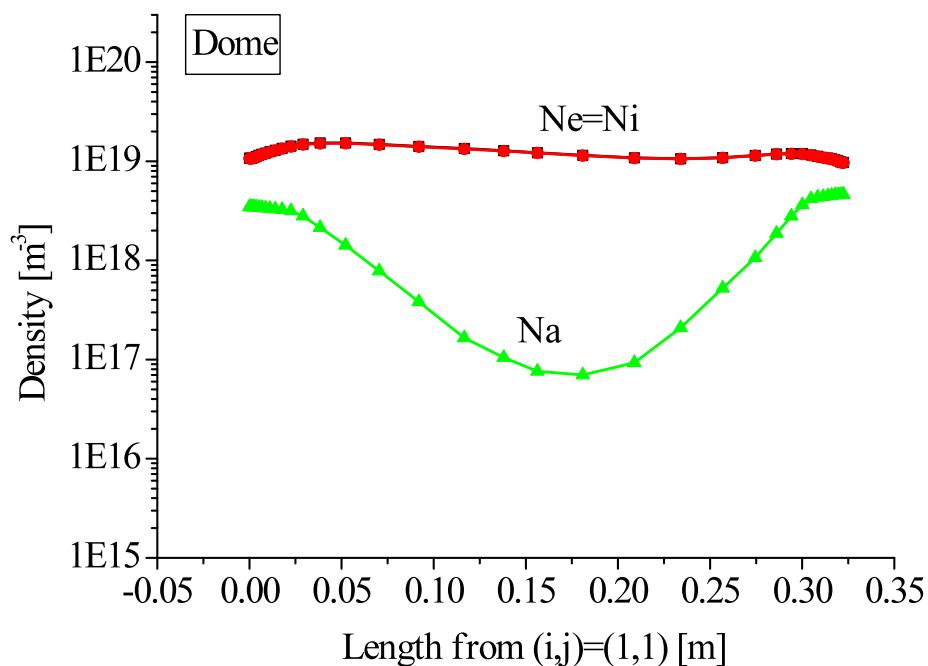
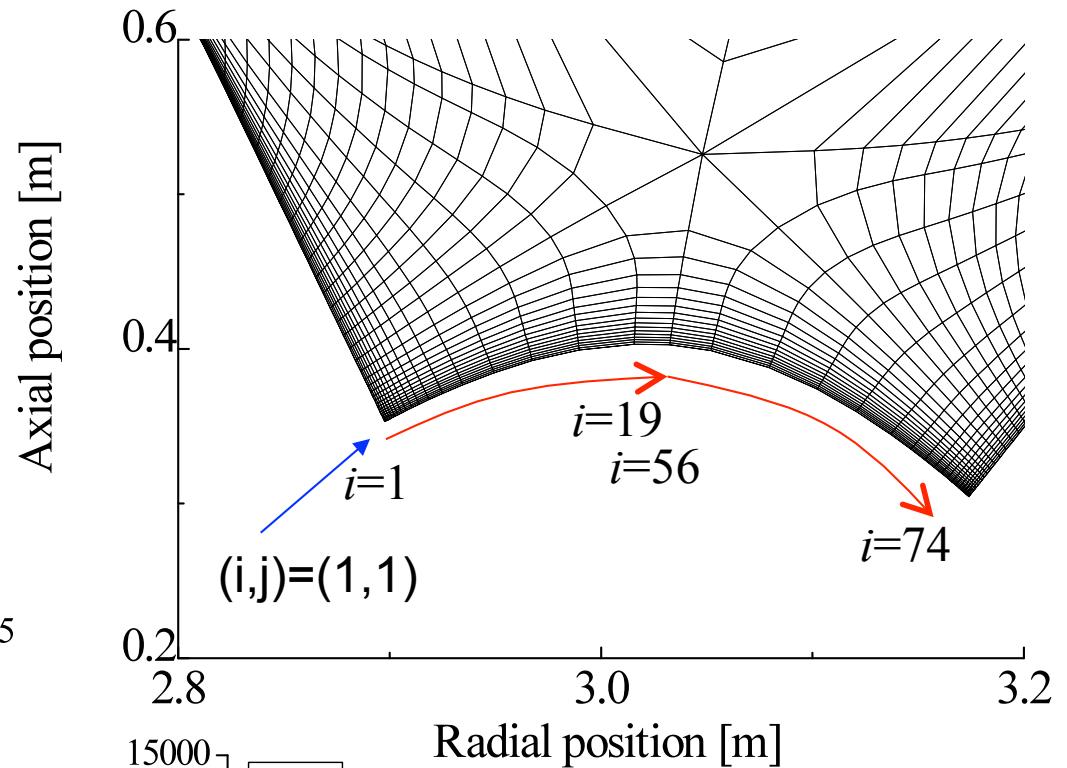
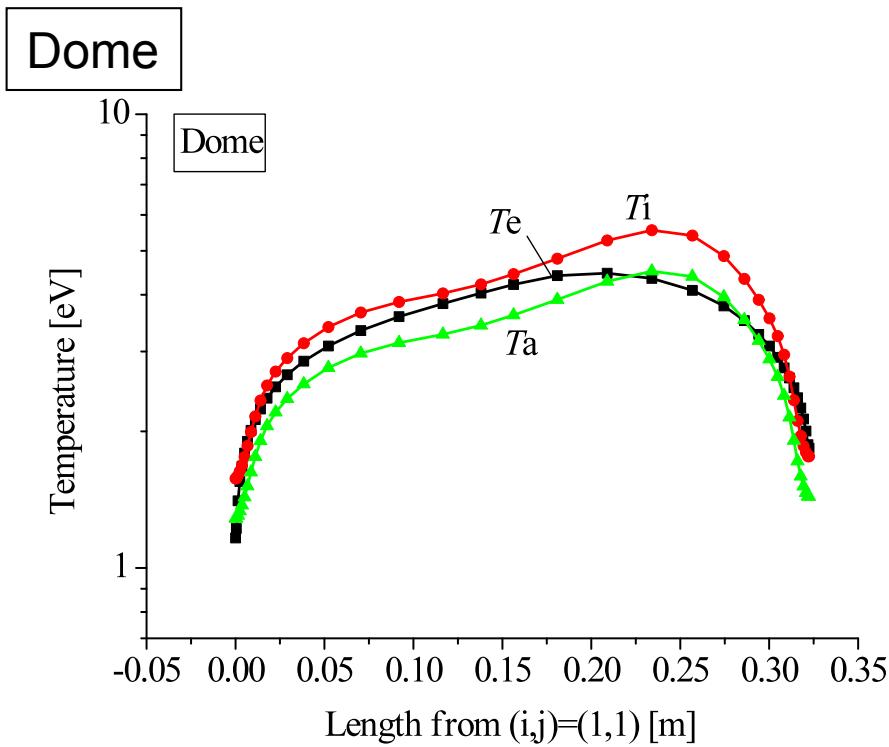
## *Applied forces onto the dust*



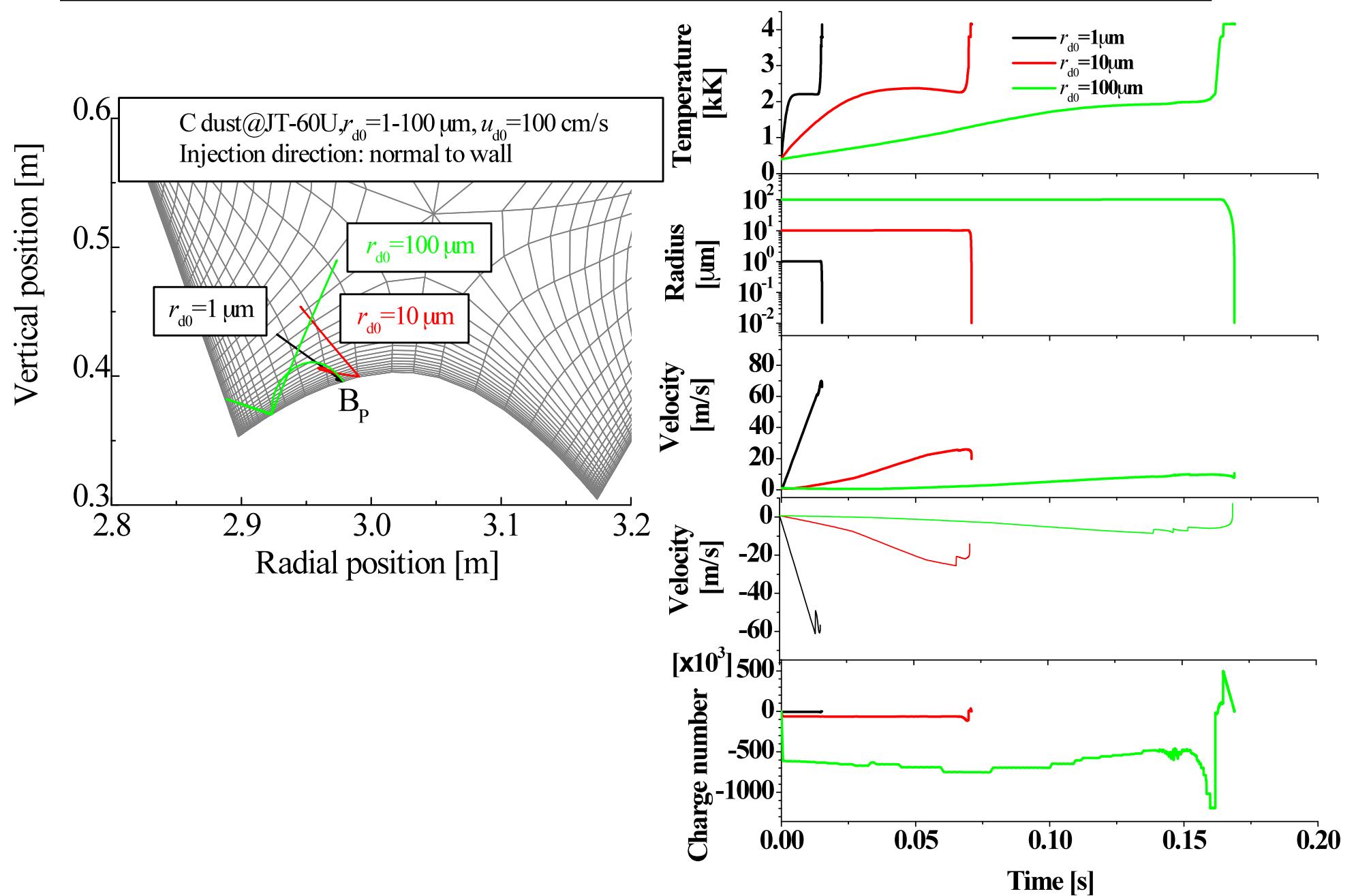
-Initially, electrostatic force is dominant, and then is ion drag force



-Dominant force is ion drag force, and atomic drag force.

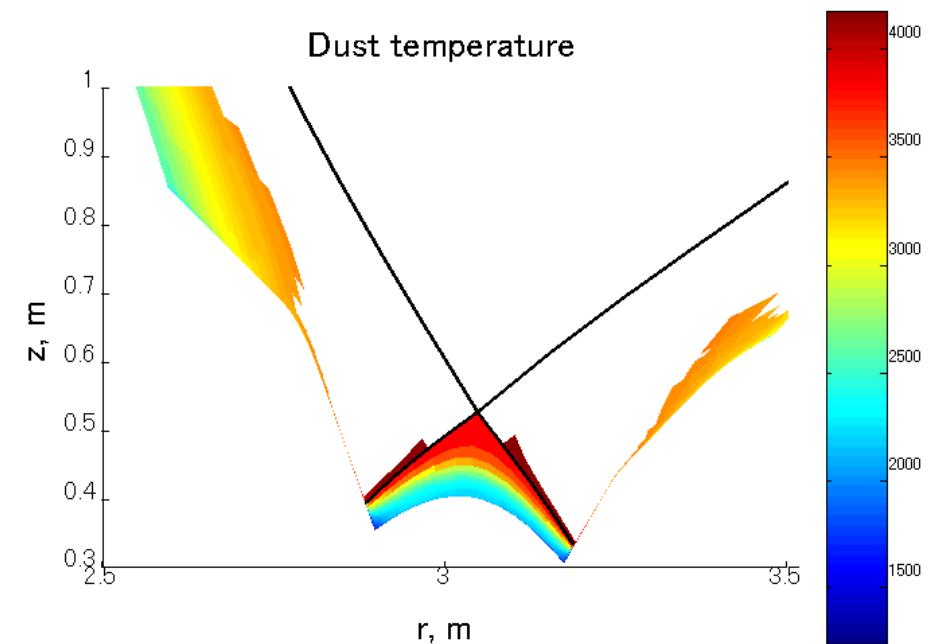
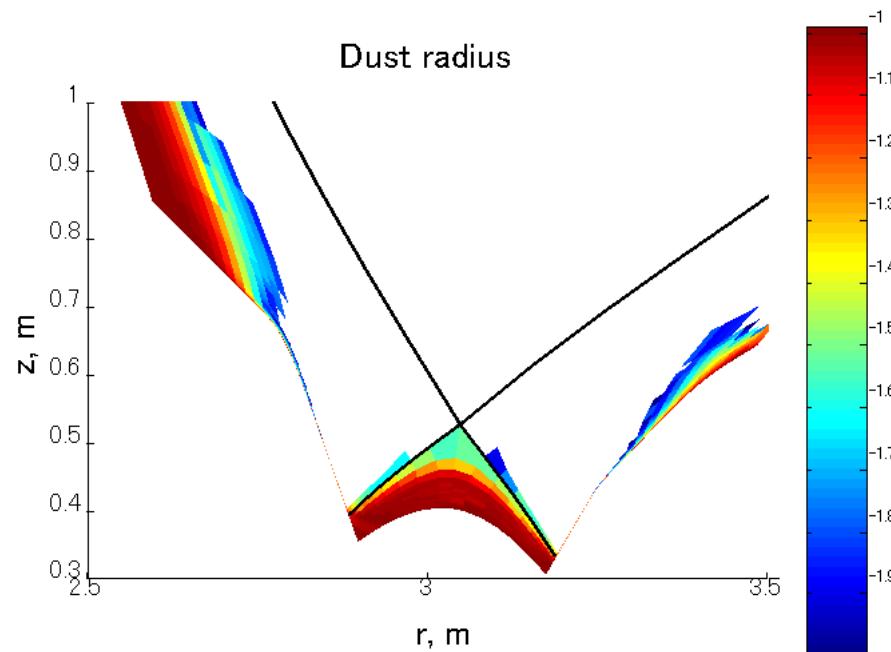


# Trajectories of the dust from private region for different initial dust velocities -#P1



## *Statistical analysis of dust behavior-1*

### *-Different position & initial velocity*

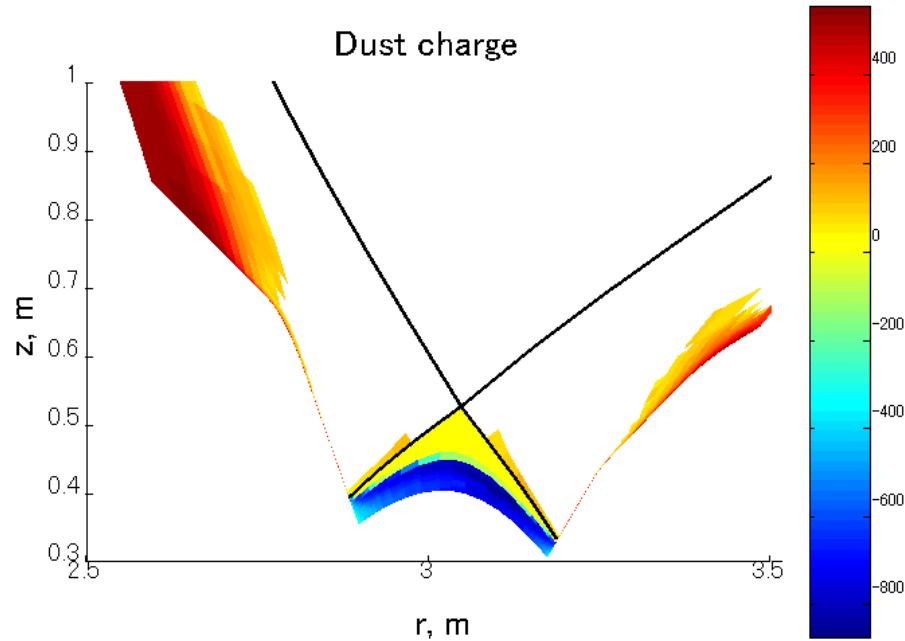


- Near the strike point, a dust particle is rapidly heated and sublimated, which causes short penetration length.
- A dust particle from private zone is slowly heated.

## *Statistical analysis of dust behavior-3*

### *-Different position & initial velocity*

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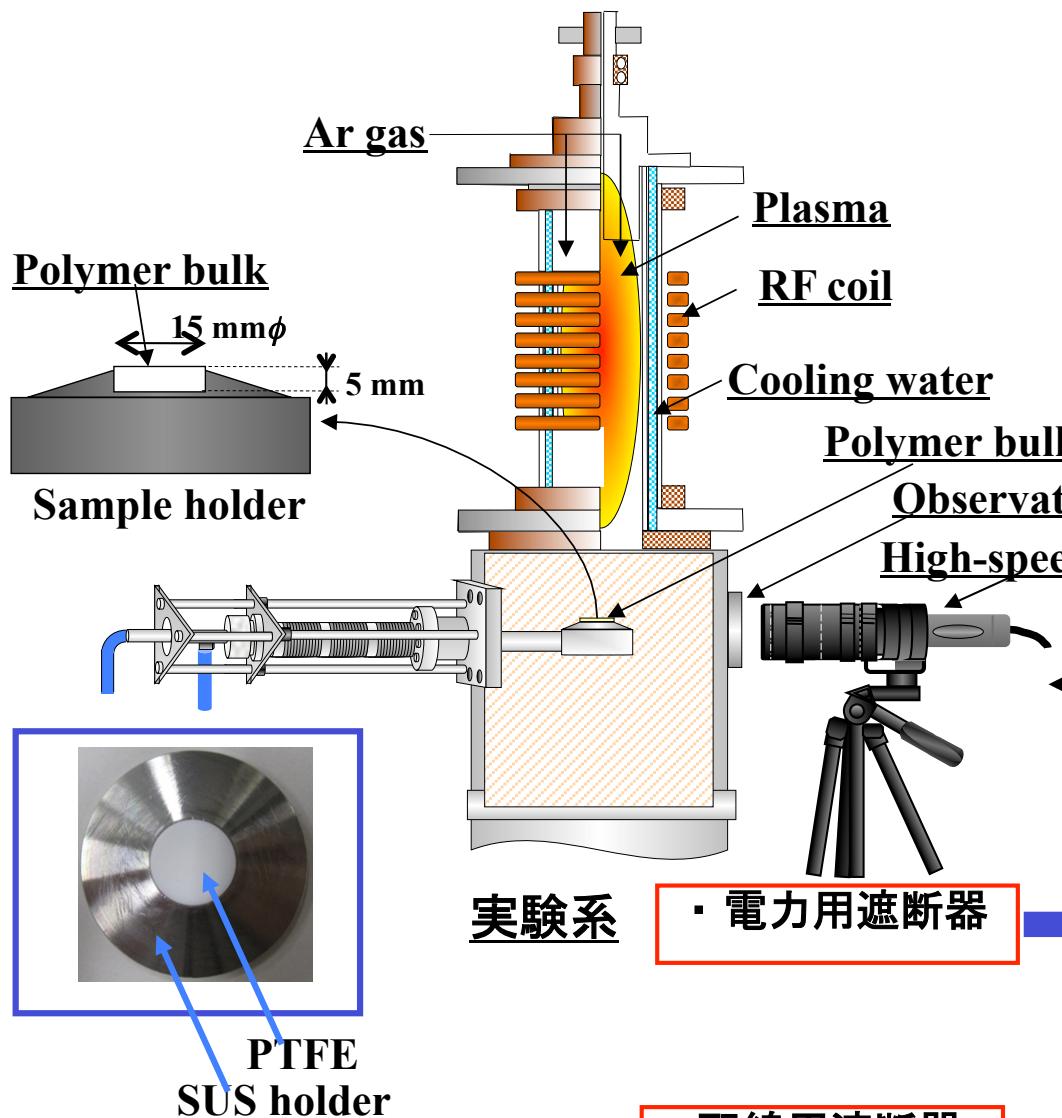
- Near the outer strike point and outer wall, a dust particle is accelerated in toroidal direction counter-clockwise.**  
This arises from ion drag force due to ion flow.
- Near the inner strike point, clockwise acceleration occurs on a dust particle.**

**Fundamental study on dust particle behavior  
Using polymer spallation particles.**

-Polymer Ablation for Application to Arc Quenching



# 実験条件、実験装置及び対象バルク材料



## 実験条件

入力電力	8.54 kW
Ar シースガス流量	30 slpm
トーチ内圧力	760 Torr

## 測定条件

フレームレート 1000 fps

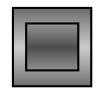
## 実験系

- 電力用遮断器

- 配線用遮断器
- アークホーン
- 宇宙分野(熱遮蔽)

## 対象ポリマー材料

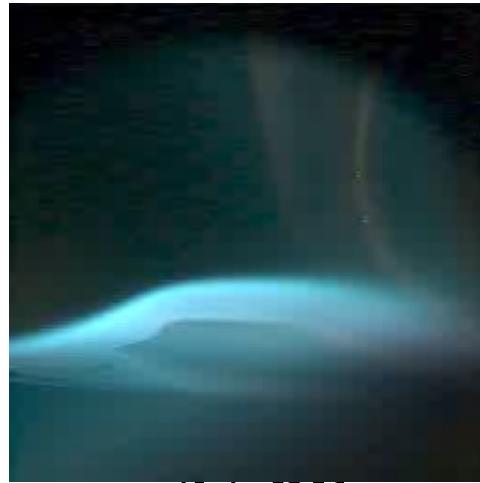
PTFE(テフロン)	$[-C_2F_4-]_n$
PE(ポリエチレン)	$[-C_2H_4-]_n$
POM(デルリン)	$[-CH_2O-]_n$
PMMA(アクリル)	$[-C_5H_8O_2-]_n$
PA66(ナイロン66)	$[-C_{12}H_{22}O_2N_2-]_n$
PA6(ナイロン6)	$[-C_6H_{11}ON-]_n$
PF(フェノール樹脂)	$[-C_7H_6-]_n$



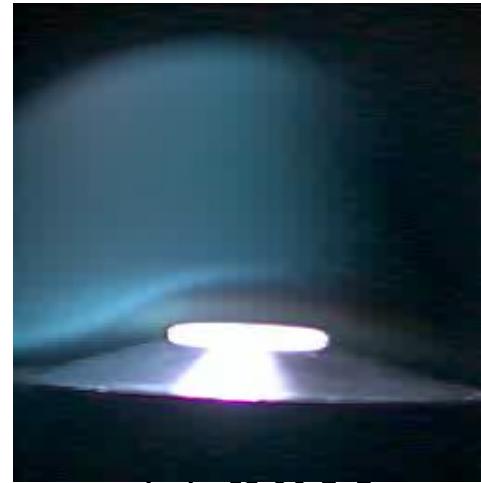
## 高速度カラービデオカメラ撮影結果



(a) PTFE  
[-C<sub>2</sub>F<sub>4</sub>-]<sub>n</sub>



(b) PE  
[-C<sub>2</sub>H<sub>4</sub>-]<sub>n</sub>



(c) POM  
[-CH<sub>2</sub>O-]<sub>n</sub>



(d) PMMA  
[-C<sub>5</sub>H<sub>8</sub>O<sub>2</sub>-]<sub>n</sub>



(e) PA66  
[-C<sub>12</sub>H<sub>22</sub>O<sub>2</sub>N<sub>2</sub>-]<sub>n</sub>



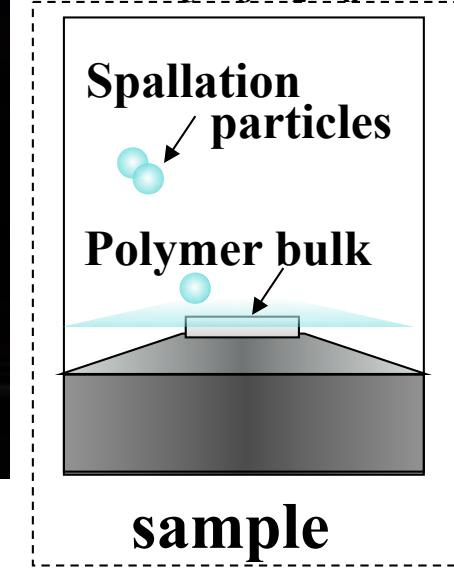
(f) PA6  
[-C<sub>6</sub>H<sub>11</sub>ON-]<sub>n</sub>



(g) PF  
[-C<sub>7</sub>H<sub>6</sub>-]<sub>n</sub>

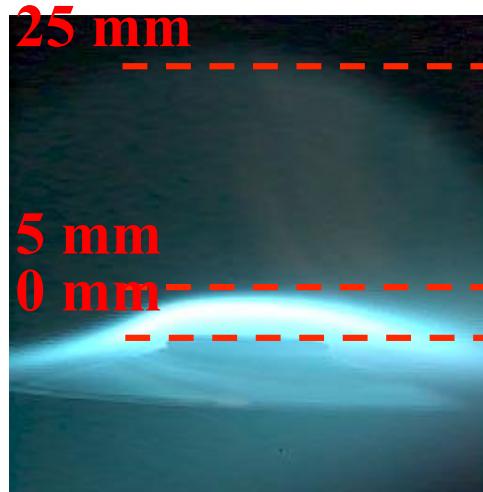
\* 露光時間50μs(POMとPFは250μs)

\*再生速度は15 fps フレームレート 1000 fps

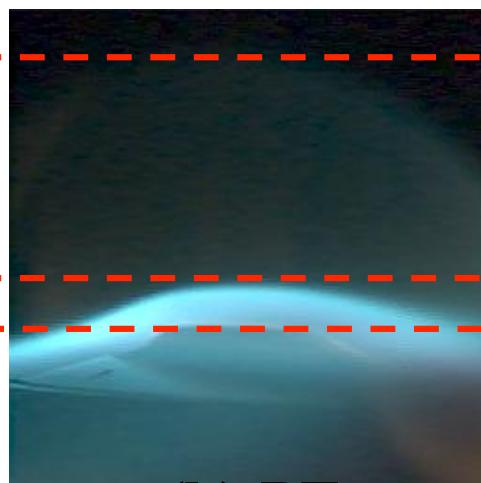




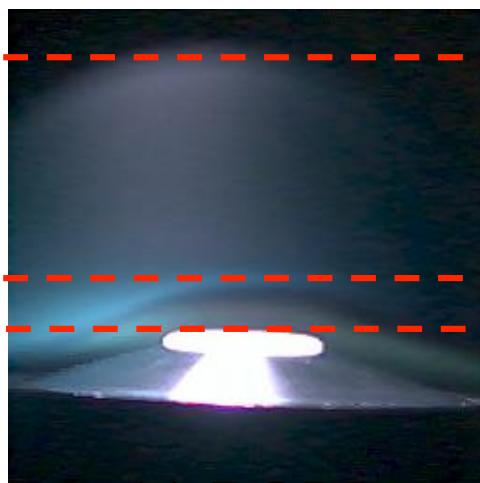
# 高速度カラービデオカメラ撮影結果



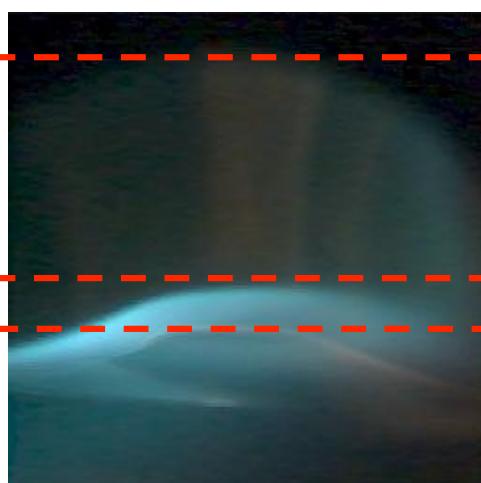
(a) PTFE  
 $[-C_2F_4]_n$



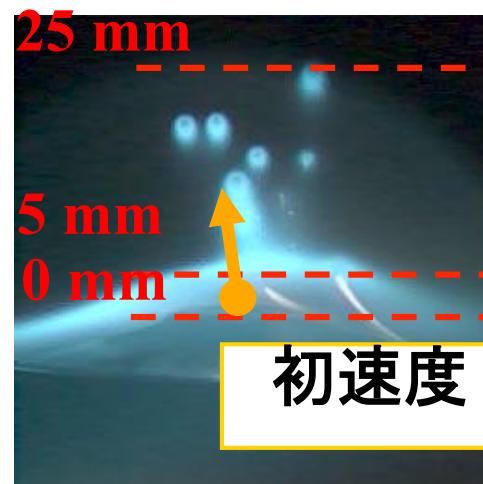
(b) PE  
 $[-C_2H_4]_n$



(c) POM  
 $[-CH_2O]_n$

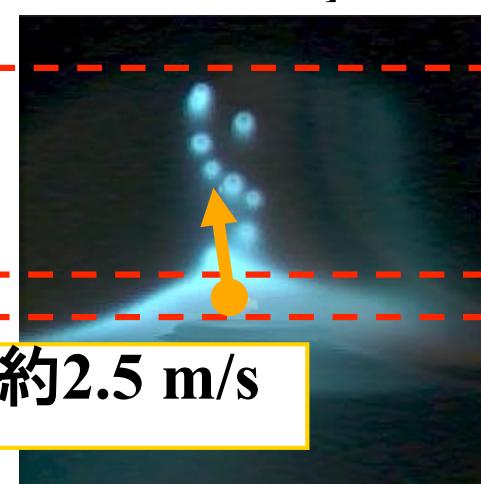


(d) PMMA  
 $[-C_5H_8O_2]_n$

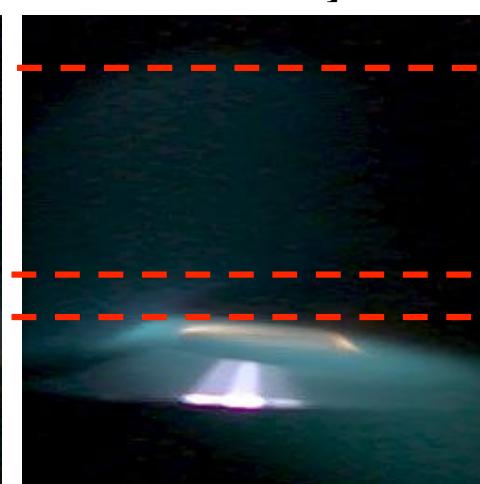


初速度 約2.5 m/s

(e) PA66  
 $[-C_{12}H_{22}O_2N_2]_n$



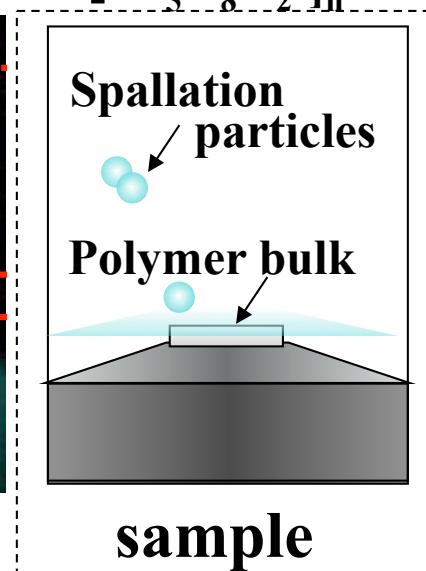
(f) PA6  
 $[-C_6H_{11}ON]_n$



(g) PF  
 $[-C_7H_6]_n$

\* 露光時間50μs(POMとPFは250μs)

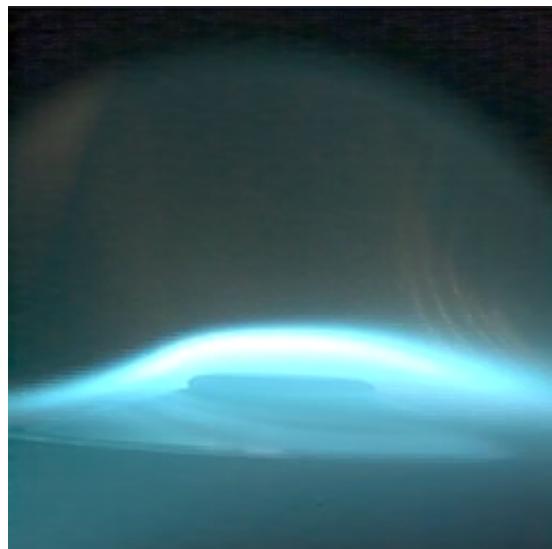
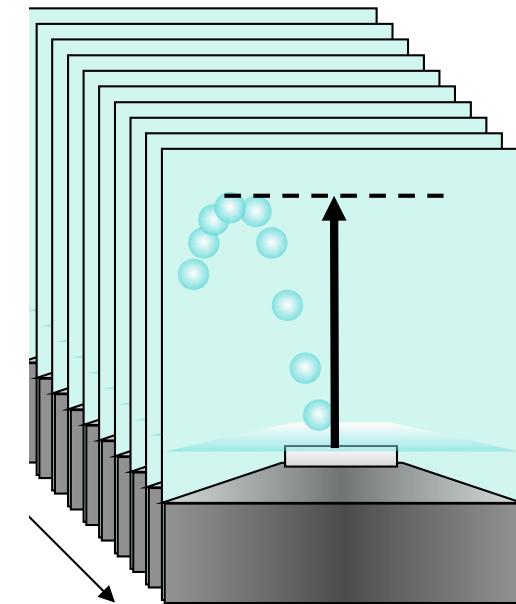
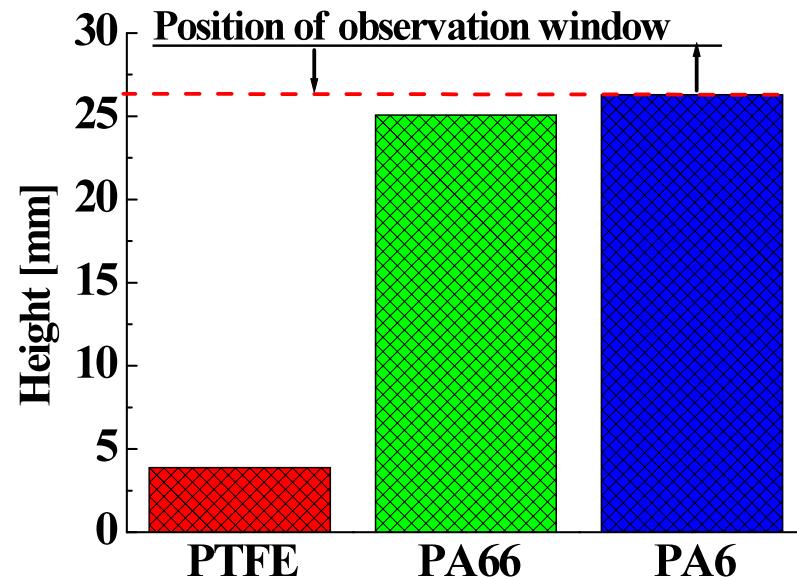
\*再生速度は15 fps フレームレート 1000 fps



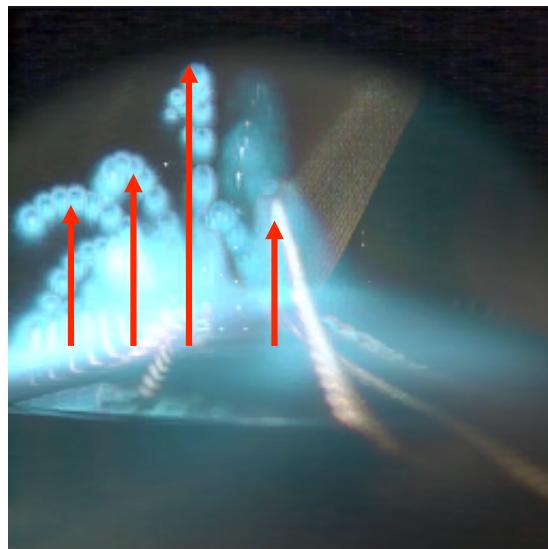


## スポレーショノ粒子の飛翔の様相

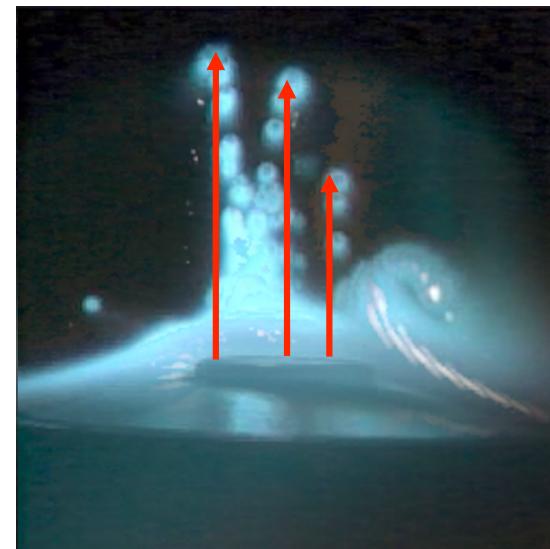
- ⇒ 100枚(0.1秒)
- ⇒ 各ピクセル
- 飛翔粒子が
- 飞翔粒子が
- ポリマー表面



(a) PTFE  
[-C<sub>2</sub>F<sub>4</sub>-]<sub>n</sub>



(b) PA66  
[-C<sub>12</sub>H<sub>22</sub>O<sub>2</sub>N<sub>2</sub>-]<sub>n</sub>



(c) PA6  
[-C<sub>6</sub>H<sub>11</sub>ON-]<sub>n</sub>

# □ スポレーション粒子飛翔軌跡の数値解析

## 運動方程式

$$\frac{dv_d}{dt} = -\frac{3}{4} C_D (v_d - u) |v_d - u| \frac{\rho}{\rho_p (2r_p)} + g$$

粒子に加わる力 ⇒ ドラッグ力 重力

## エネルギー保存式

### Innershells

$$\rho_p C_{pp} \frac{\partial T_p(r,t)}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \kappa_p \frac{\partial T_p(r,t)}{\partial r} \right) \quad (T_p < T_{melt}, T_{melt} < T_p < T_{boil})$$

$$\rho_p H_m \frac{\partial \chi_p(r,t)}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \kappa_p \frac{\partial T_p(r,t)}{\partial r} \right) \quad (T_p = T_{melt})$$

### Outershell

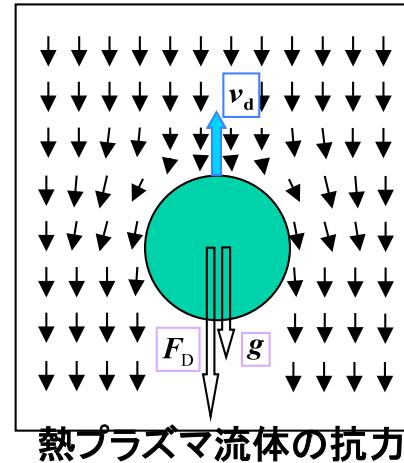
$$\frac{4\pi}{3} \rho_p C_{pp} (r_p^3 - r_{p-1}^3) \frac{\partial T_p(r,t)}{\partial t} = Q \quad (T_p < T_{melt}, T_{melt} < T_p < T_{boil})$$

$$\frac{4\pi}{3} \rho_p H_m (r_p^3 - r_{p-1}^3) \frac{\partial \chi_p(r,t)}{\partial t} = Q \quad (T_p = T_{melt})$$

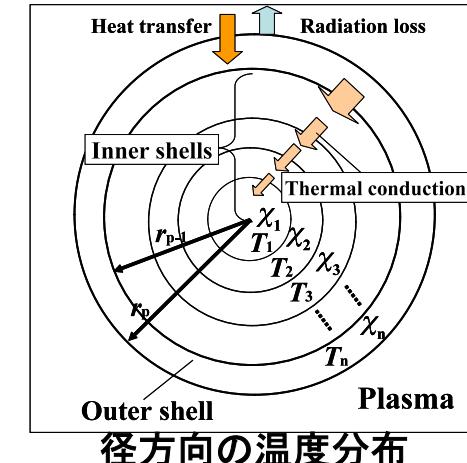
$$Q = 4\pi r_p^2 (h_c(T - T_p) - \sigma_s \epsilon (T_p^4 - T_a^4)) - 4\pi r_{p-1}^2 \kappa_p \frac{\partial T_p(r,t)}{\partial r} \Big|_{r=r_{p-1}}$$

## 質量保存式

$$\frac{\partial r_p}{\partial t} = -\frac{Q}{4\pi \rho_p H_v r_p^2} \quad (T_p \geq T_{boil})$$



熱プラズマ流体の抗力



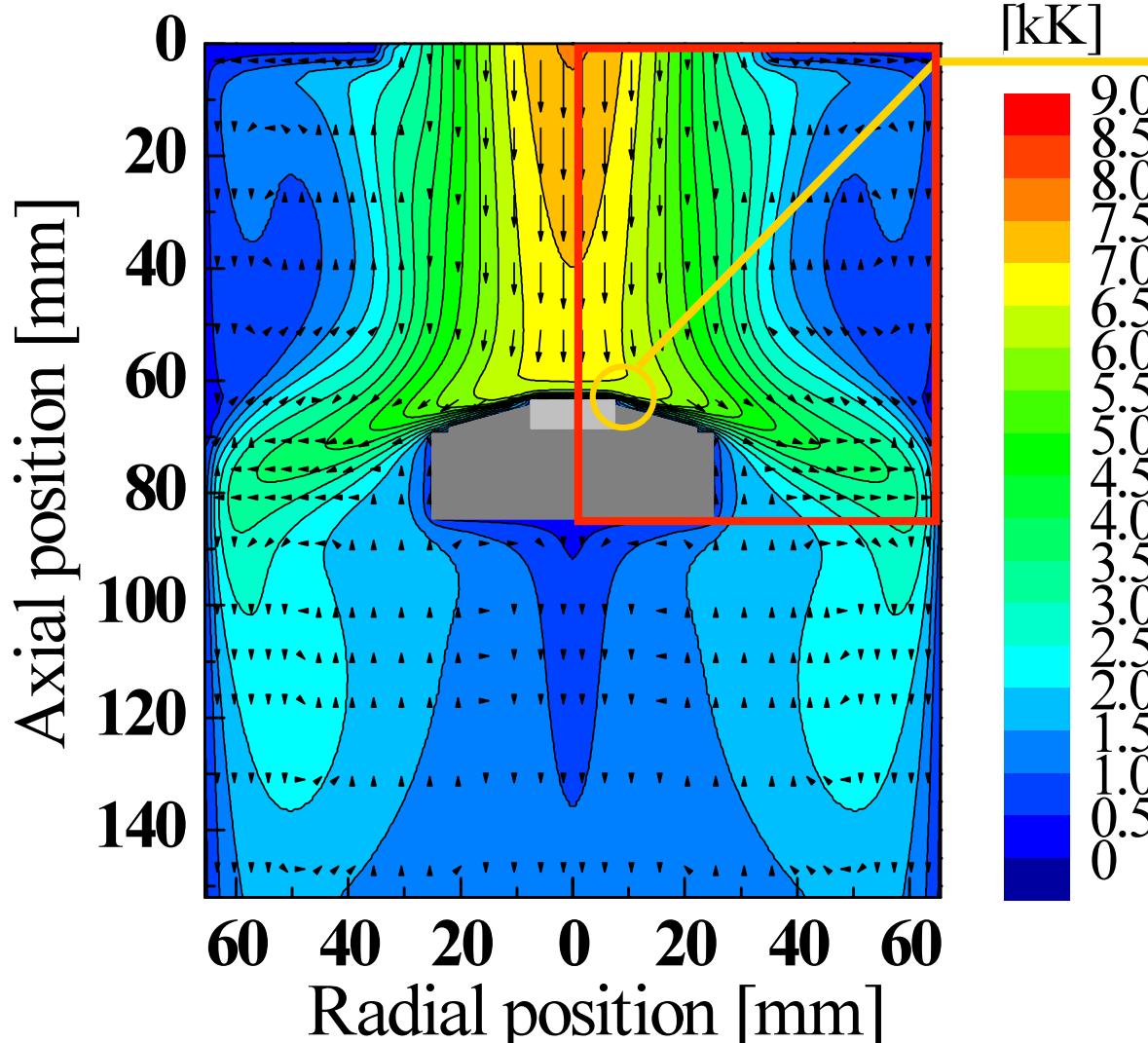
径方向の温度分布

$r$	径方向位置
$v_d$	粒子の速度
$u$	プラズマの速度
$r_p$	粒子の半径
$\rho$	プラズマの質量密度
$\rho_p$	粒子の質量密度
$C_D$	ドラッグ係数
$g$	重力加速度
$T_p$	粒子の温度
$\chi_p$	粒子の液化率
$C_{pp}$	ポリマーの定圧比熱
$H_m$	ポリマーの融点の潜熱
$H_v$	ポリマーの沸点の潜熱
$\kappa_p$	ポリマーの熱伝導率
$h_c$	熱伝達係数

⇒ Next  
背景プラズマ場の計算手法

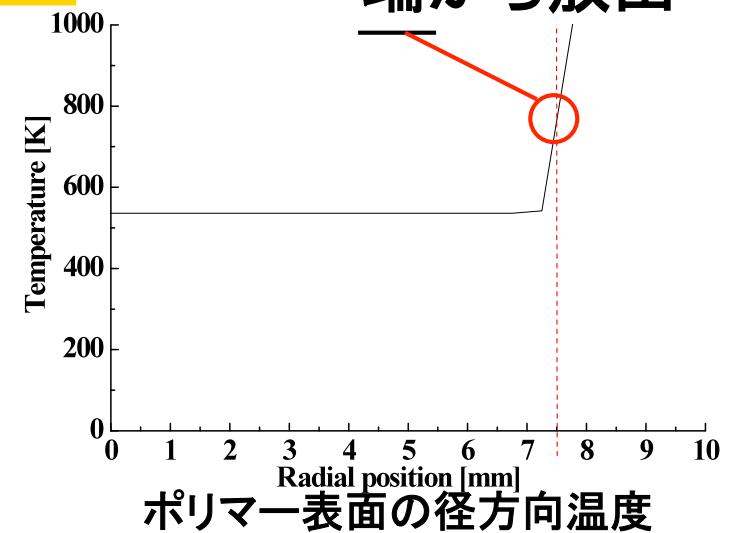


# 計算空間と各計算条件



熱プラズマの温度場と流速ベクトル

ポリマーバルク材の  
端から放出



ポリマー表面の径方向温度

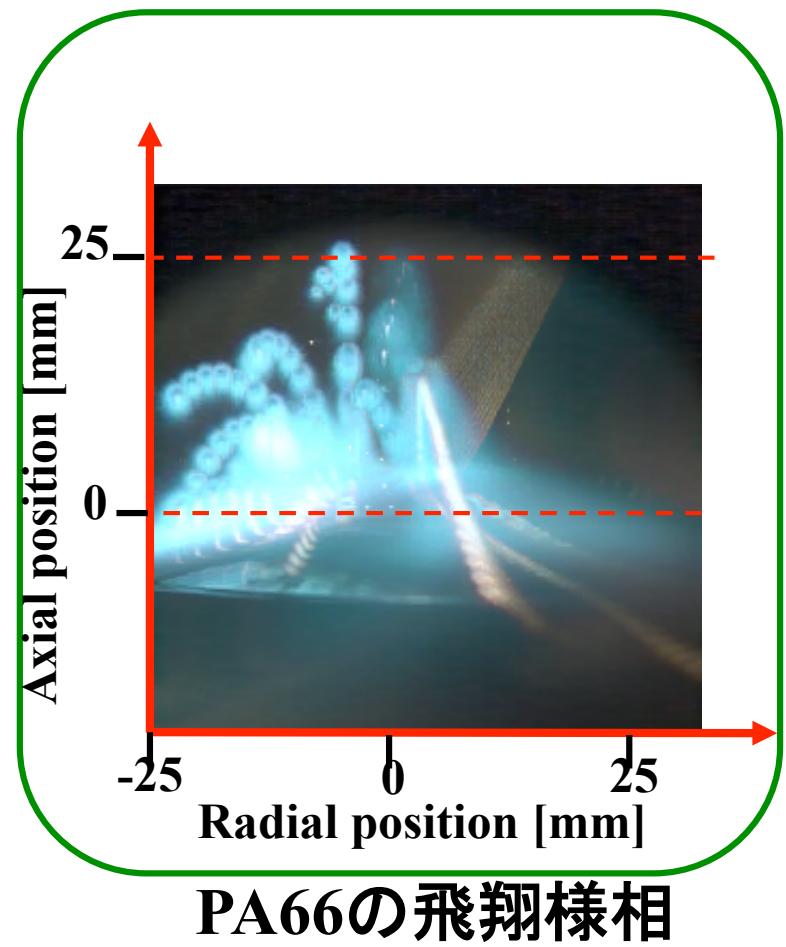
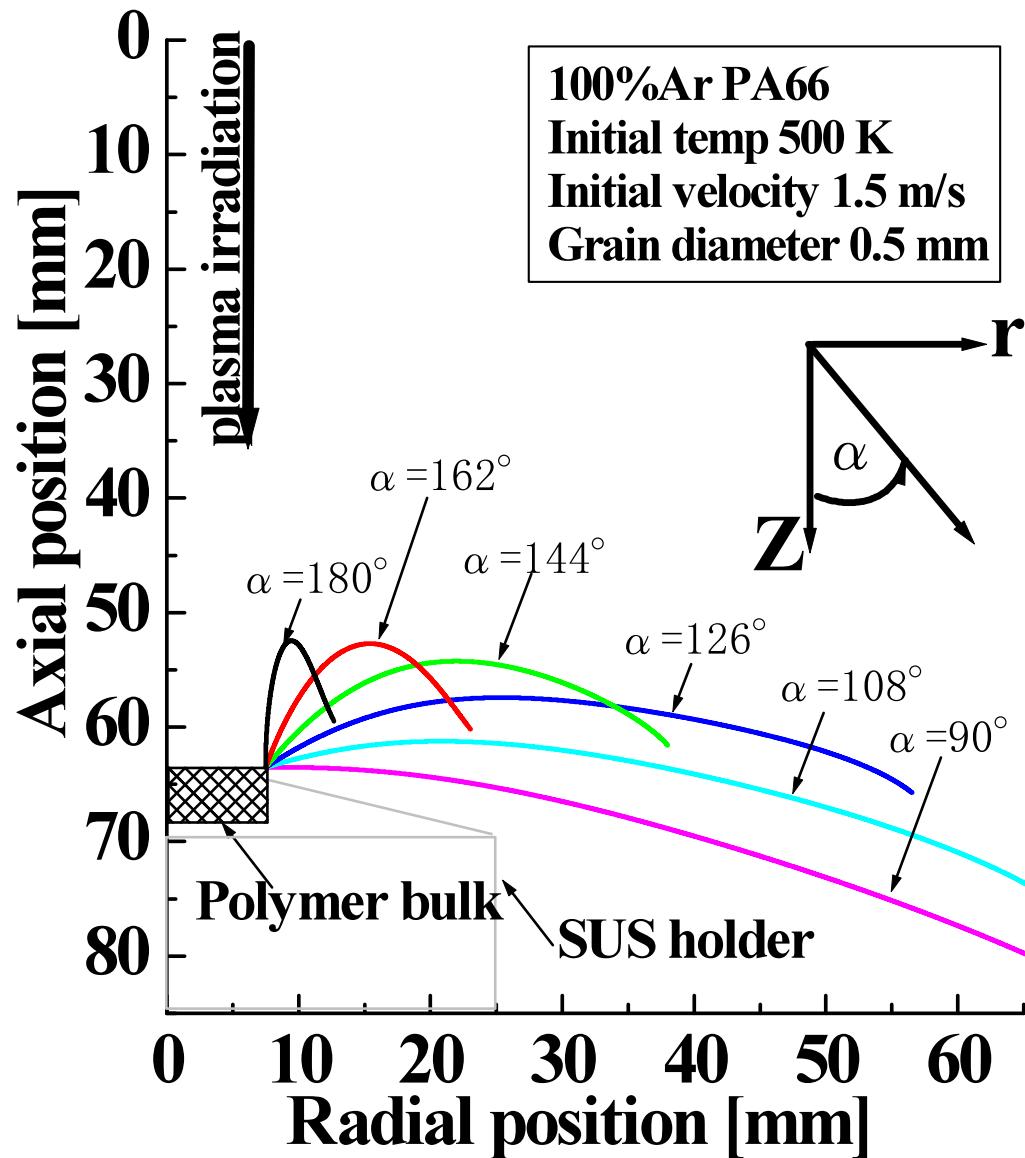
スポレーショん粒子の初期条件

対象ポリマー材料	PA66
初期温度	500 K
初期直径	0.5 mm
初期速度	1.5 m/s

計算終了条件

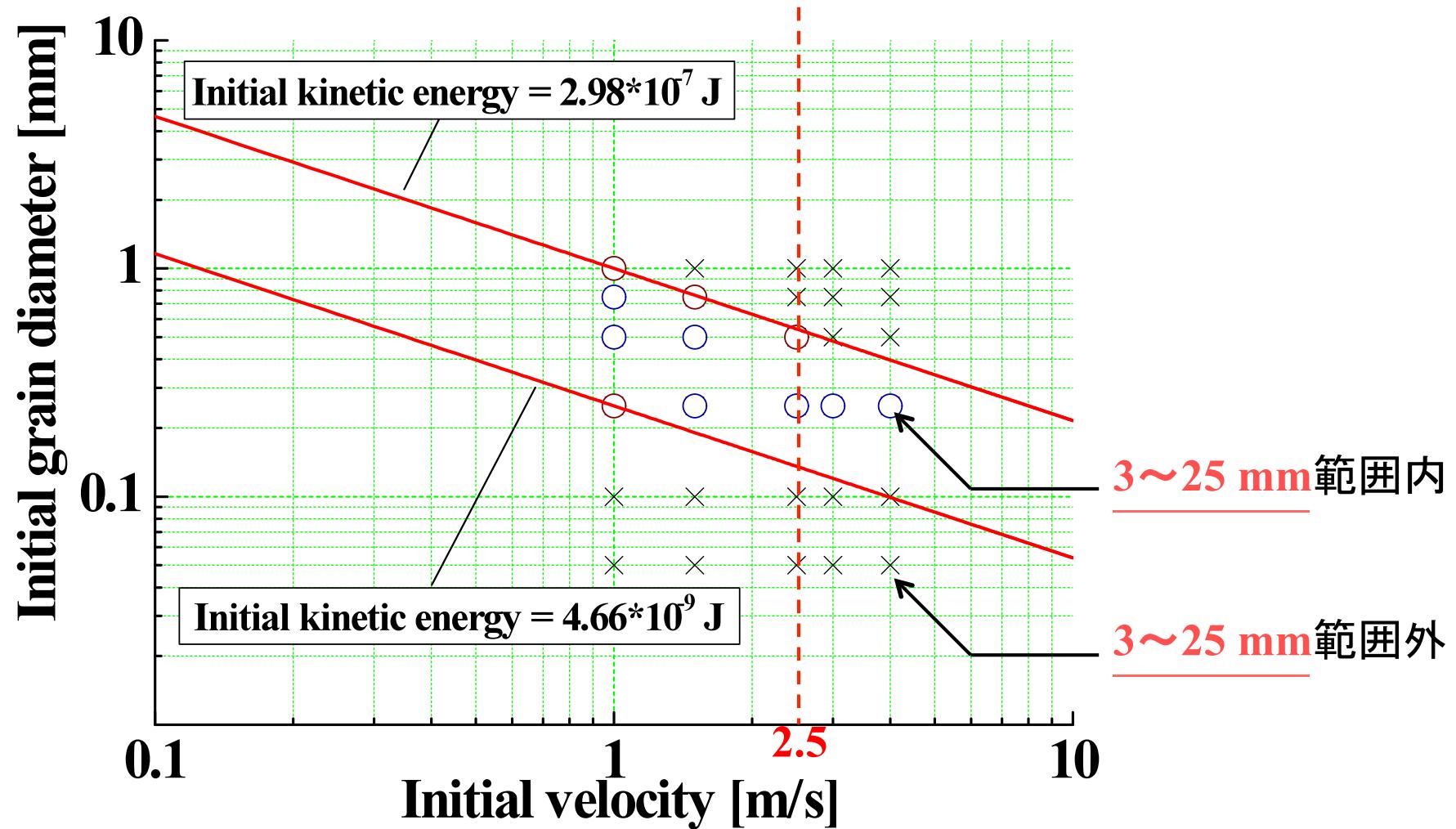
初期直径の1/100以下  
⇒ 蒸発して消滅した

# スポレーション粒子の飛翔軌跡



軸方向に近い方向角  
⇒ ほぼ同様な軌跡

# 飛翔軌跡の撮影結果と計算結果との比較



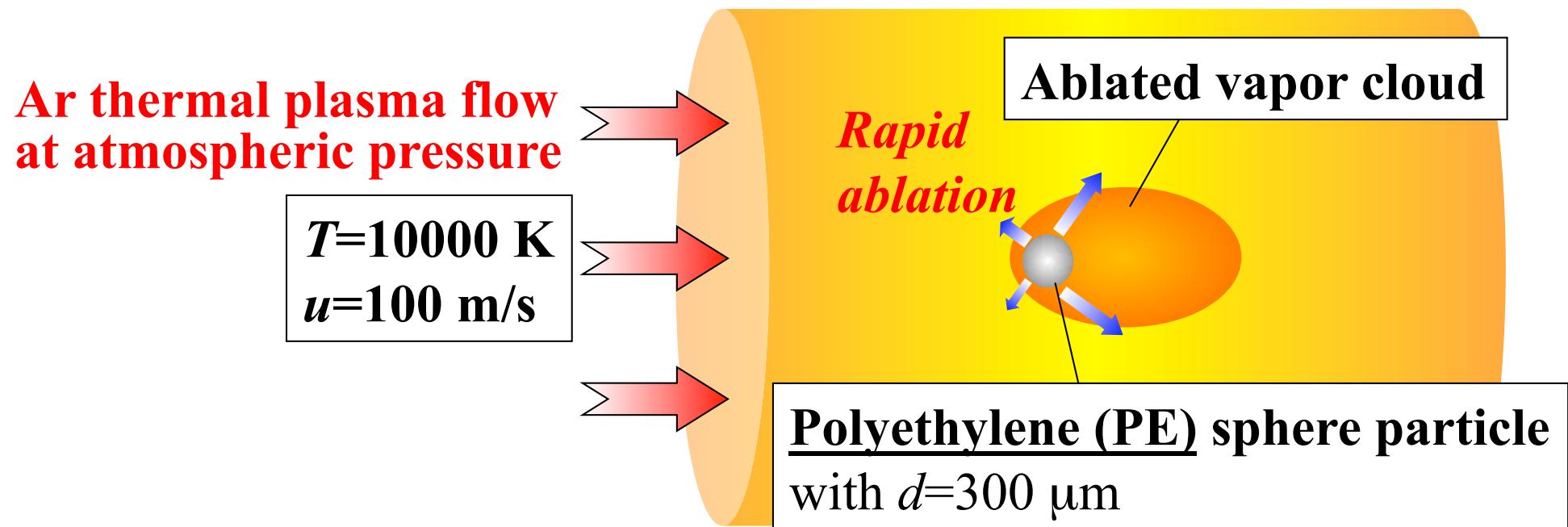
スポレーショん粒子が飛翔時に持つ初期エネルギー

1~100 nJ程度

高速度ビデオカメラ撮影 ⇒ 初期速さ 約2.5 m/s

直徑約0.15 mm

# The present case



## The physics to be considered:

- Heat transfer
- Rapid ablation  $\rightarrow$  Rapid pressure rise  $\rightarrow$  Strong gas flow
- Rapid ablation  $\rightarrow$  Energy loss
- Change in properties of the surrounding plasma
- Transport of ablated vapor
- Shielding due to the ablated vapor from Ar plasmas

# Governing Equations

-Mass equation:

$$\frac{D\rho}{Dt} = -\rho(\nabla \cdot \mathbf{u})$$

-Momentum equation:

$$\frac{Du}{Dt} = -\frac{1}{\rho} \nabla p$$

-Energy equation:

$$\frac{DT}{Dt} = -\frac{p_{th}}{\rho C_v} (\nabla \cdot \mathbf{u}) + \frac{1}{\rho C_v} [\nabla \cdot (\lambda \nabla T) - P_{rad} - S_{abl} - \varepsilon_{emit} \sigma_{sb} (T^4 - T_a^4) \delta \Omega]$$

-Mass fraction of ablated vapor:

$$\frac{DY_{pol}}{Dt} = \frac{1}{\rho_g} [\nabla \cdot (\rho_g D_{pol} \nabla Y_{pol}) + S_{Cg}]$$

-VOF function:

$$\frac{Df}{Dt} = -S_f$$

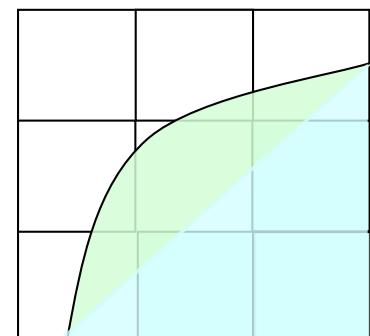
-Equation of state (EOS):

$$p = p(\rho, T)$$

**These equations are solved by the CIP-CUP method developed by Prof. Yabe.**

The **CIP-CUP method** is an **unified algorithm to solve incompressible and compressible flow, and thus it can simulate multiphase flow.**

heat



$$f = \frac{V_{solid}}{V_{cv}}$$

$$\left\{ \begin{array}{l} f=1: \text{Solid} \\ 0 < f < 1: \text{containing solid surface} \\ f=0: \text{Gas or plasma} \end{array} \right.$$

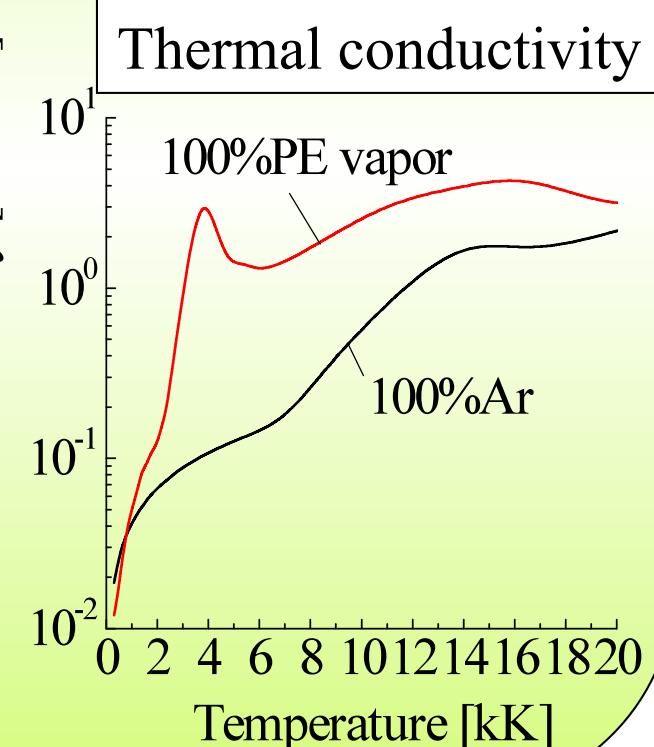
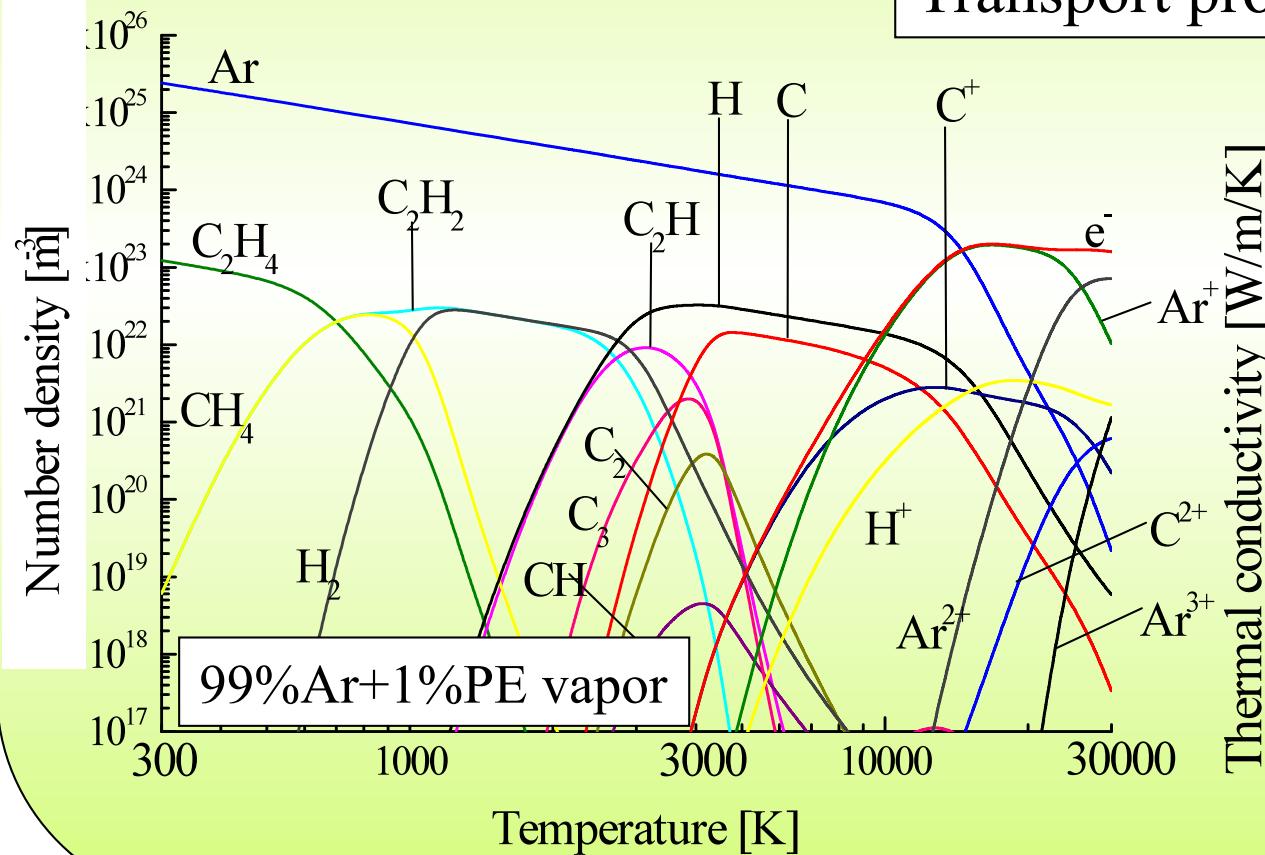
# *Thermodynamic and transport properties of Ar and ablated vapor*

Equilibrium composition of Ar, and ablated vapor

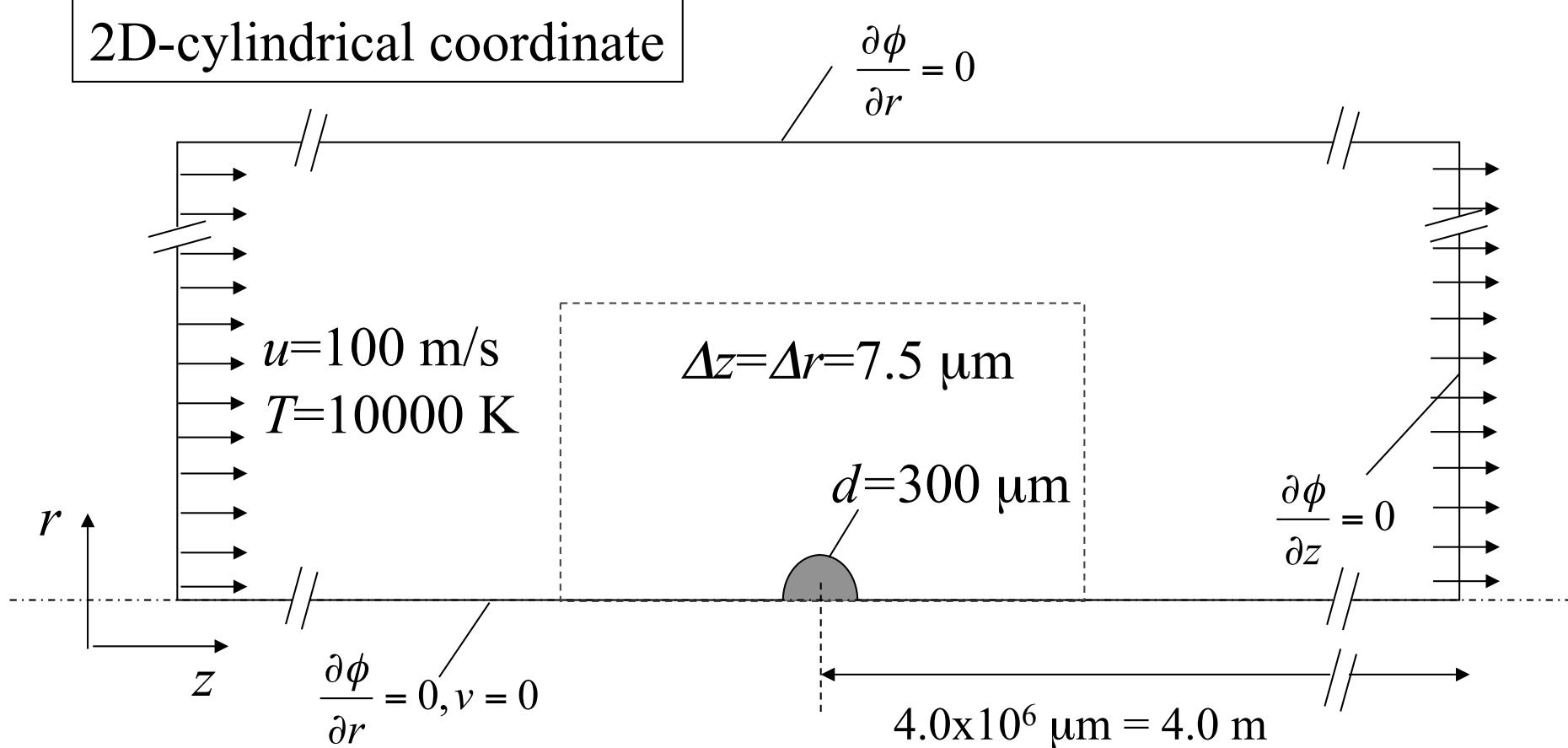
Thermodynamic properties

The first order approximation  
of Chapman-Enskog method

Transport properties



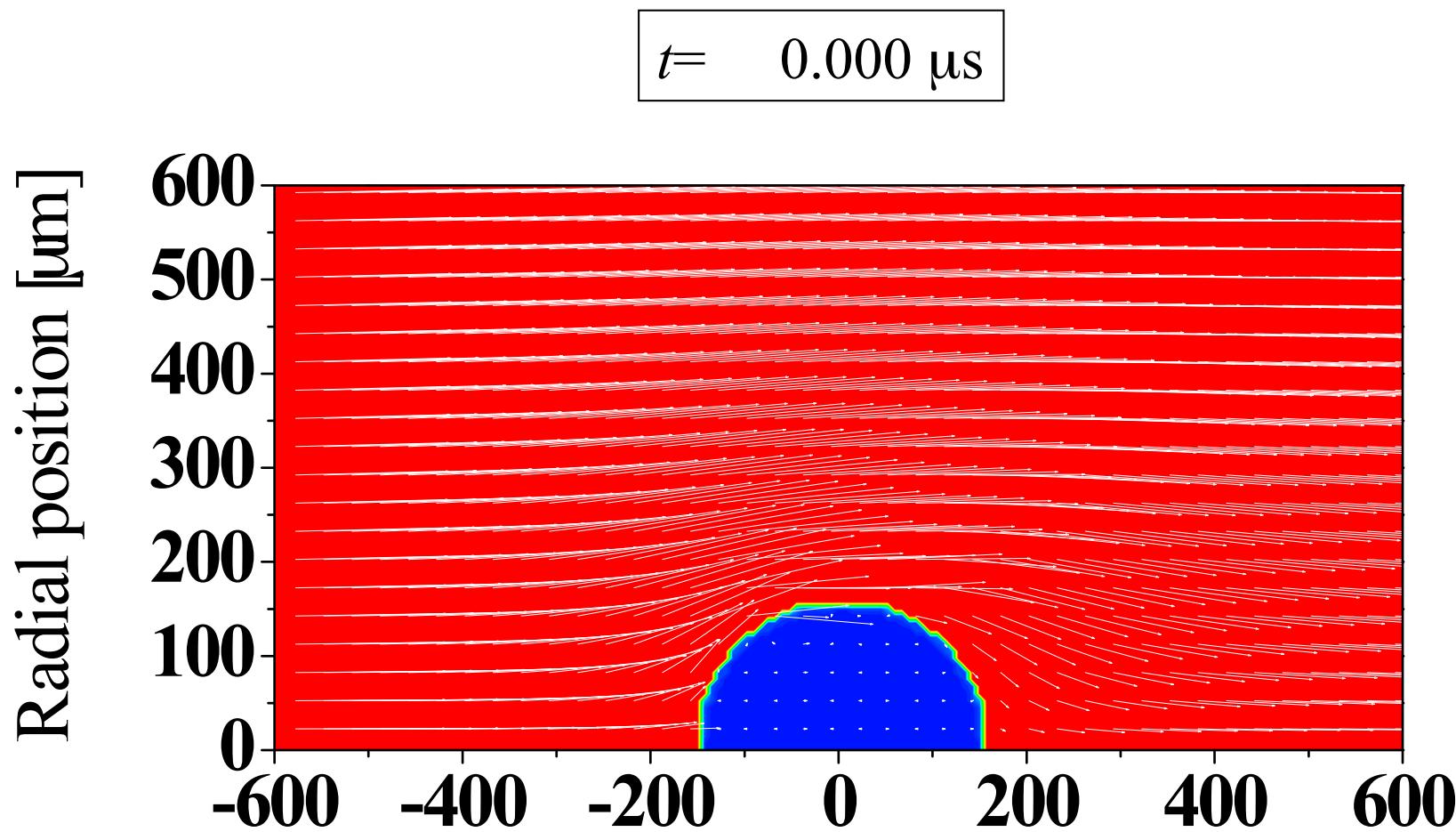
# *Calculation space*



-Kundsen number:  $Ku \sim 0.03$

-Reynolds number:  $Re \sim 0.65$

# *Gas flow velocity and temperature fields*

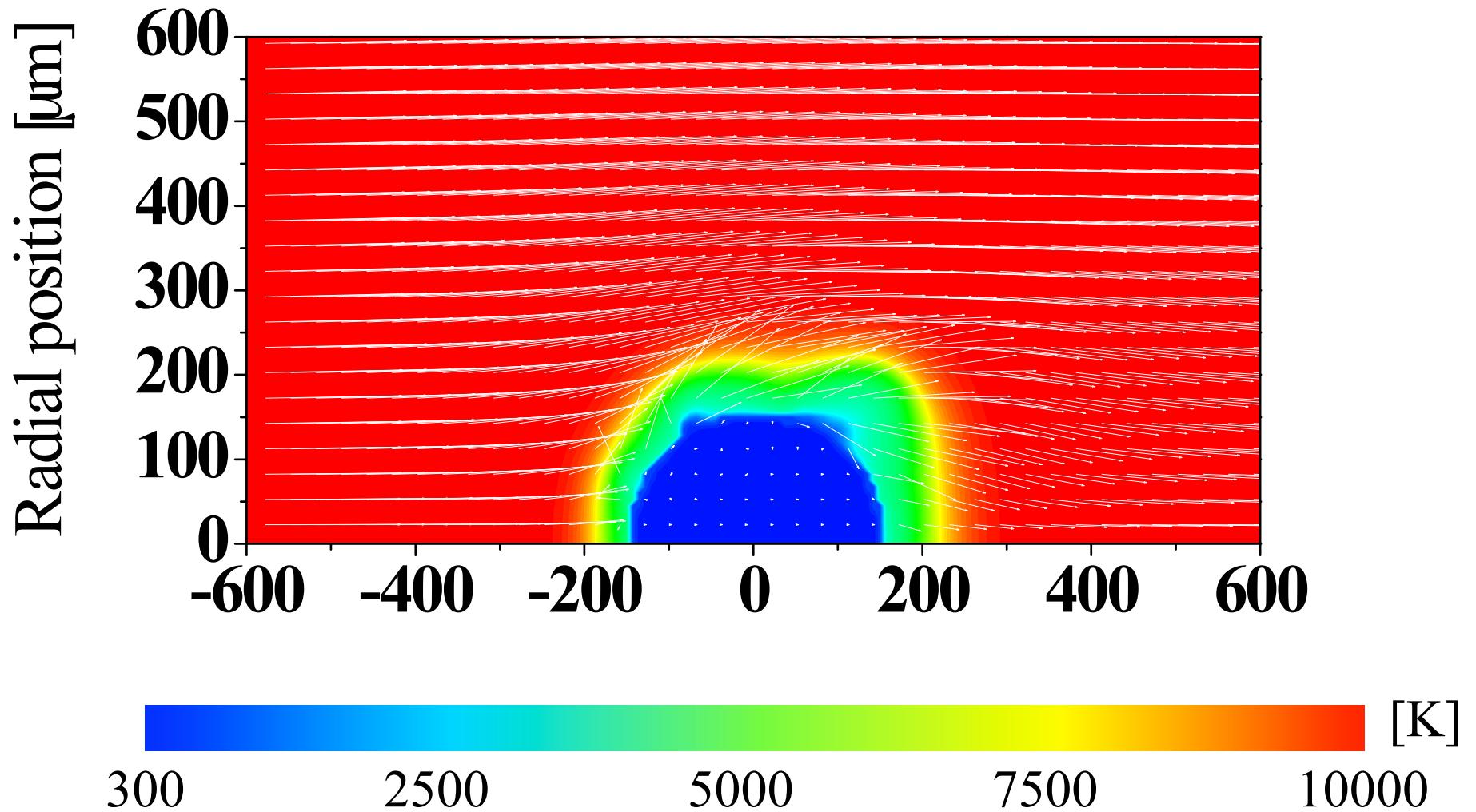


Initial temperature:  $T=10000 \text{ K}$  for Ar plasma,  $T=300 \text{ K}$  for PE particle  
Initial gas flow field was calculated without ablation



## *Gas flow velocity and temperature fields*

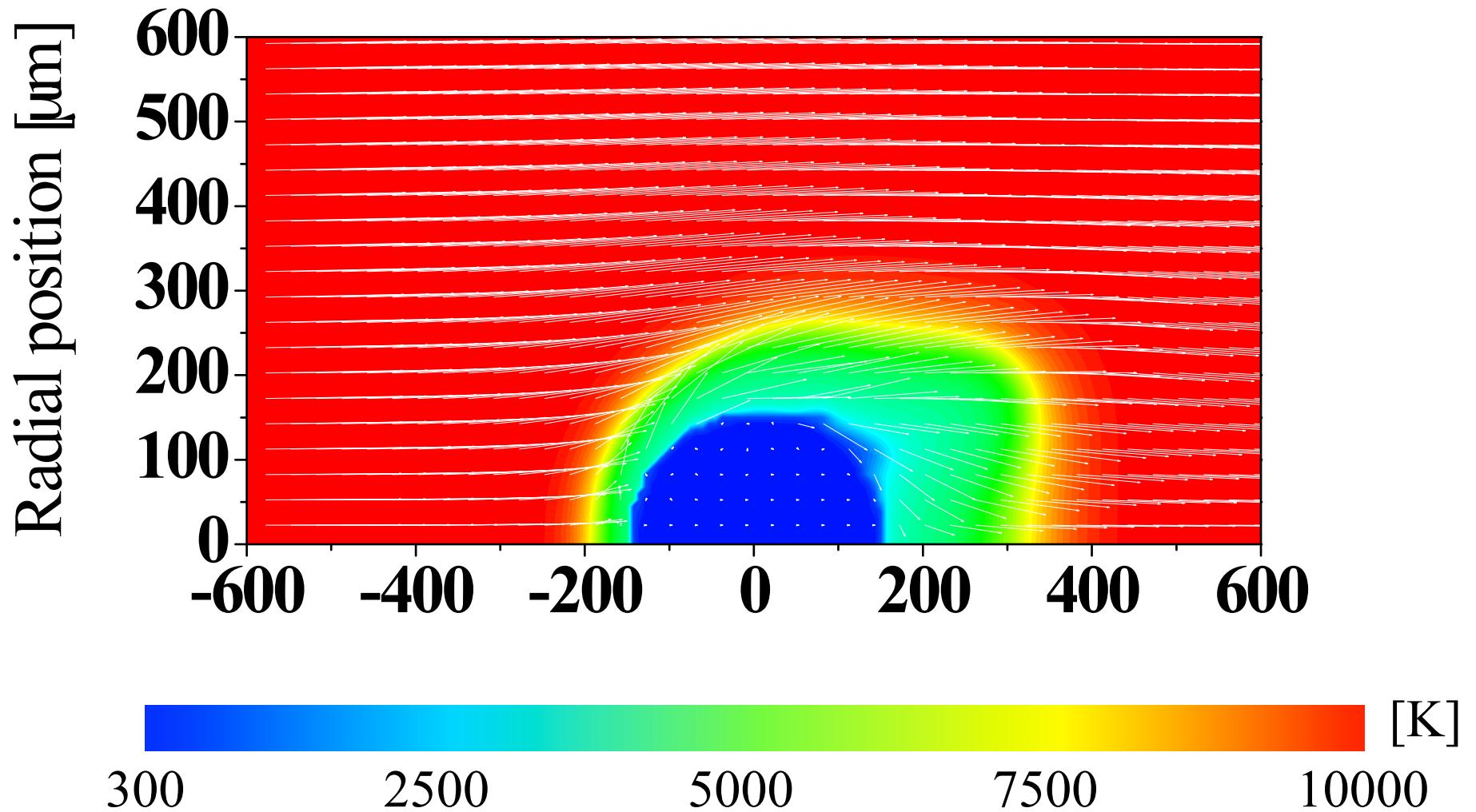
$t = 1.371 \mu\text{s}$





## *Gas flow velocity and temperature fields*

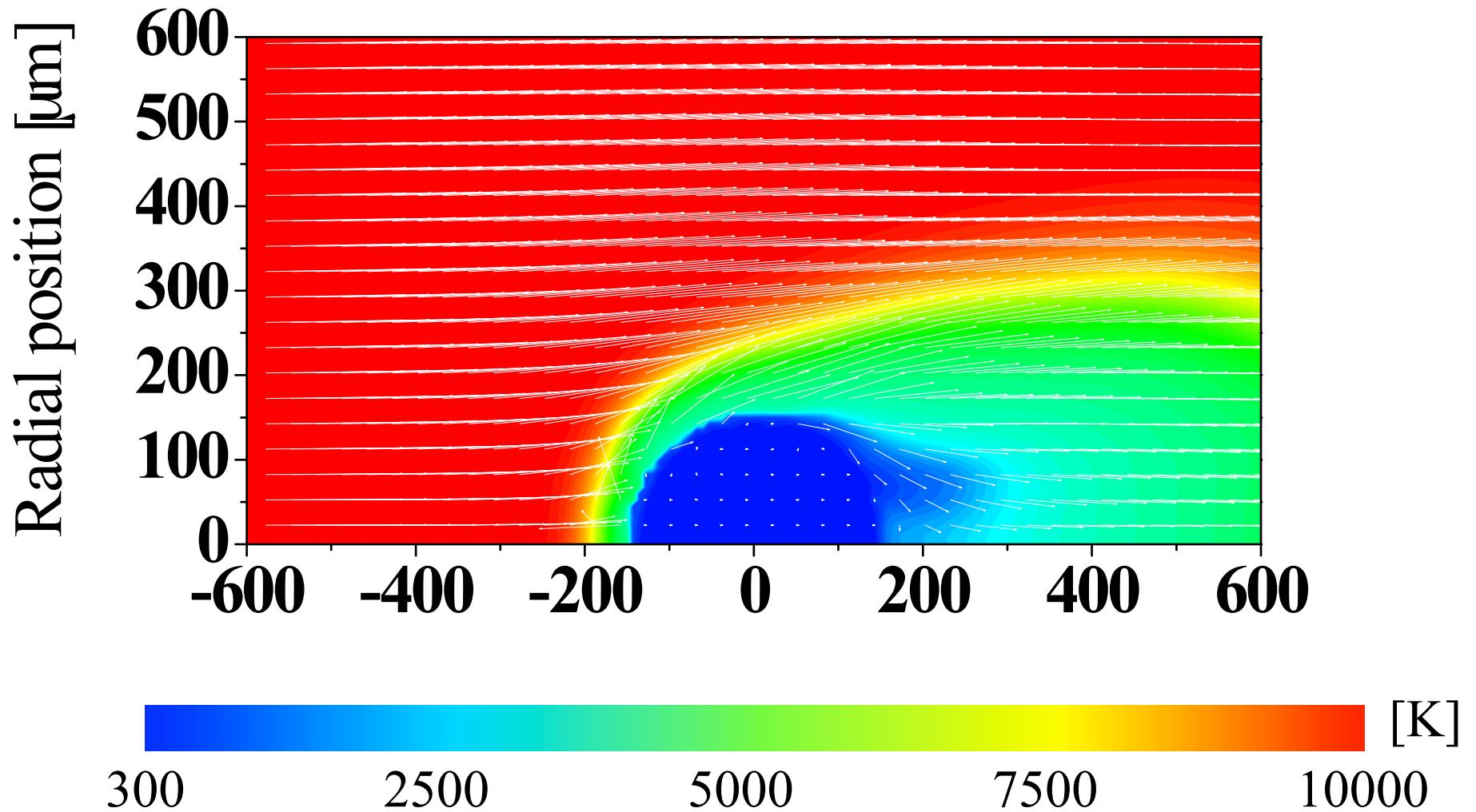
$t = 3.185 \mu\text{s}$





## *Gas flow velocity and temperature fields*

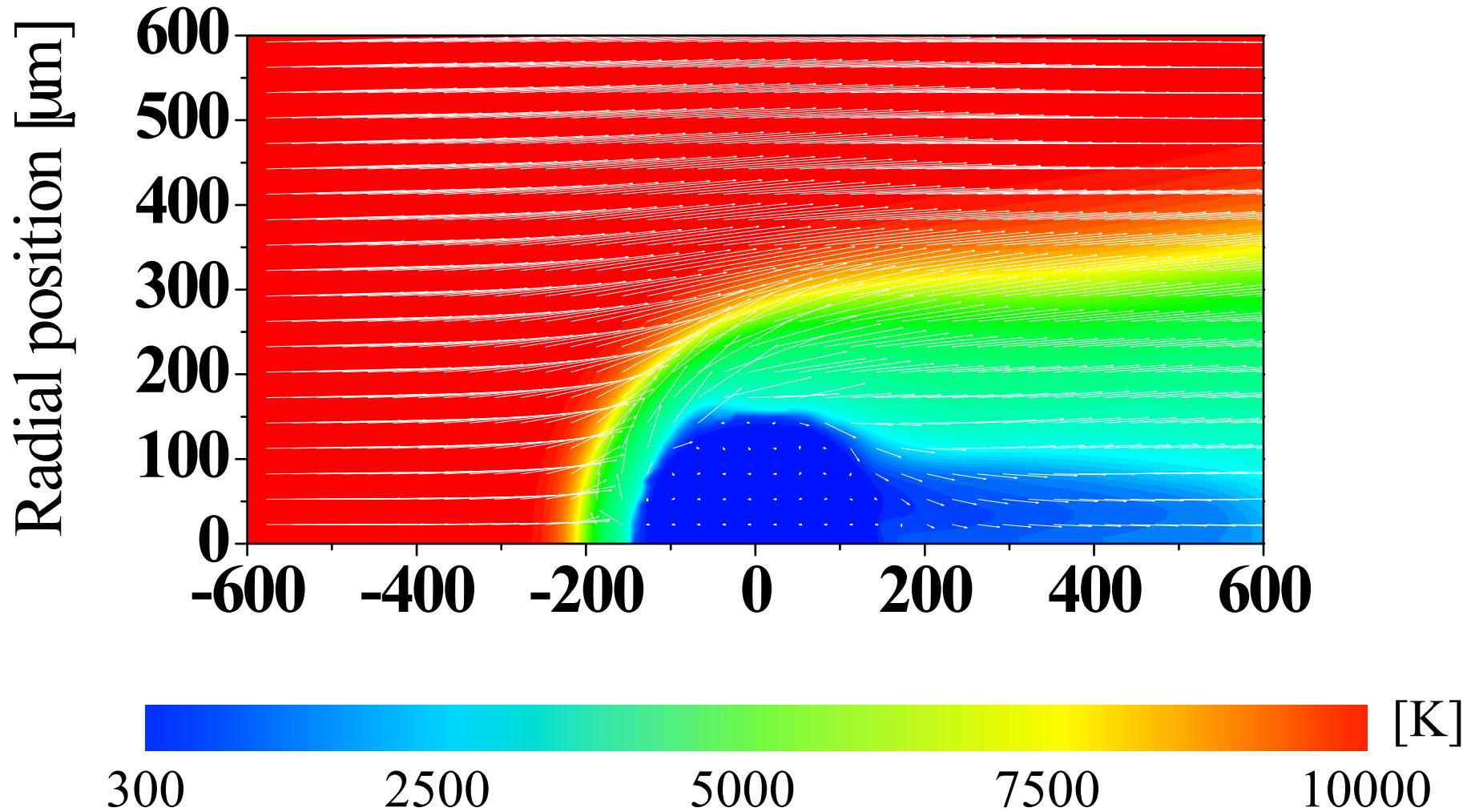
$t = 8.736 \mu\text{s}$





## *Gas flow velocity and temperature fields*

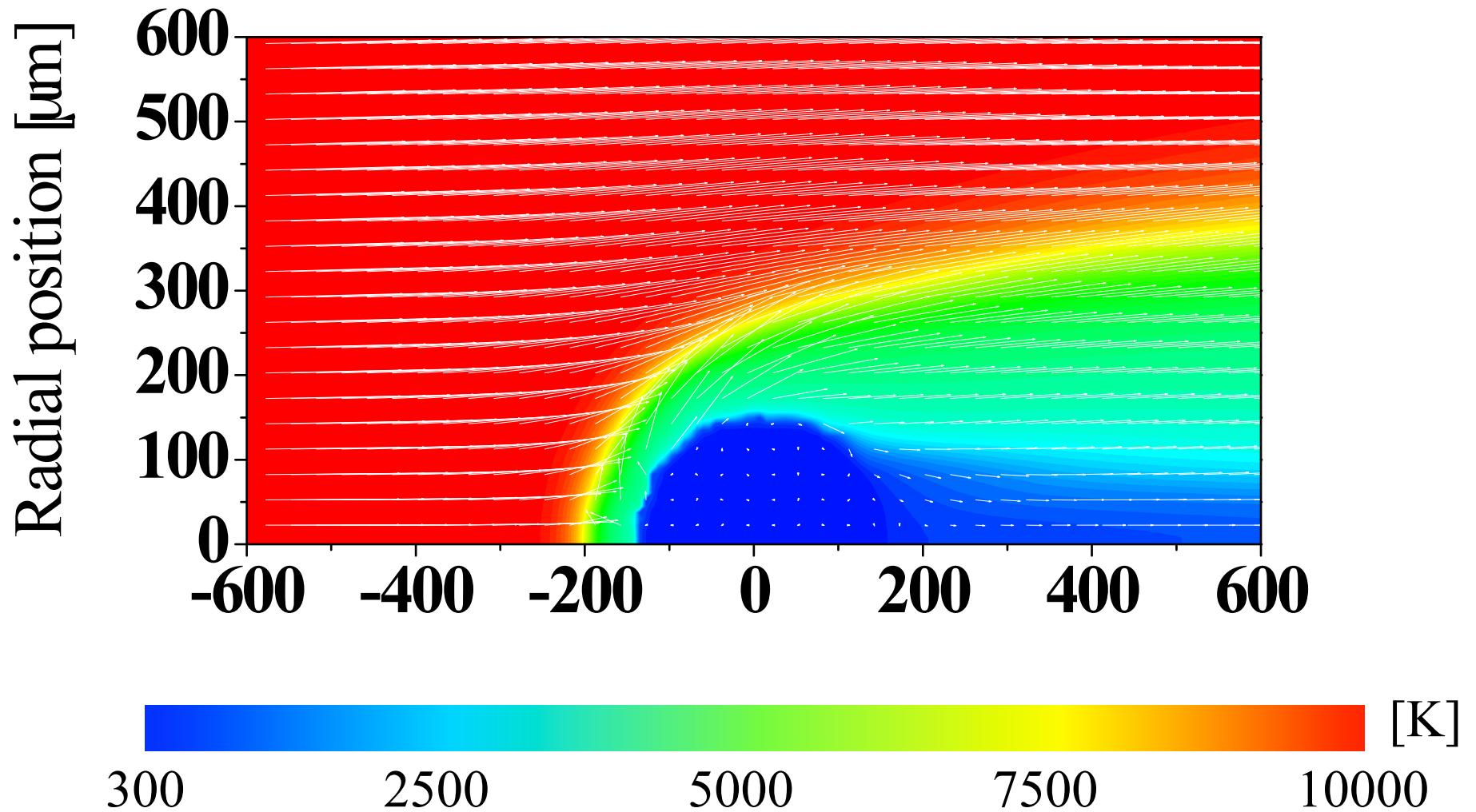
$t = 17.56 \mu\text{s}$





# *Gas flow velocity and temperature fields*

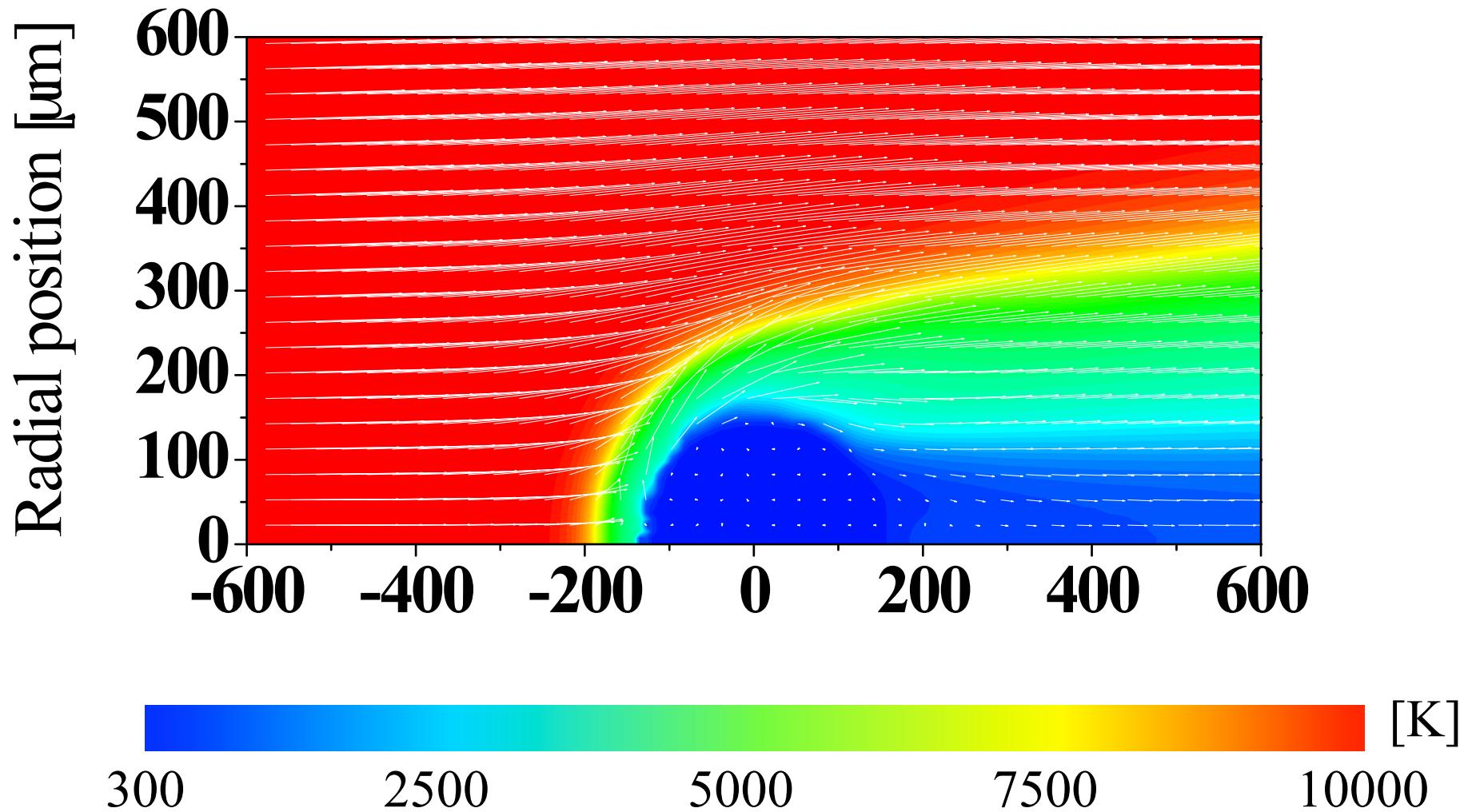
$t = 35.71 \mu\text{s}$





## *Gas flow velocity and temperature fields*

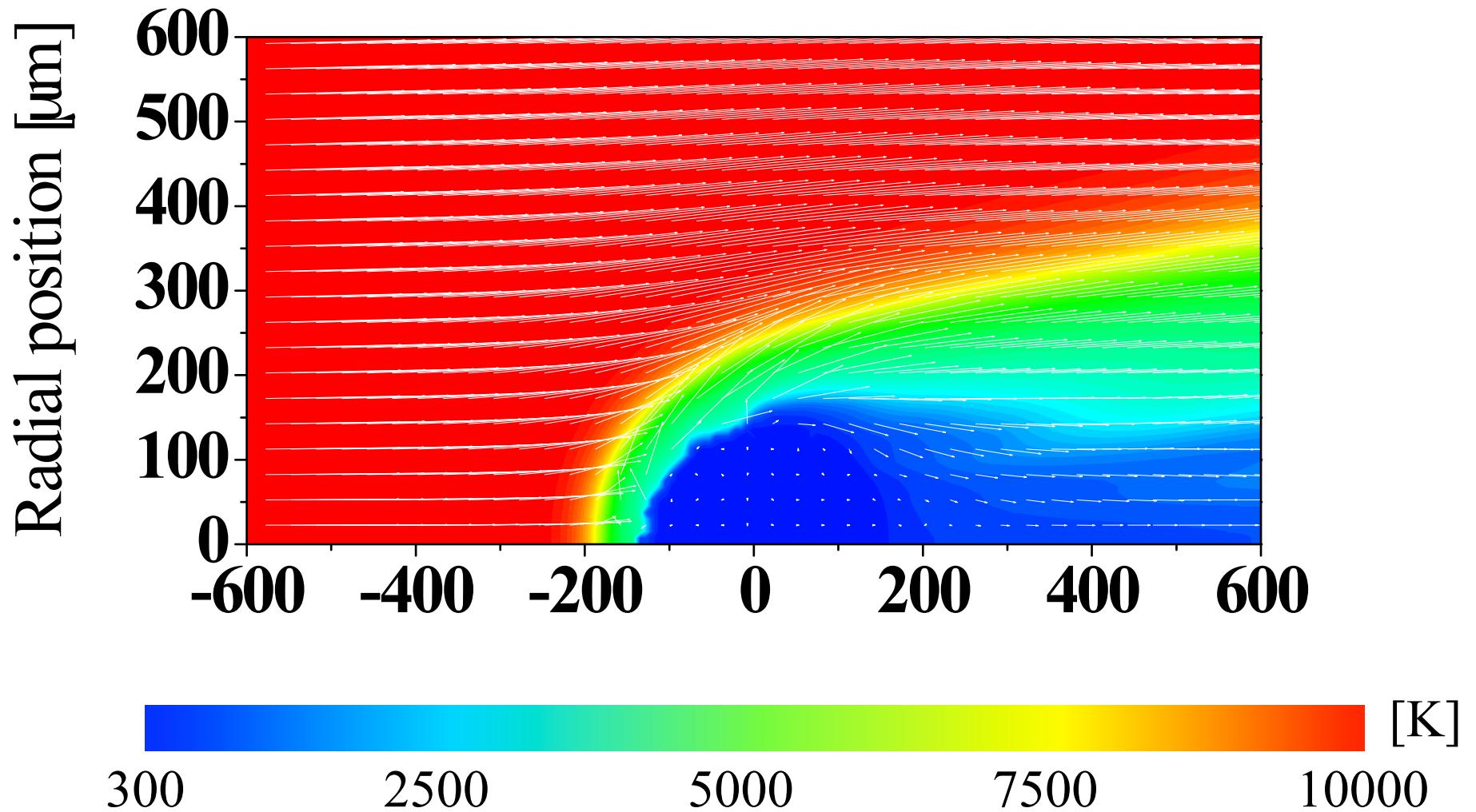
$t = 91.25 \mu\text{s}$





## *Gas flow velocity and temperature fields*

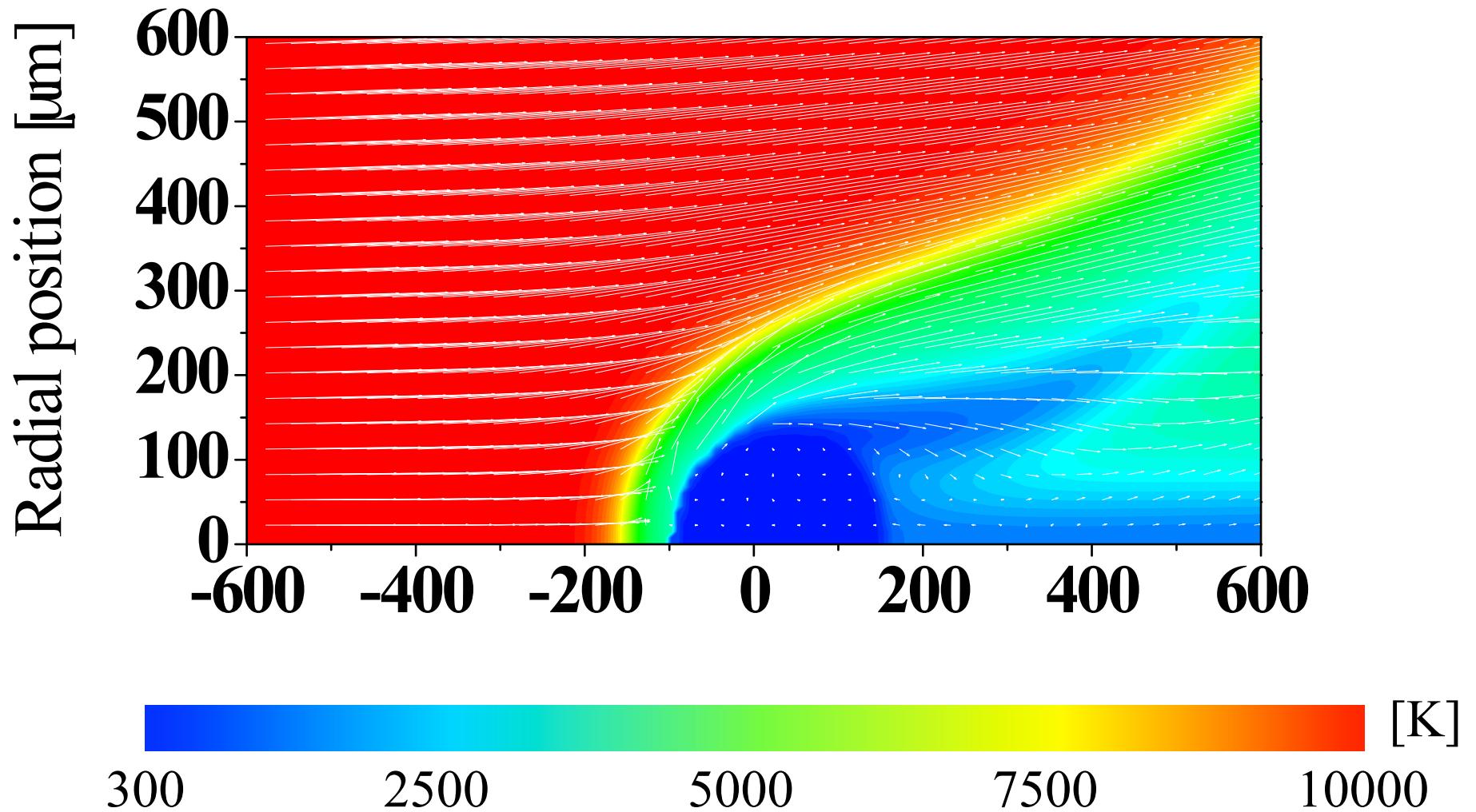
$t = 183.0 \mu\text{s}$





# *Gas flow velocity and temperature fields*

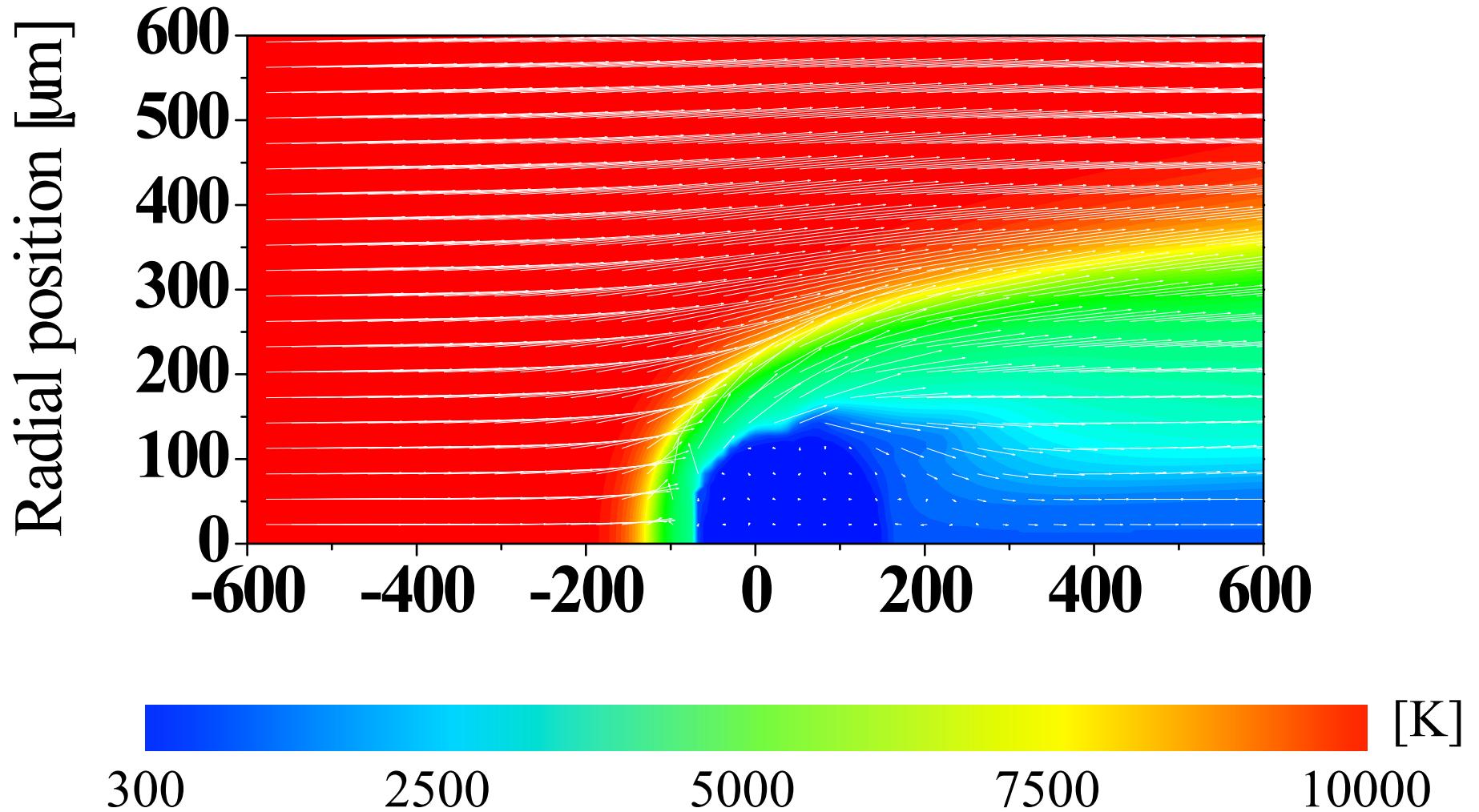
$t = 344.7 \mu\text{s}$

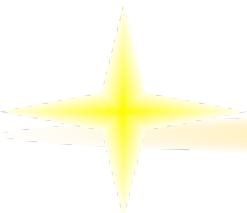




## *Gas flow velocity and temperature fields*

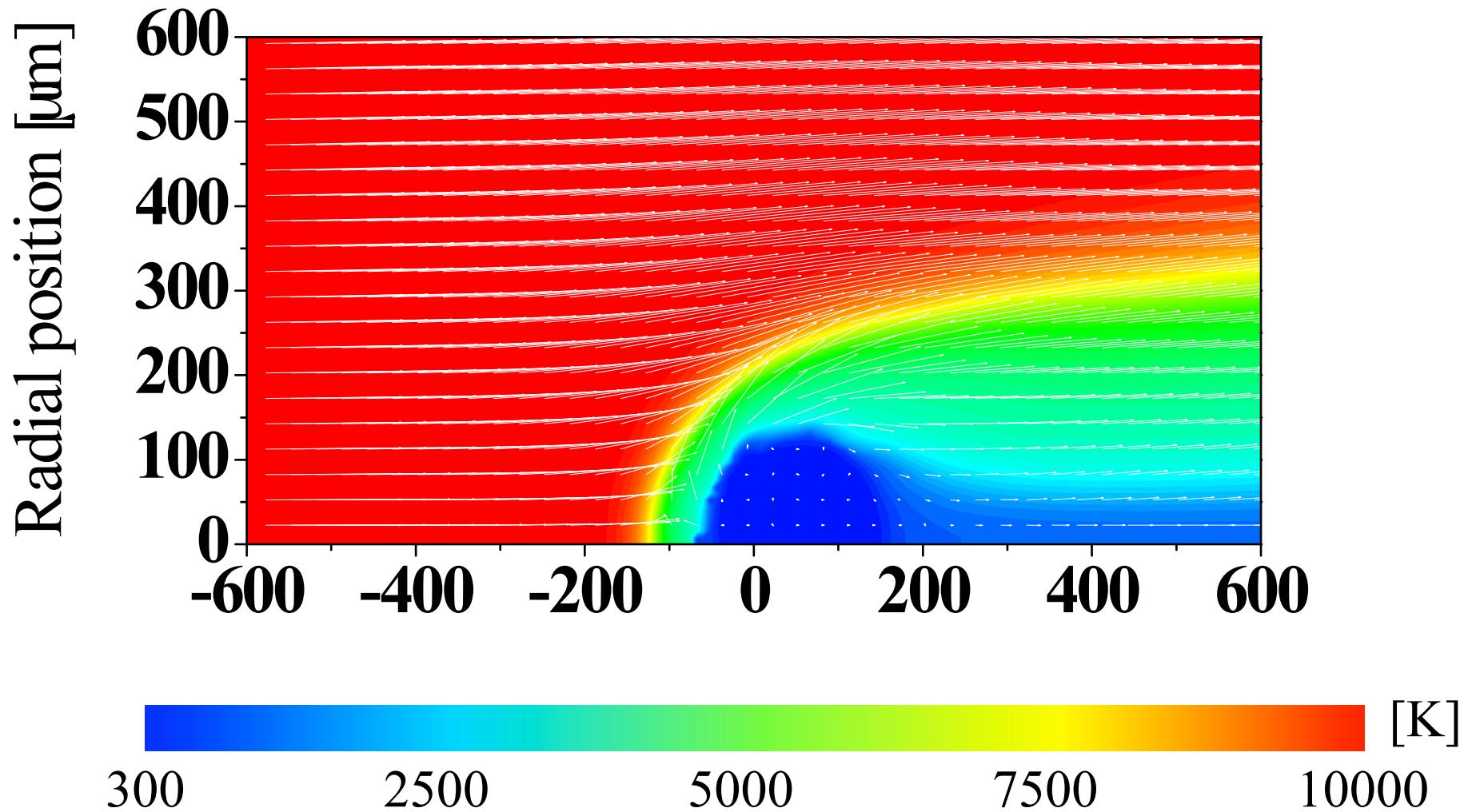
$t = 430.7 \mu\text{s}$





## *Gas flow velocity and temperature fields*

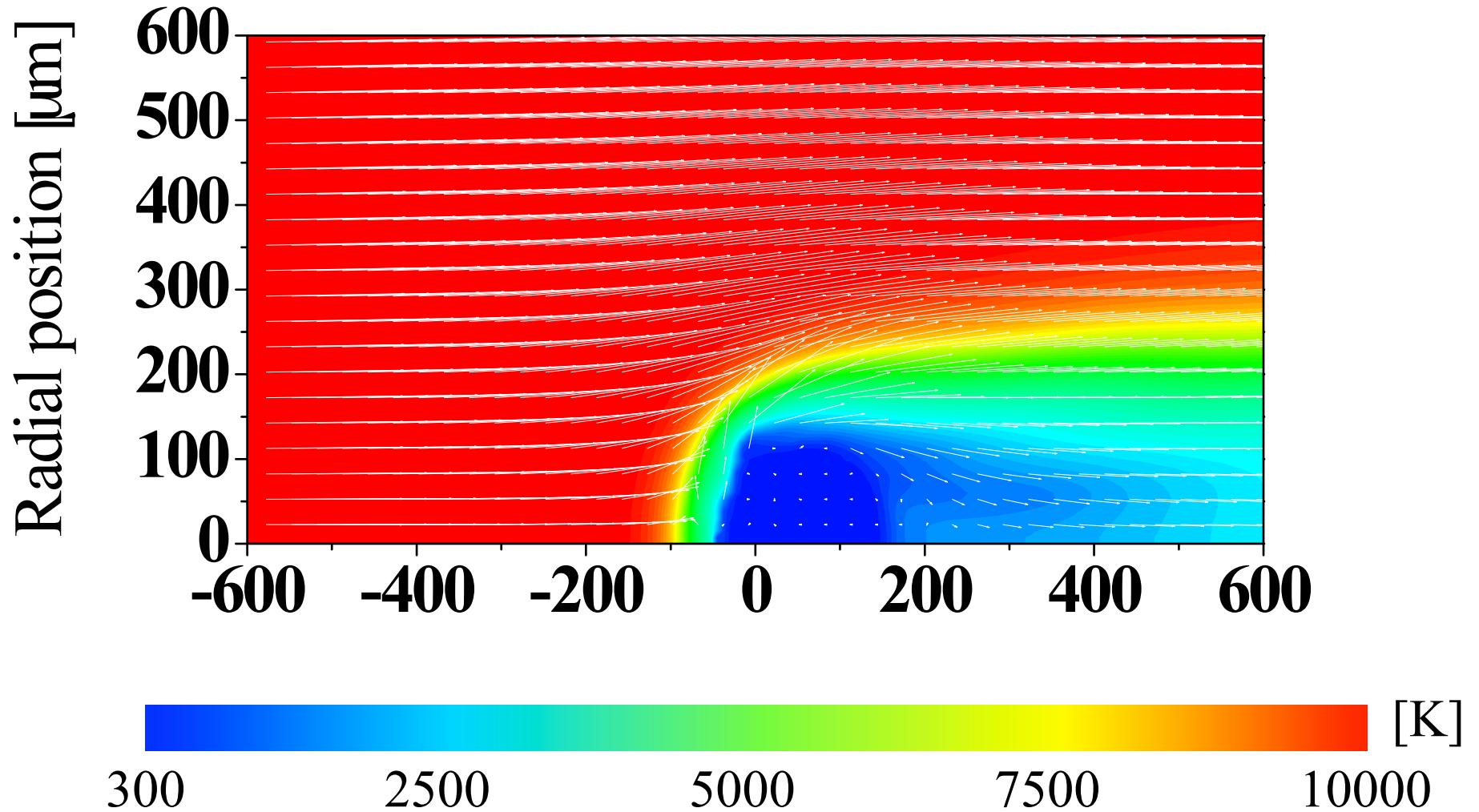
$t = 523.4 \mu\text{s}$





## *Gas flow velocity and temperature fields*

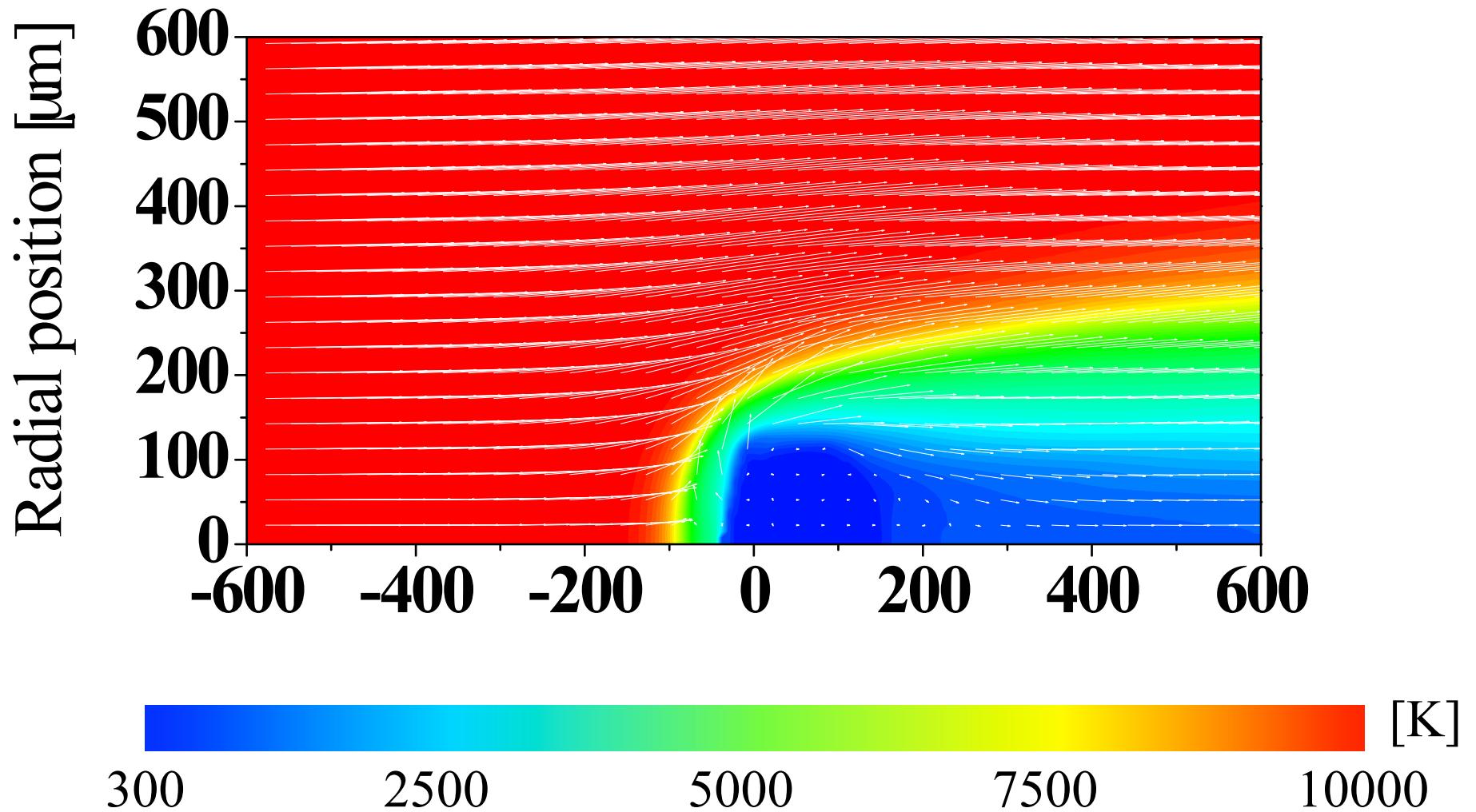
$t = 616.51 \mu\text{s}$





## *Gas flow velocity and temperature fields*

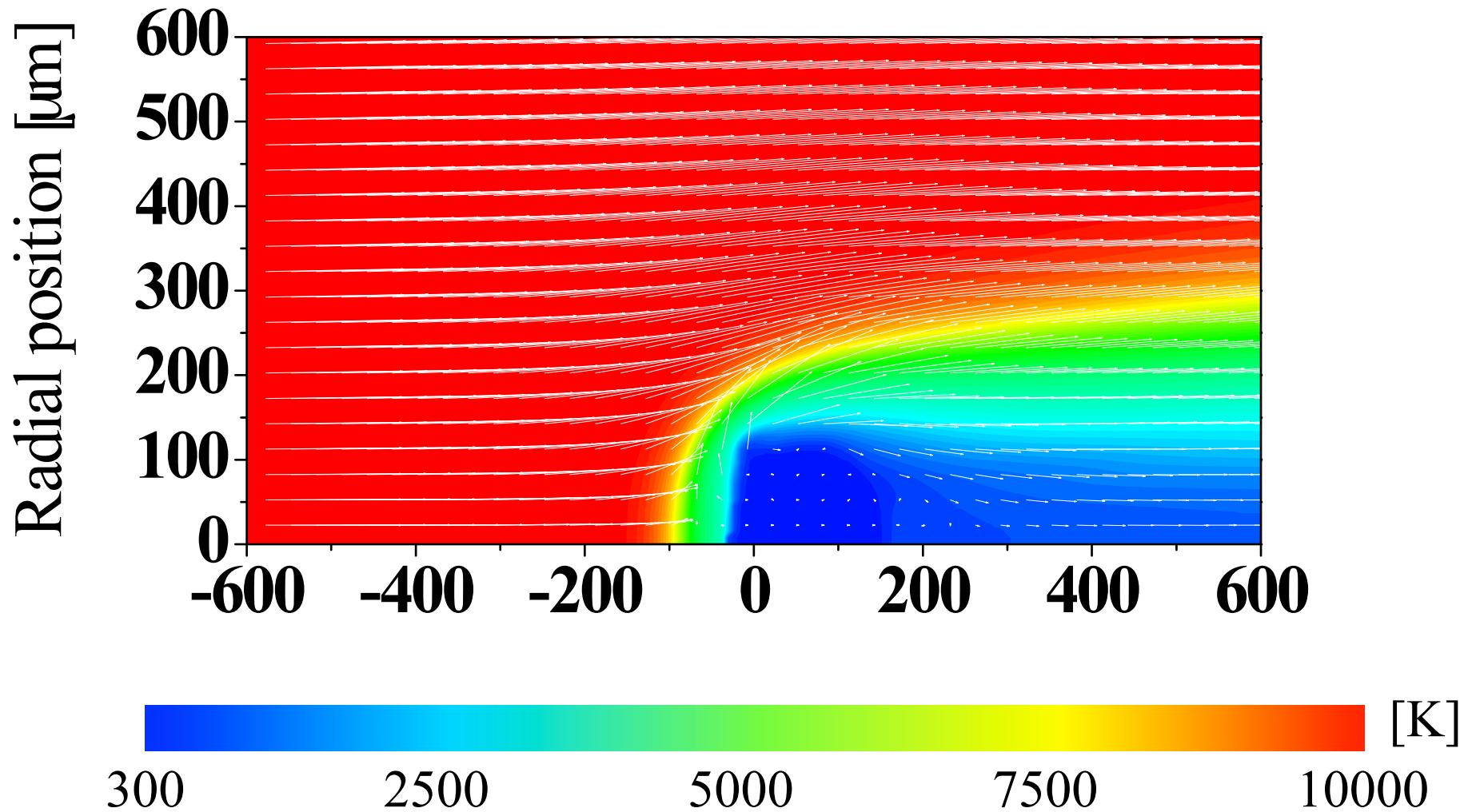
$t = 709.89 \mu\text{s}$





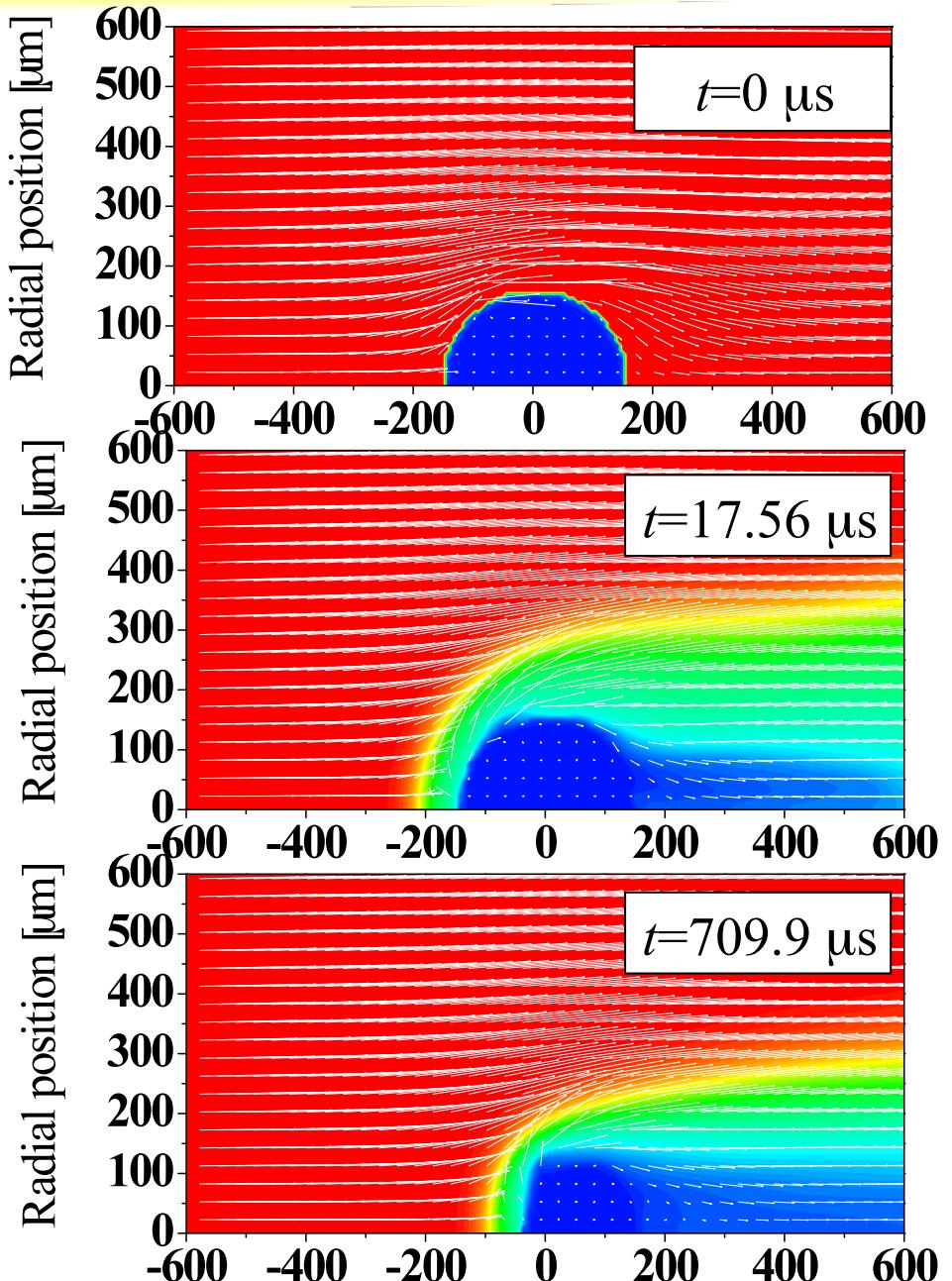
## *Gas flow velocity and temperature fields*

$t = 803.33 \mu\text{s}$

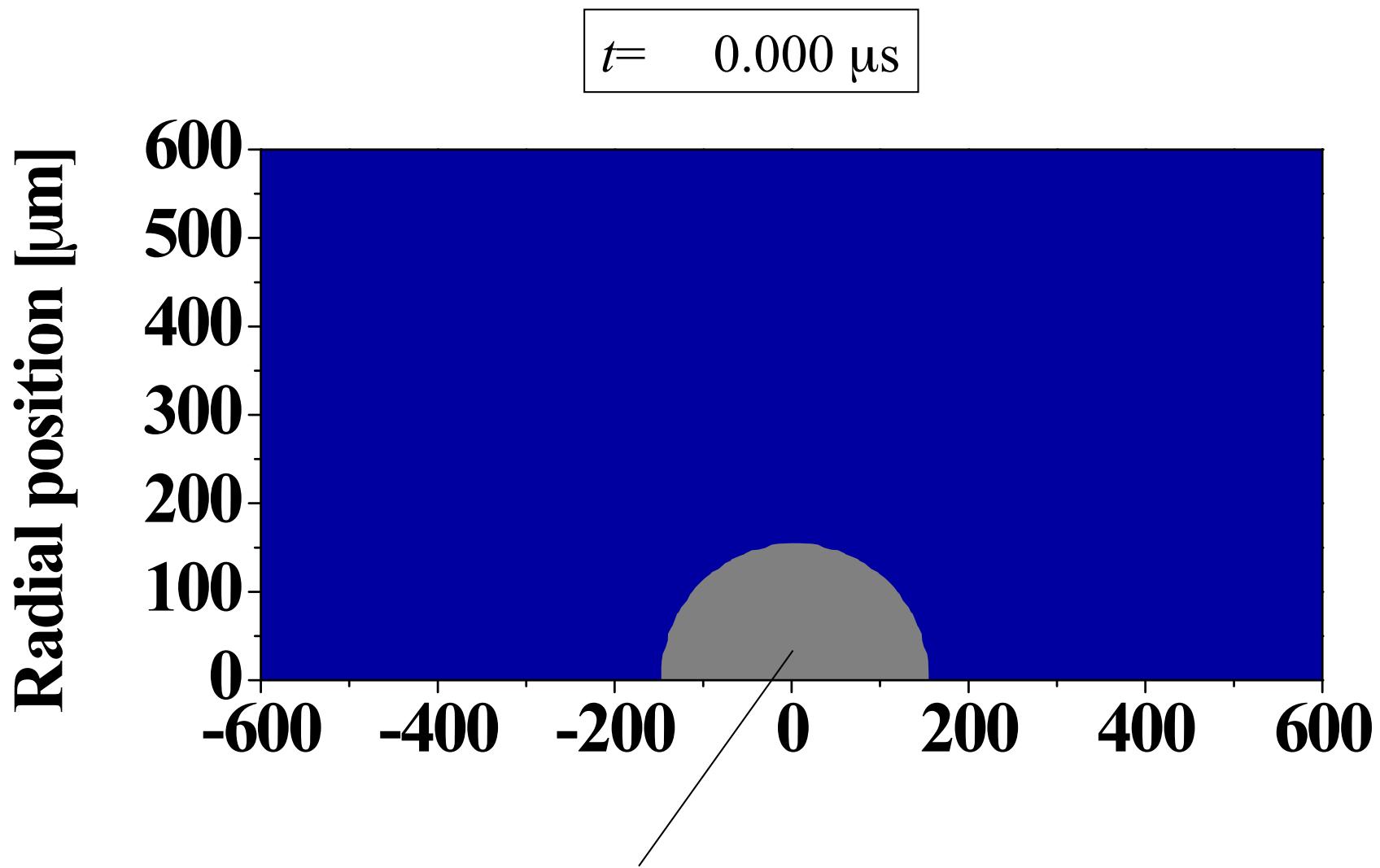


## *Time evolution in gas flow and temperature fields*

- Rapid ablation occurs especially at upstream surface of the solid particle, which produces gas flow.
- Temperature around the particle is decreased because of thermal conduction and convection by low temperature ablated vapor.
- The ablated vapor shields the solid particle from direct interaction with the Ar plasma.



## *Mass fraction of ablated vapor and VOF function*

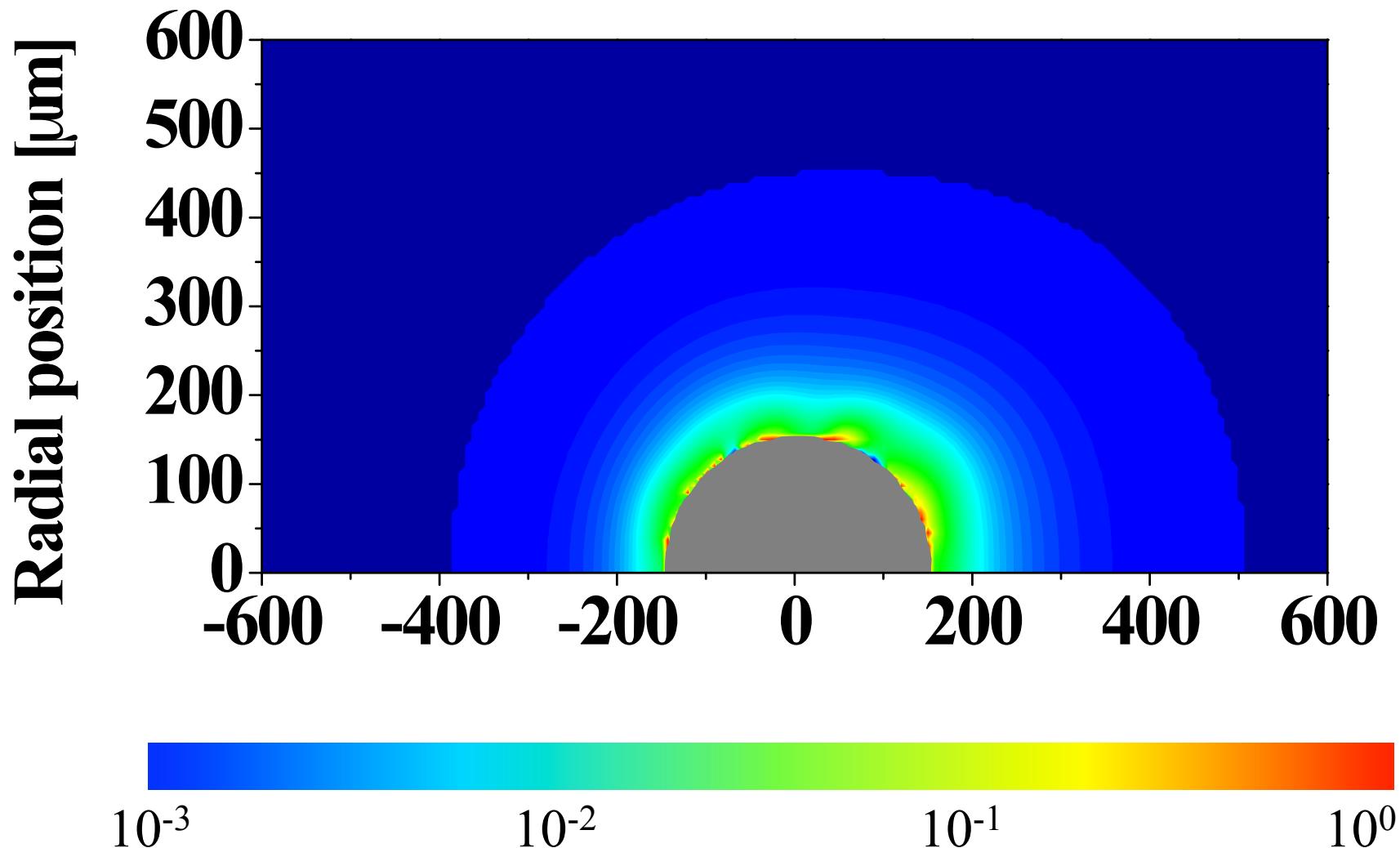


The VOF function. If  $f > 0.5$ , the color is gray



## *Mass fraction of ablated vapor*

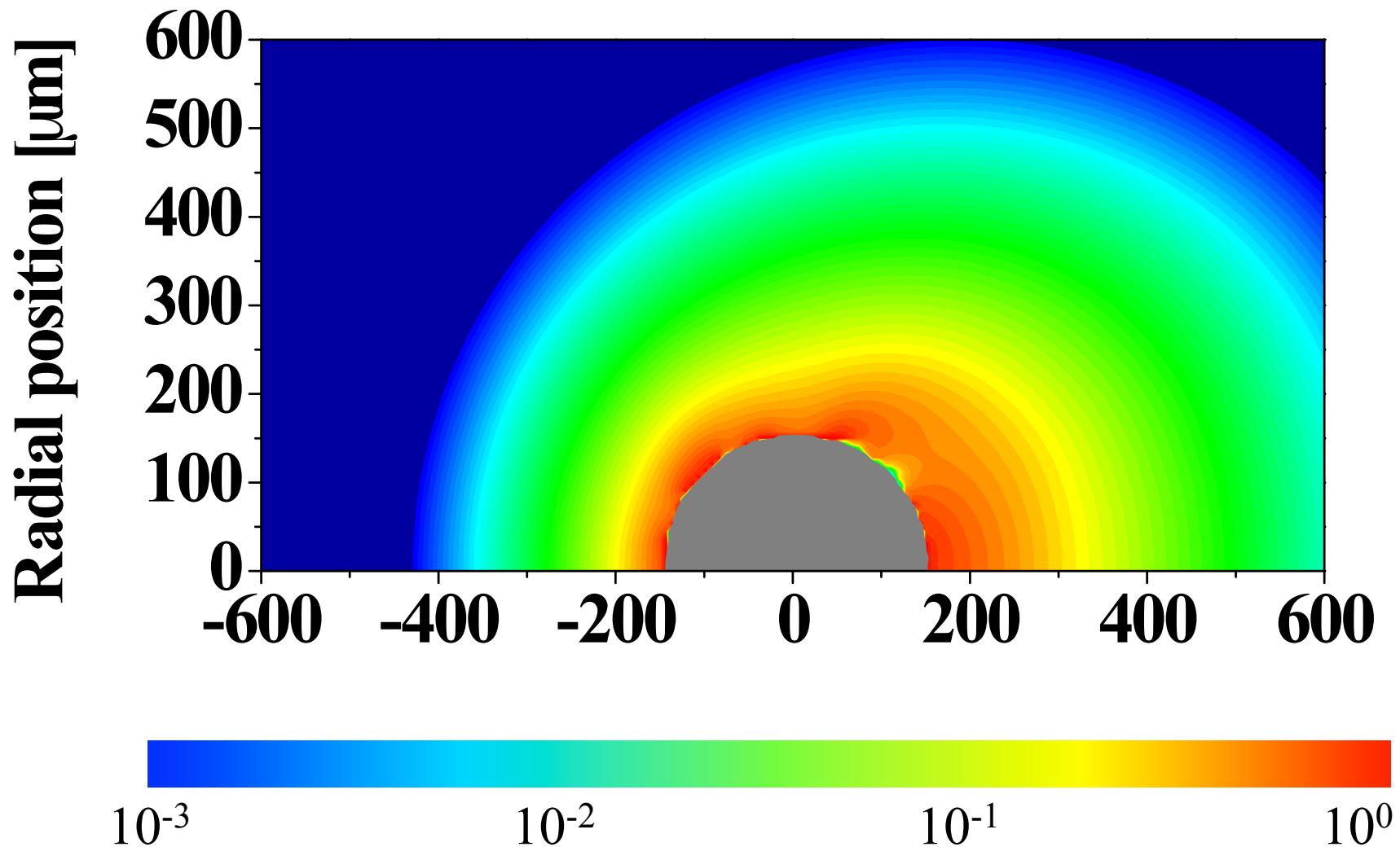
$t = 1.371 \mu\text{s}$





## *Mass fraction of ablated vapor*

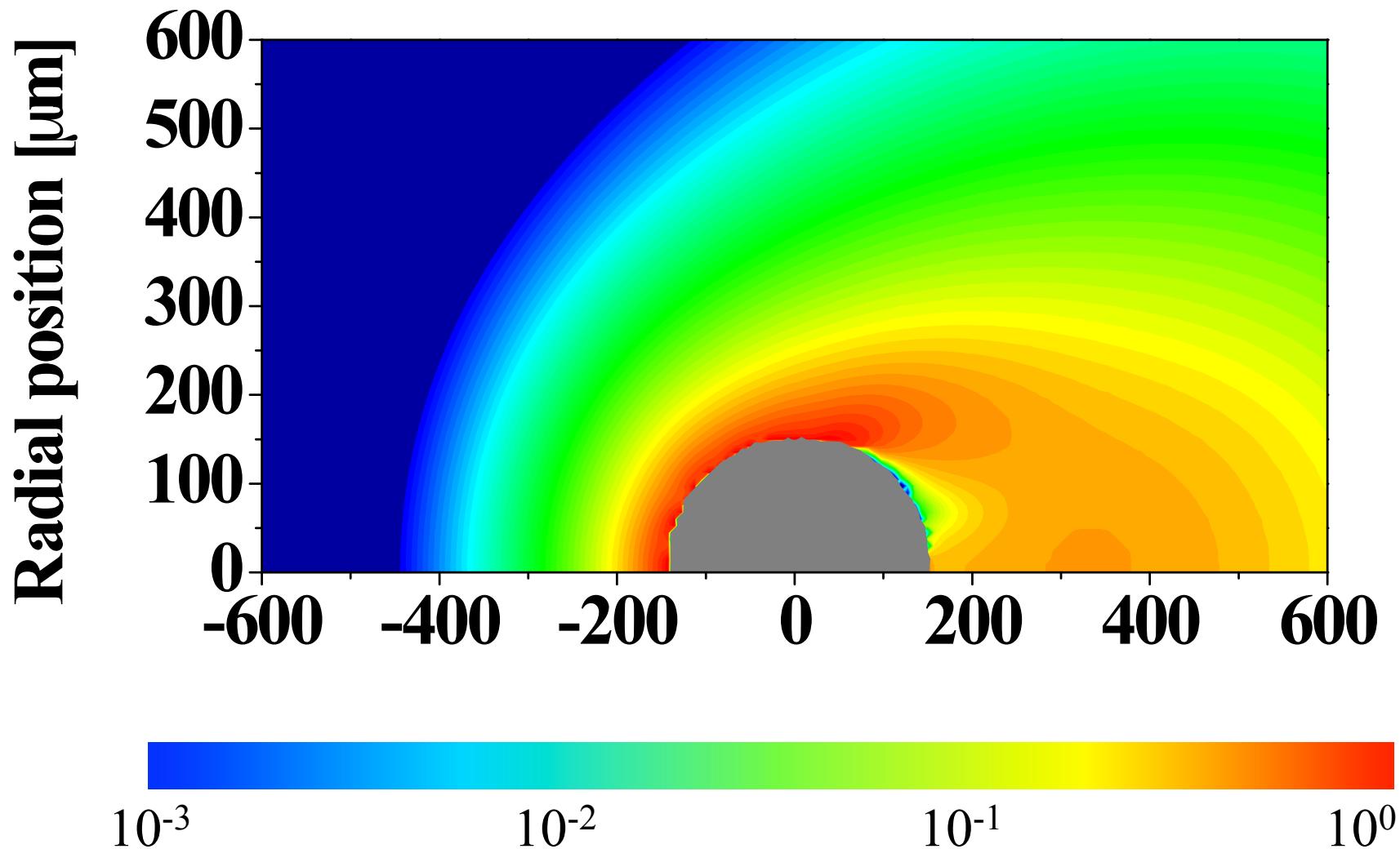
$t = 3.185 \mu\text{s}$





## *Mass fraction of ablated vapor*

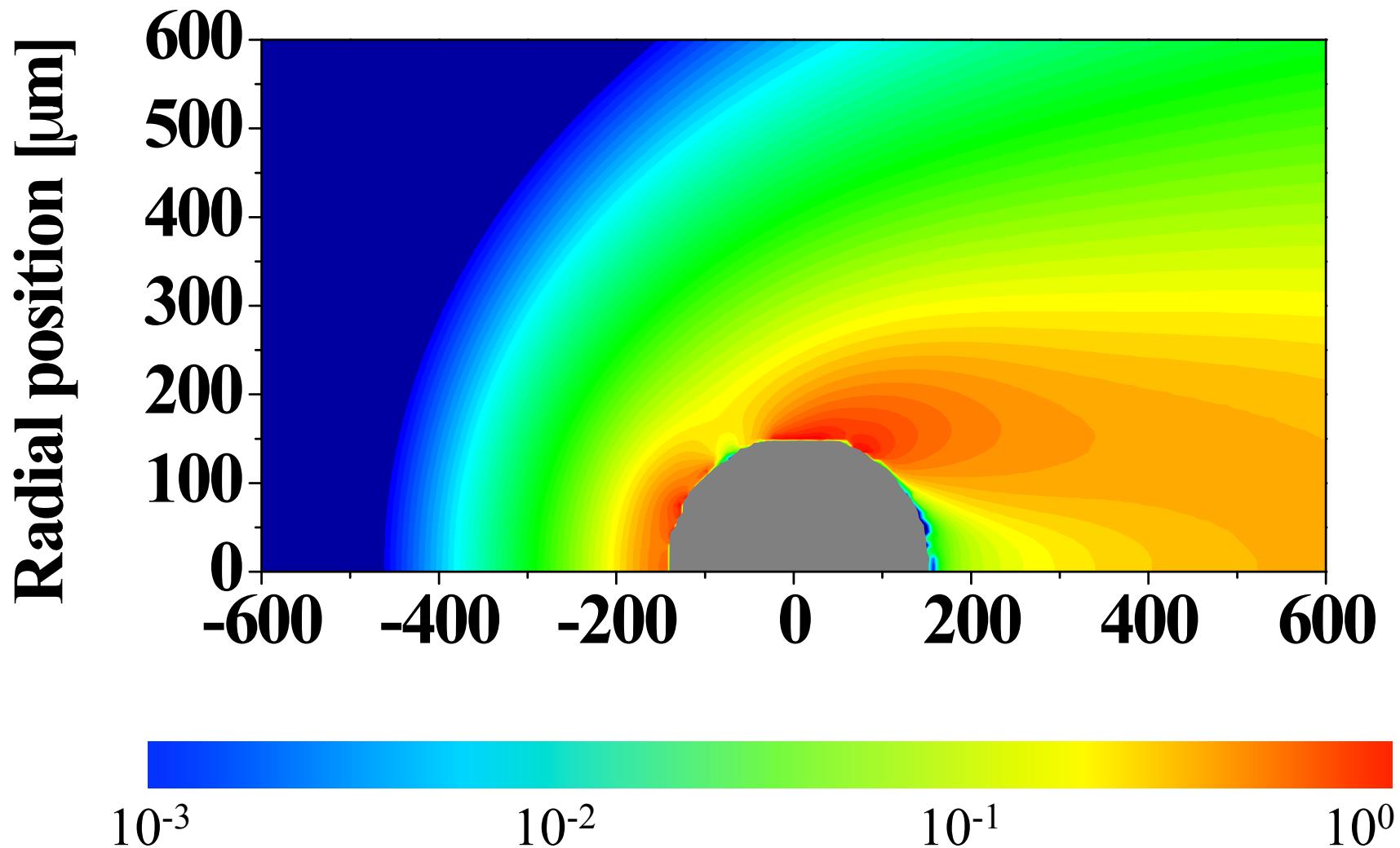
$t = 8.736 \mu\text{s}$



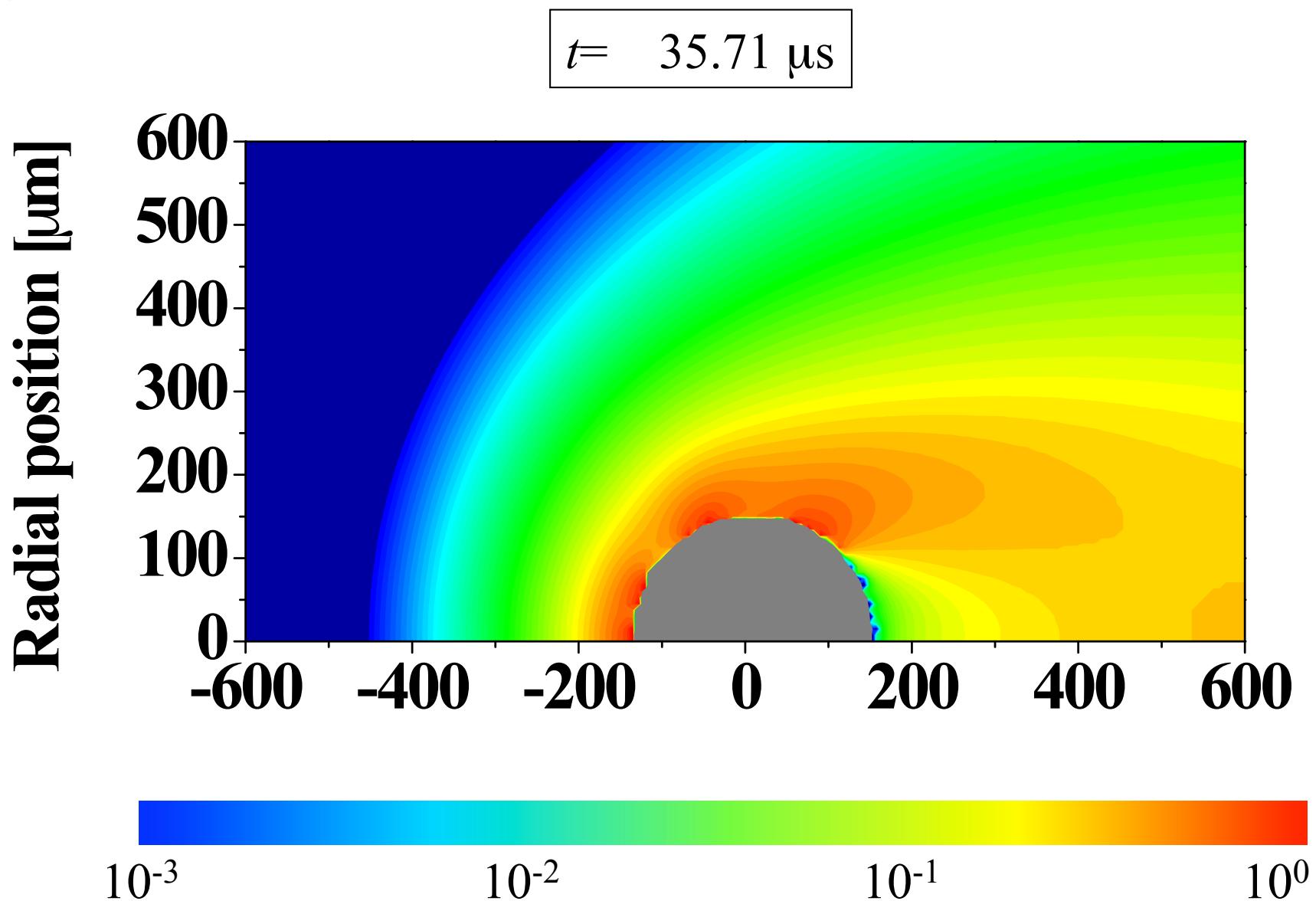


## *Mass fraction of ablated vapor*

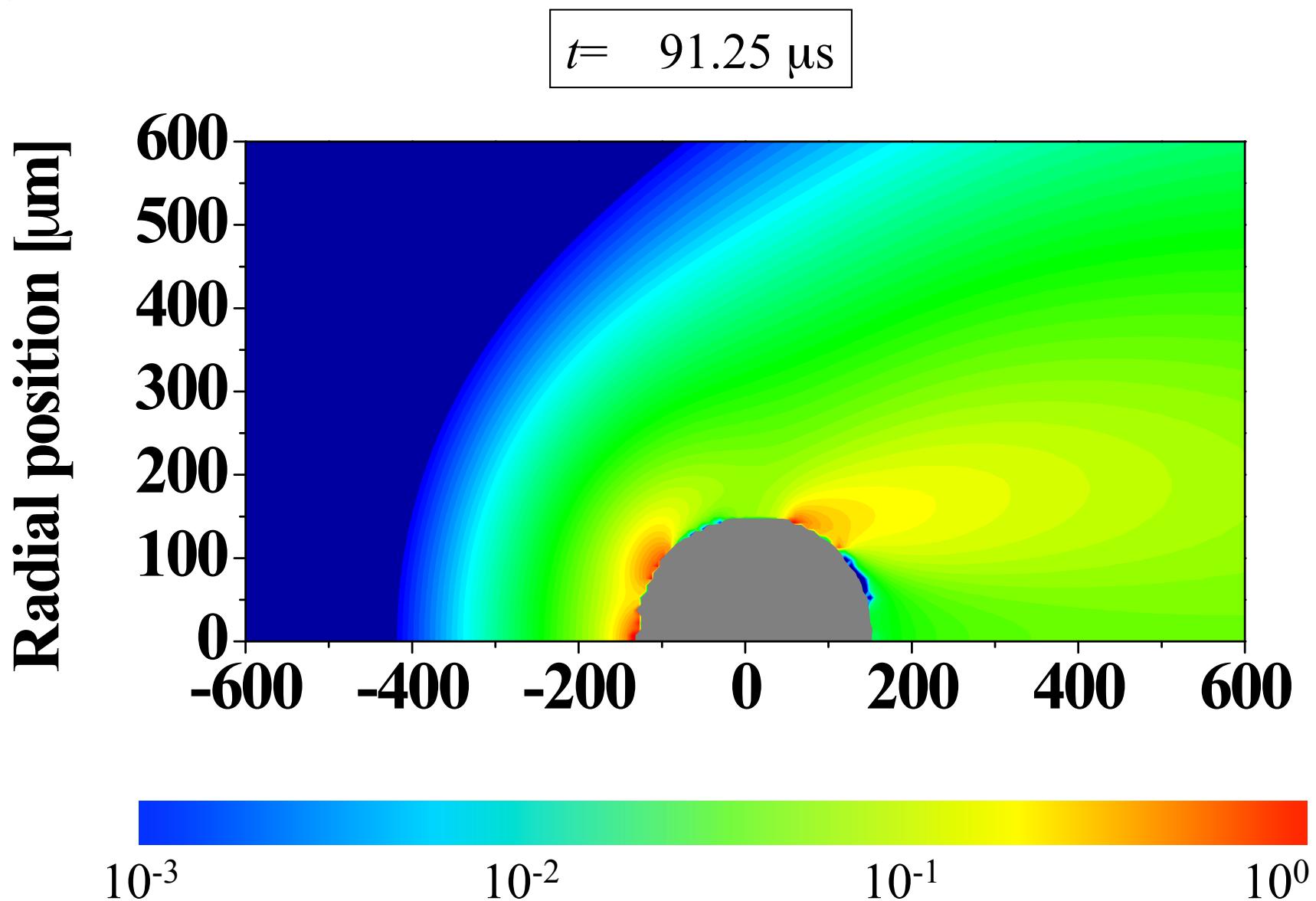
$t = 17.56 \mu\text{s}$



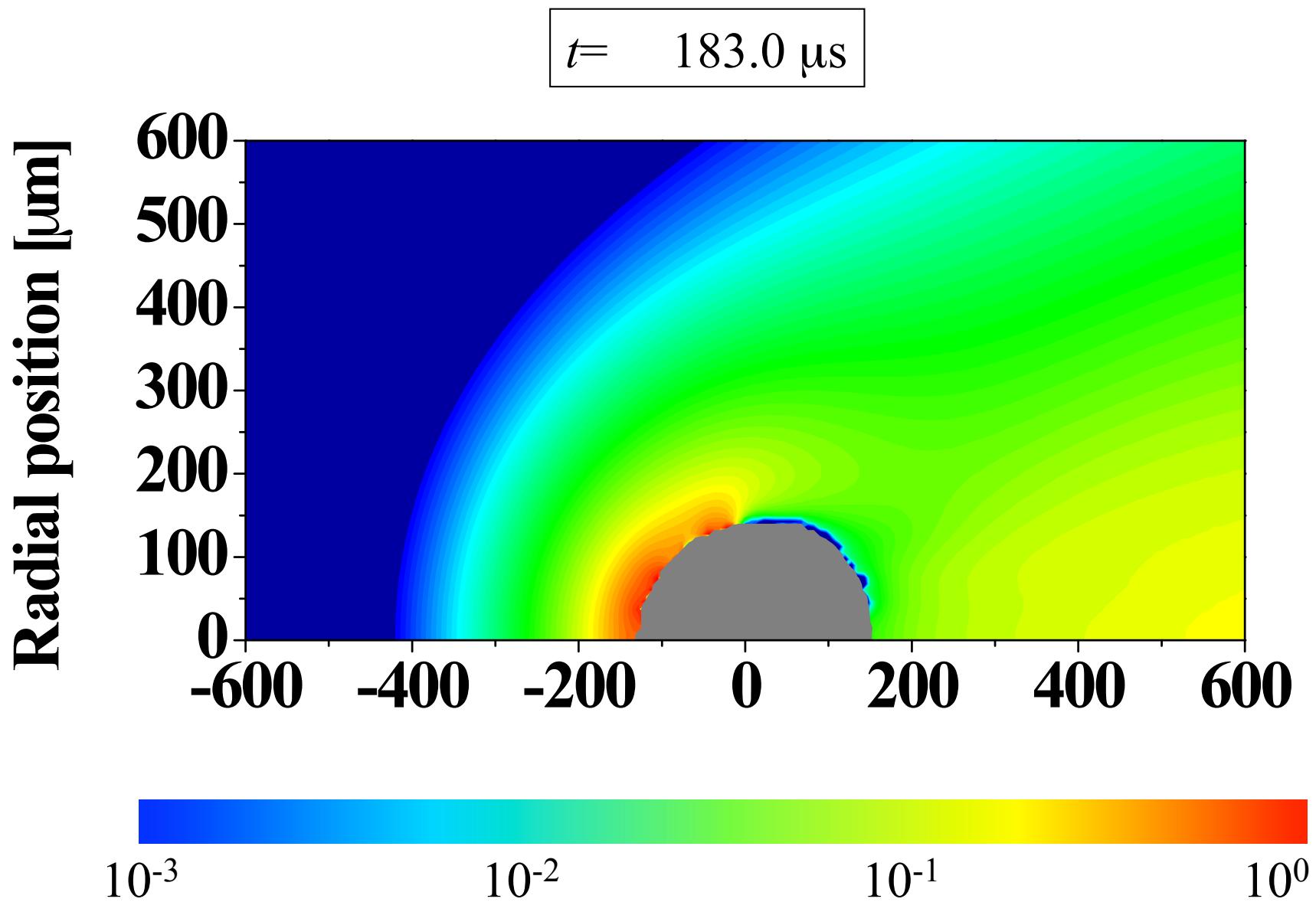
# *Mass fraction of ablated vapor*



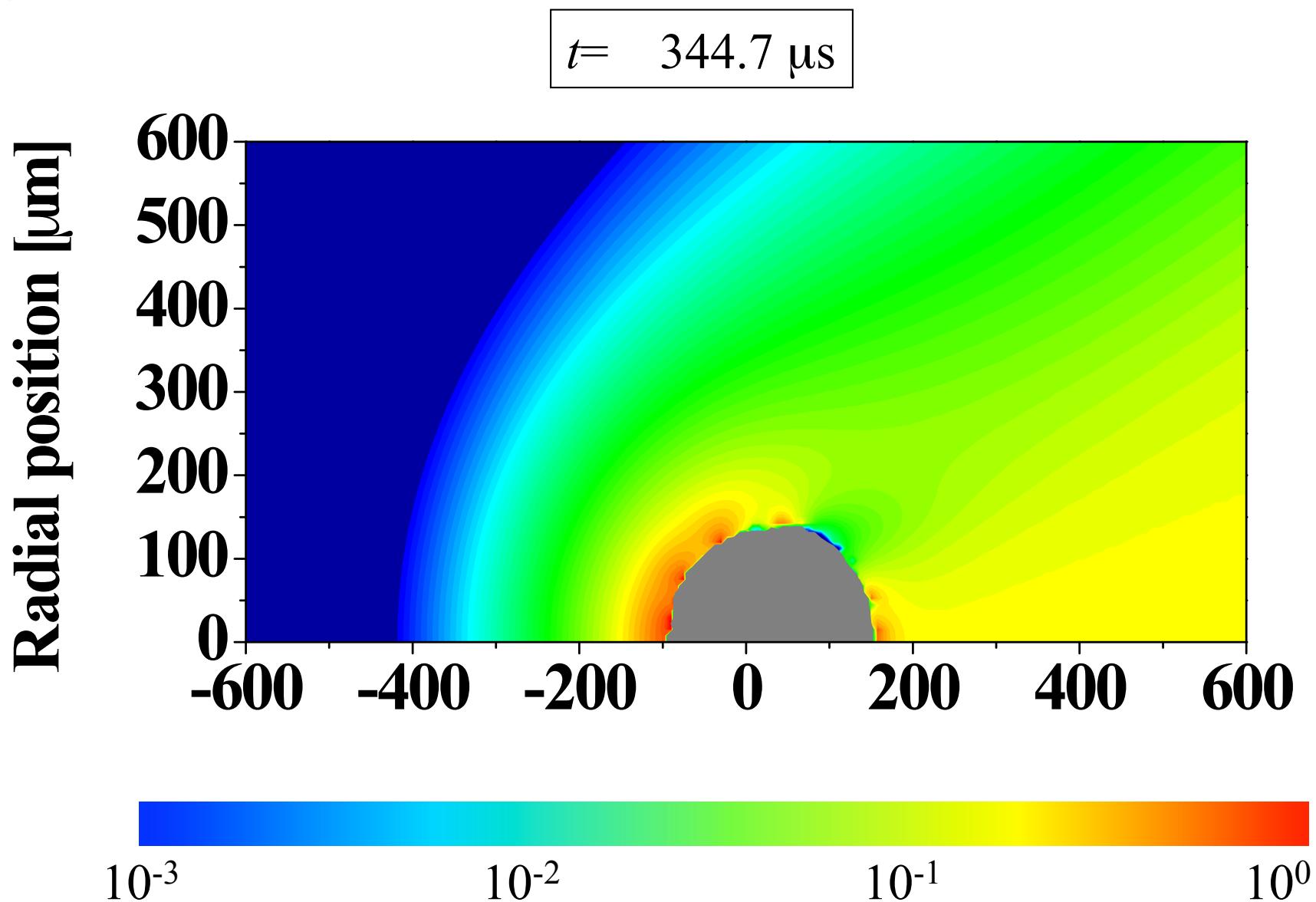
# *Mass fraction of ablated vapor*



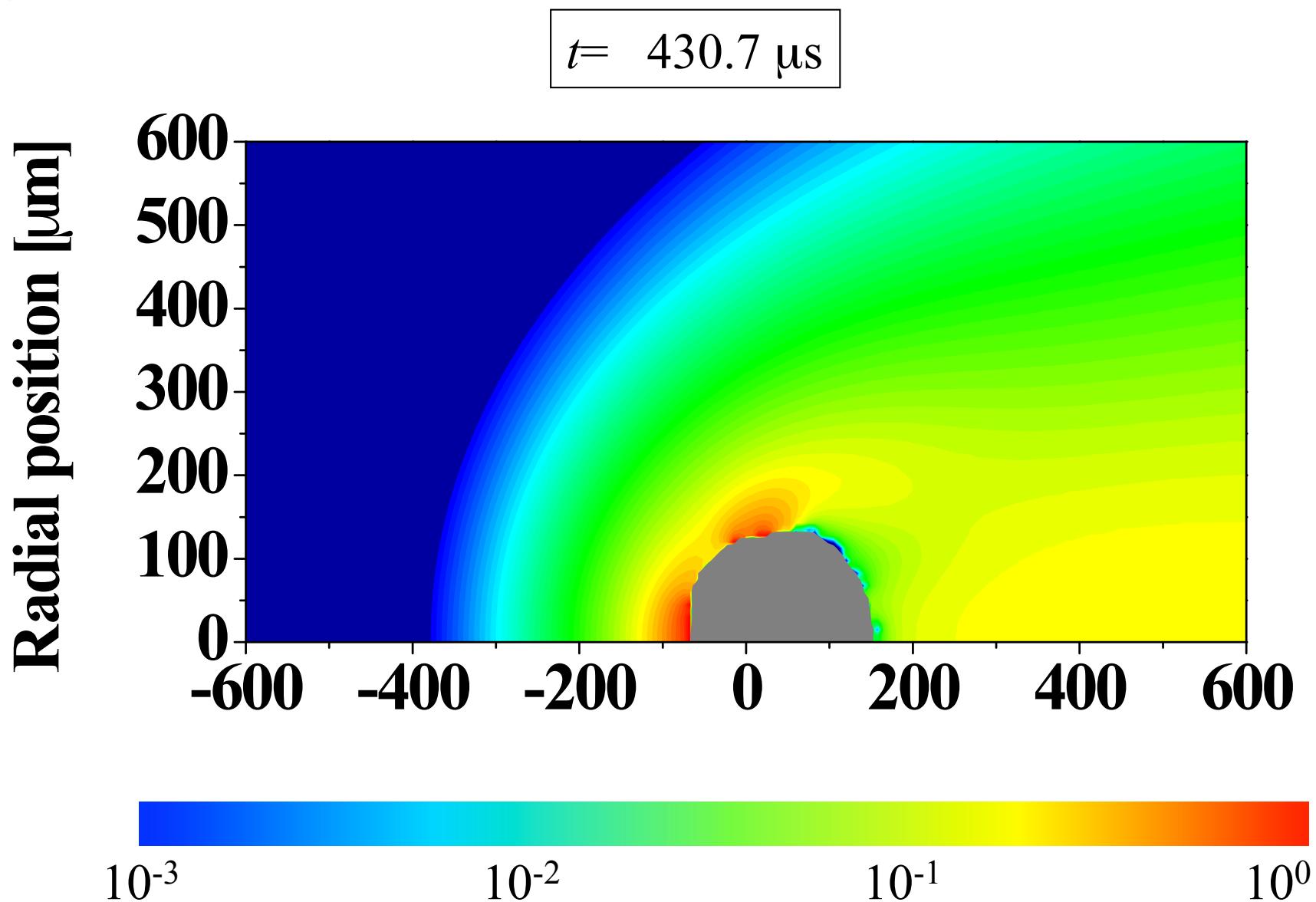
# *Mass fraction of ablated vapor*



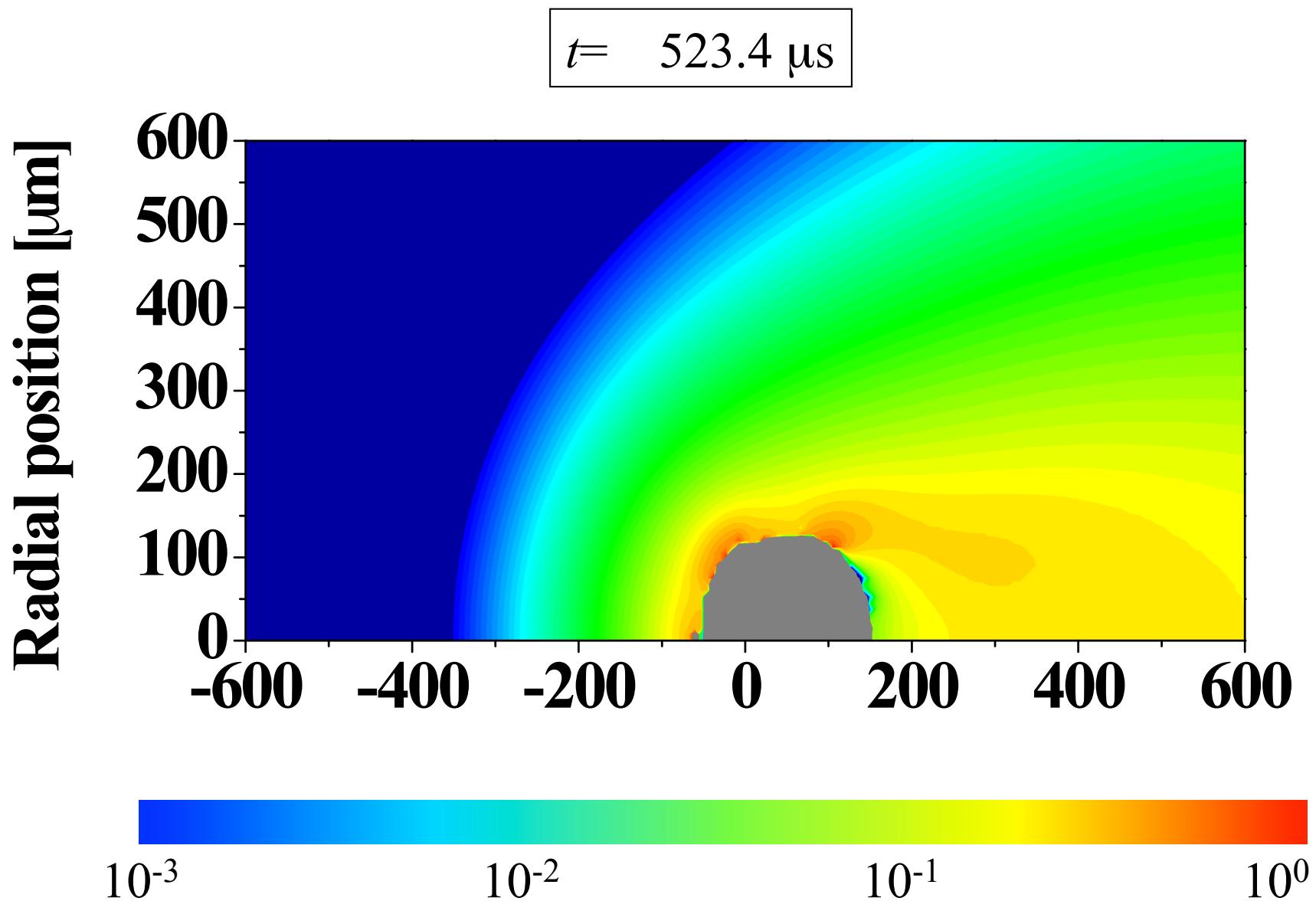
# *Mass fraction of ablated vapor*



# *Mass fraction of ablated vapor*



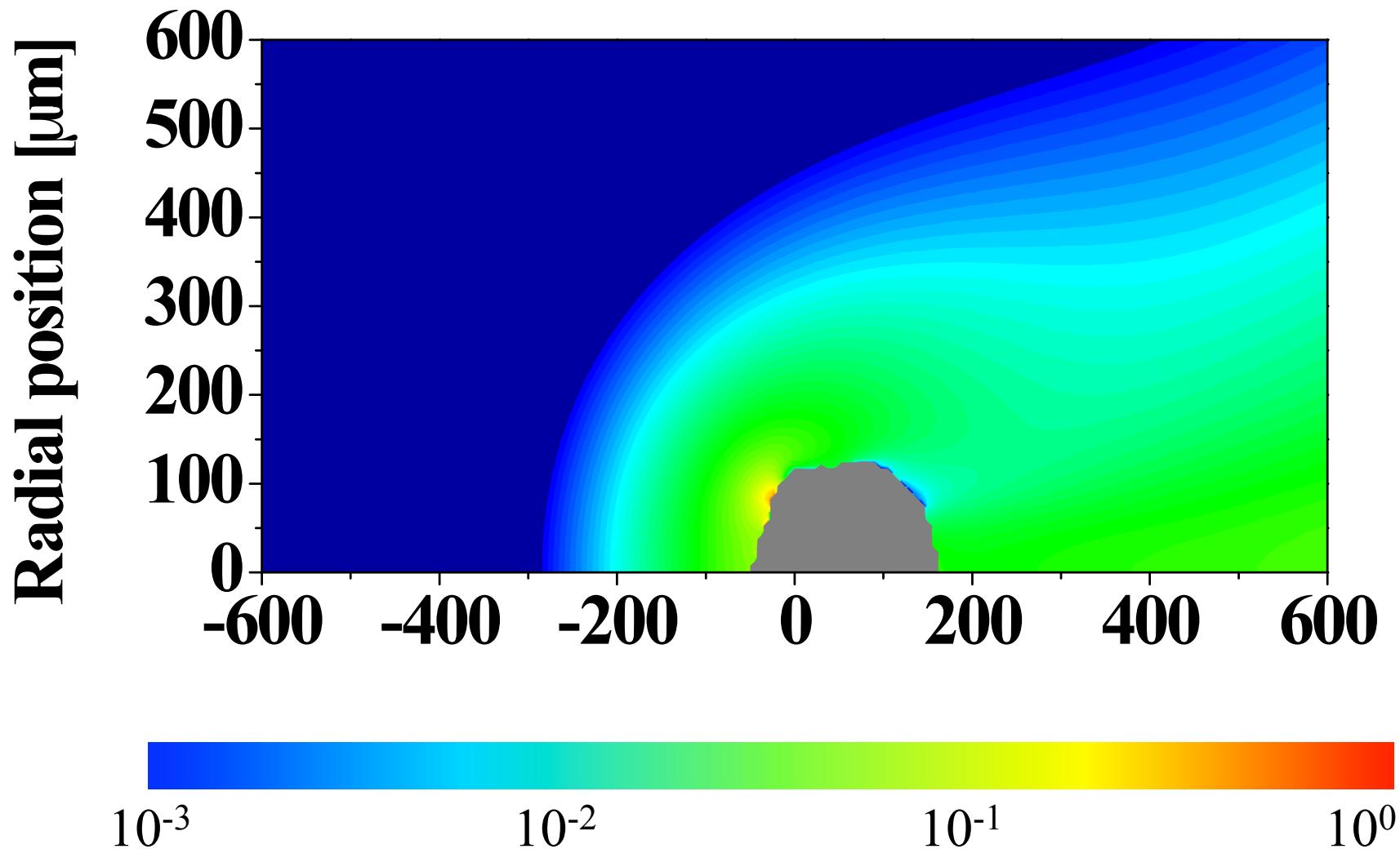
# *Mass fraction of ablated vapor*





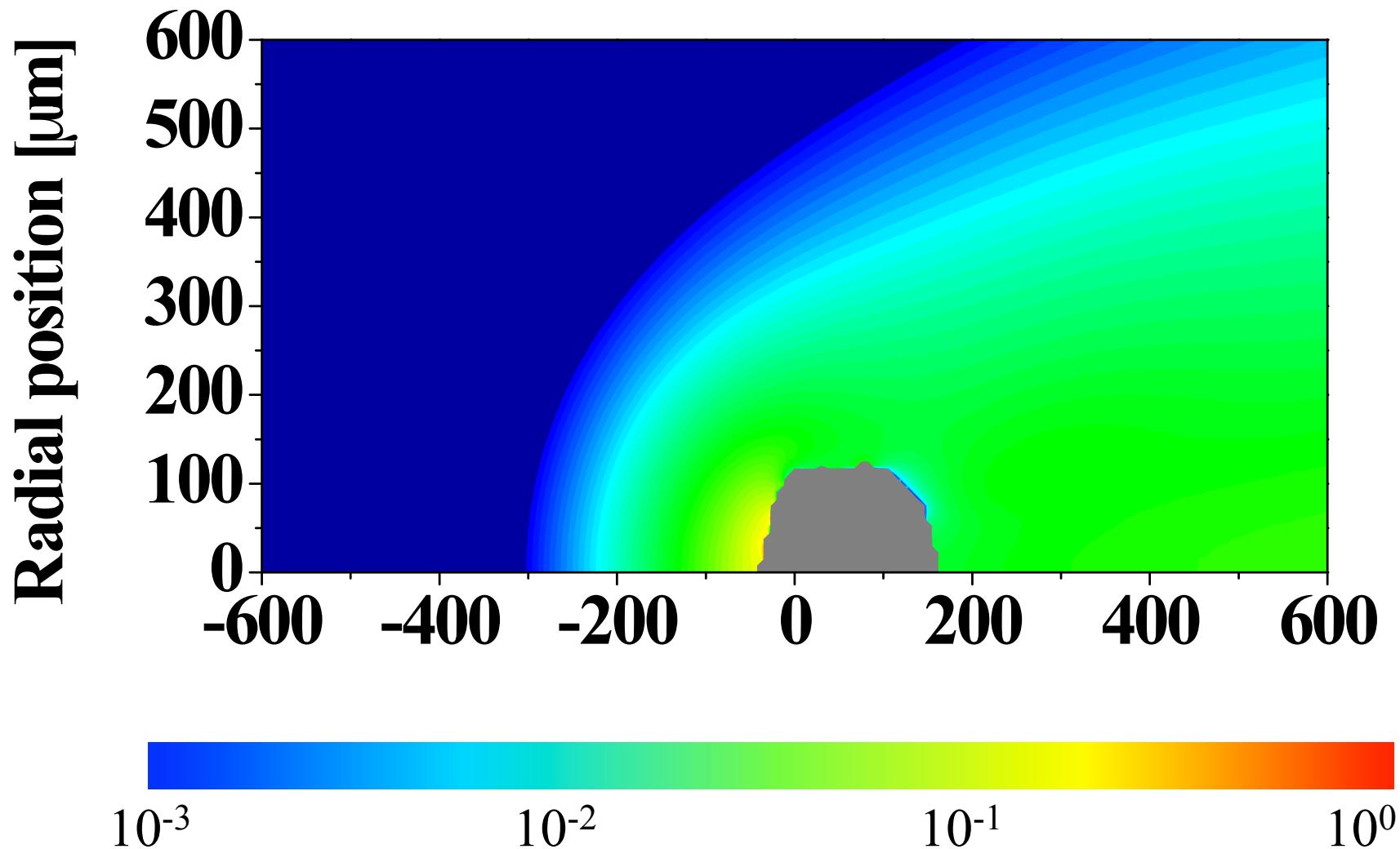
## *Mass fraction of ablated vapor*

$t = 616.51 \mu\text{s}$

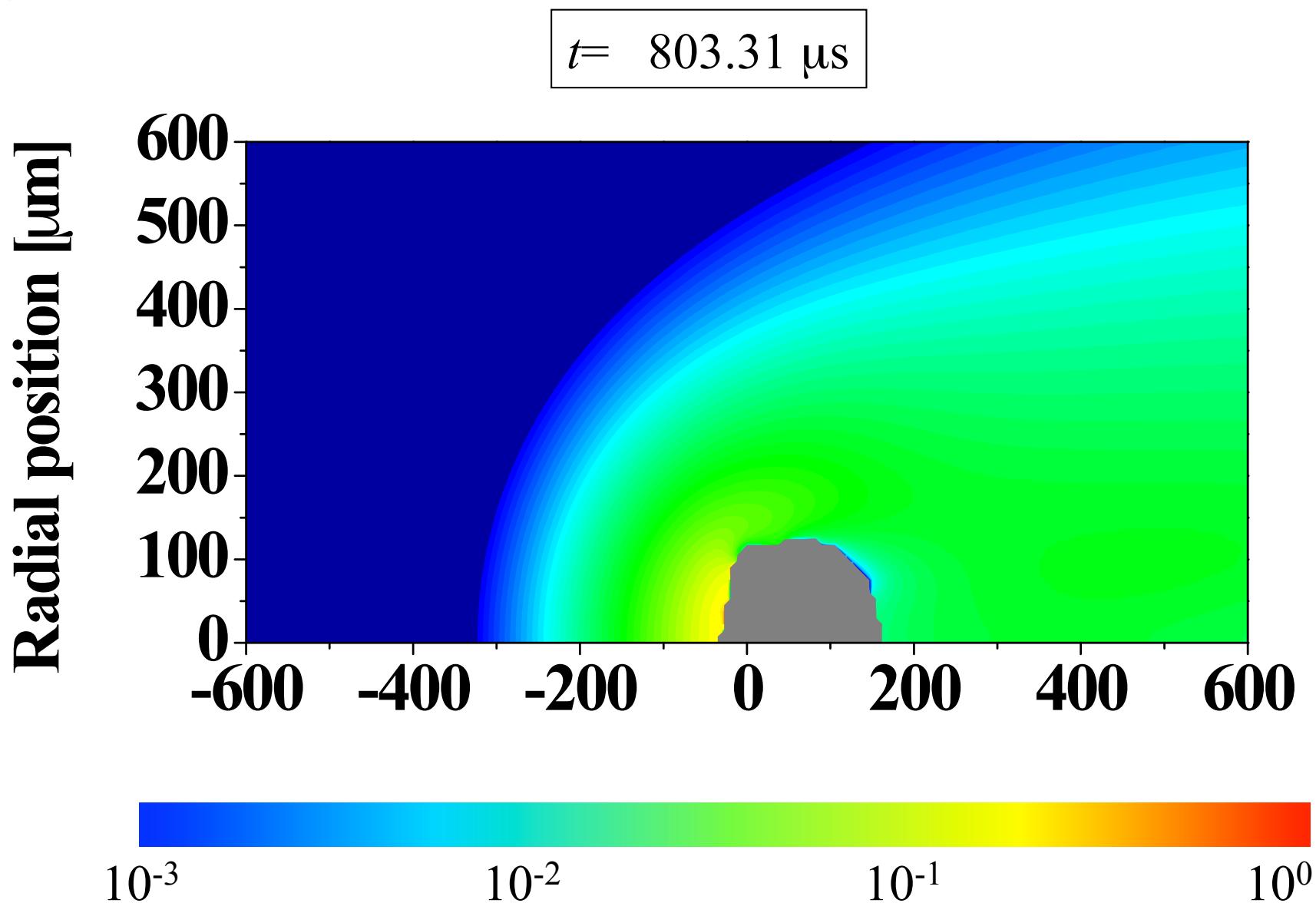


# *Mass fraction of ablated vapor*

$t = 709.89 \mu\text{s}$

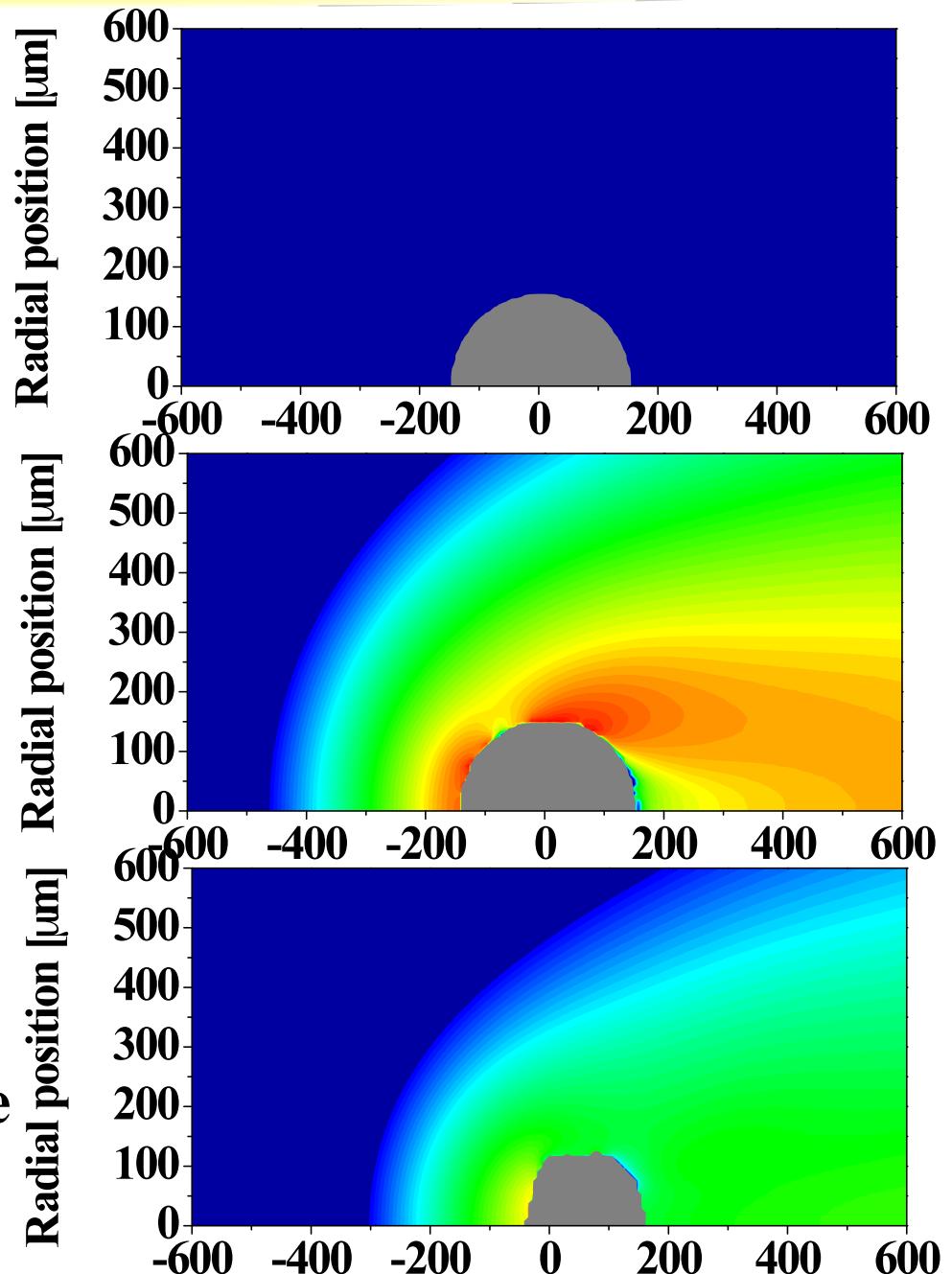


# *Mass fraction of ablated vapor*



## *Transport of ablated vapor and shape change of the particle*

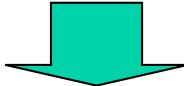
- Ablated vapor is transported by diffusion, and by also convection due to the external Ar gas flow and the gas flow produced by the ablation.
- Rapid ablation especially around upstream of the particle decreases the upstream radius of the particle.
- Lifetime of dust particle was estimated to be 6 times longer than the conventional method without considering temperature decrease around the particle.**



## **Conclusions**

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- The DUSTT code was adopted to a dust particle in plasma of JT-60U configuration.
- Behaviors of carbon dust particles with radii of 1-100  $\mu\text{m}$  from different walls were calculated by solving mass, motion and energy equations.



- Behavior of dust particle is dominated by ion drag force.**
- Dust radius is reduced mainly by thermal sublimation.**

### Future work

- Comparison with experimental data
- Statistical analysis of dust particles with other radii